



## A Small Study of Flatback Airfoils

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# Presentations from the Aeroelastic Workshop – latest results from AeroOpt

## Risø-R-Report



$$\begin{Bmatrix} F_x \\ F_y \\ F_z \\ M_x \\ M_y \\ M_z \end{Bmatrix} = \begin{bmatrix} S_{11} & S_{12} & & S_{14} & & \\ & S_{22} & & & S_{25} & \\ & & S_{33} & & & S_{36} \\ & & & S_{44} & S_{45} & \\ & & & & S_{55} & \\ & & & & & S_{66} \end{bmatrix} \begin{Bmatrix} \varepsilon_x \\ \varepsilon_y \\ \varepsilon_z \\ \kappa_x \\ \kappa_y \\ \kappa_z \end{Bmatrix}$$

Morten Hartvig Hansen (Ed.)  
Risø-R-1769(EN)  
February 2011



**Author:** Morten Hartvig Hansen (Ed.)  
**Title:** Presentations from the Aeroelastic Workshop – latest results from AeroOpt  
**Division:** Wind Energy Division

**Risø-R-1769(EN)**  
**February 2011**

**Abstract (max. 2000 char.):**

This report contains the slides of the presentations at the Aeroelastic Workshop held at Risø-DTU for the wind energy industry in Denmark on January 27, 2011. The scientific part of the agenda at this workshop was

- Anisotropic beam element in HAWC2 for modelling of composite lay-ups (Taeseong Kim)
- Nonlinear beam element in HAWC2 for modelling of mooring systems (Bjarne Kallesøe)
- Enhanced BEM including wake expansion and swirl (Christian Bak)
- Unsteady viscous-inviscid interactive airfoil code for wind turbines (Néstor Ramos García)
- PIV measurements on model scale wind turbine in water channel (Robert Mikkelsen)
- Potential of fatigue and extreme load reductions on swept blades using HAWC2 (David Verelst)
- Aeroelastic modal analysis of backward swept blades using HAWCStab2 (Morten H. Hansen)
- Aeroelastic rotor design minimizing the loads (Christian Bak)
- A small study of flat back airfoils (Niels N. Sørensen)
- Status of airfoil design and plans for wind tunnel tests of new thick airfoils (Christian Bak)

The presented results are mainly obtained in the EUDP project “Aeroelastic Optimization of MW Wind Turbines (AeroOpt)” funded under contract no. 63011-0190.

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## Preface

This report contains the slides of the presentations at the Aeroelastic Workshop held at Risø-DTU for the wind energy industry in Denmark on January 27, 2011. The scientific part of the agenda at this workshop was

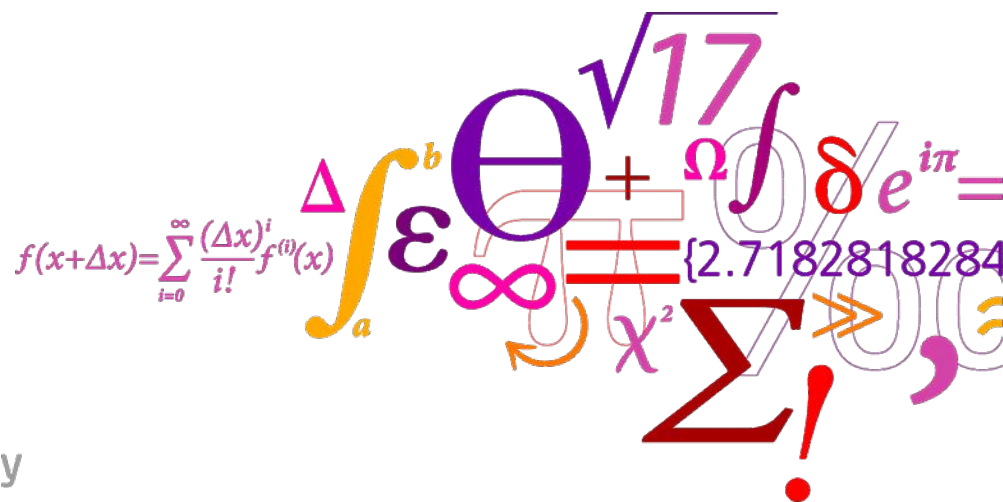
- Anisotropic beam element in HAWC2 for modelling of composite lay-ups (Taeseong Kim)
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# **1 Anisotropic beam element**

# Anisotropic Beam Element in HAWC2 for Modeling of Composite lay-ups

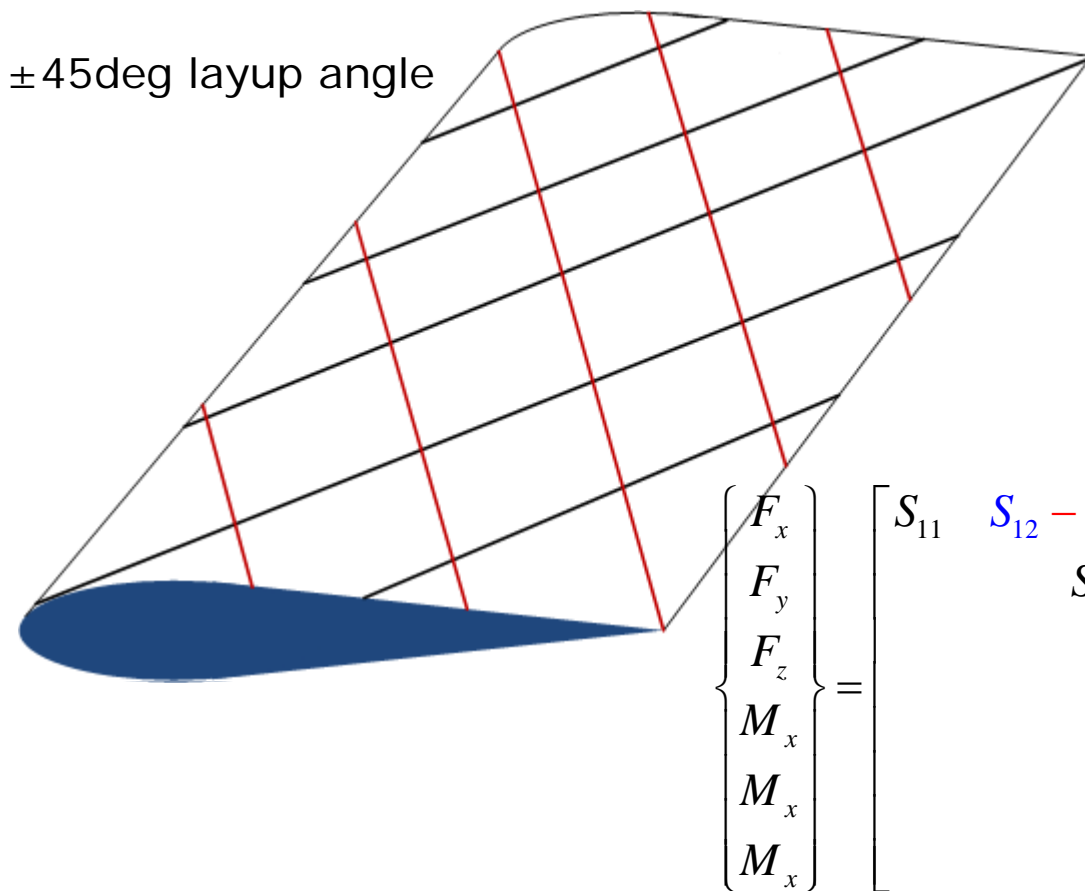
Taeseong Kim



# Introduction

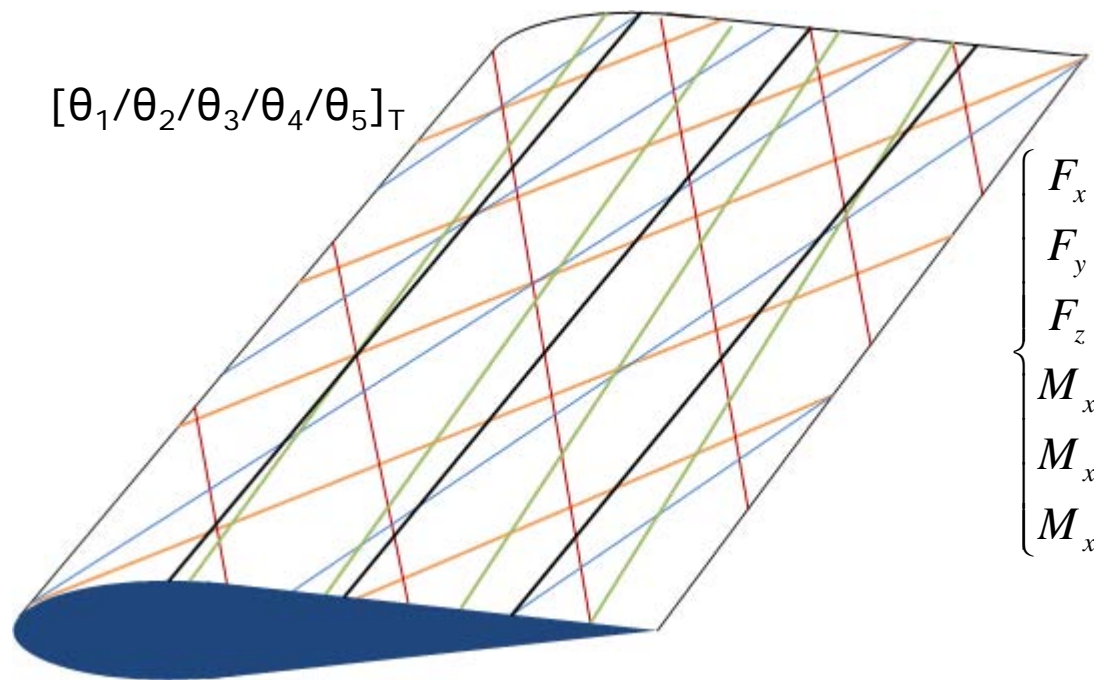
- All of composite blades have anisotropic material properties due to different layup angles.
  - It introduces additional bending-bending and bending-twist couplings.
- The existing beam model in HAWC2 is capable for modeling of geometric couplings e.g the offset between elastic axis and shear center
  - The offset introduces the bending and torsion couplings
- Aeroelastic codes such as HAWC2, Bladed, FAST, and Flex are using classical engineering beam models.
- Classical beam models are derived by assuming isotropic material beam properties.
  - Anisotropic material properties of composite beam cannot be modeled with those classical beam models.

# Typical layup conditions



$$\begin{bmatrix} S_{11} & S_{12} - S_{12} = 0 & S_{13} \\ S_{22} & S_{23} & S_{24} \\ S_{33} & S_{34} & S_{35} \\ S_{44} & S_{45} - S_{45} = 0 & S_{46} \\ S_{55} & S_{56} & S_{57} \\ S_{66} & S_{67} & S_{68} \end{bmatrix} \begin{Bmatrix} \epsilon_x \\ \epsilon_y \\ \epsilon_z \\ \kappa_x \\ \kappa_y \\ \kappa_z \end{Bmatrix}$$

# Possible new layup conditions



$[\theta_1/\theta_2/\theta_3/\theta_4/\theta_5]_T$

$$\begin{Bmatrix} F_x \\ F_y \\ F_z \\ M_x \\ M_x \\ M_x \end{Bmatrix} = \begin{bmatrix} S_{11} & \textcolor{brown}{S}_{12} & & & & \\ & S_{22} & & & & \\ & & S_{33} & & & \\ & & & S_{44} & & \\ & & & & \textcolor{brown}{S}_{45} & \\ & & & & S_{55} & \\ & & & & & S_{66} \end{bmatrix} \begin{Bmatrix} \epsilon_x \\ \epsilon_y \\ \epsilon_z \\ \kappa_x \\ \kappa_y \\ \kappa_z \end{Bmatrix}$$

$S_{11}$  (black),  $\textcolor{brown}{S}_{12}$  (brown),  $S_{22}$  (black),  $S_{33}$  (black),  $\textcolor{blue}{S}_{14}$  (blue),  $\textcolor{green}{S}_{25}$  (green),  $\textcolor{red}{S}_{36}$  (red),  $S_{44}$  (black),  $\textcolor{brown}{S}_{45}$  (brown),  $S_{55}$  (black),  $S_{66}$  (black)

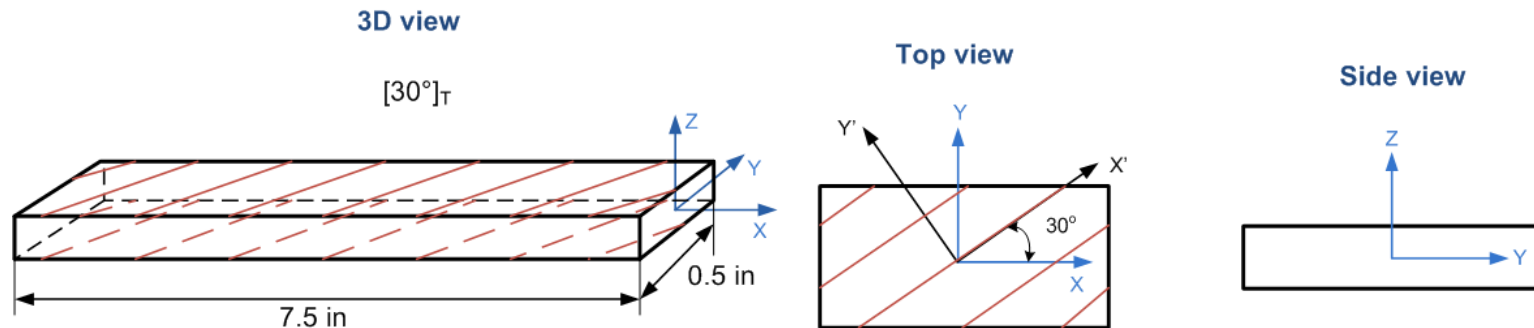
- To analyze anisotropic composite blade ***anisotropic beam model*** should be introduced.

# Method

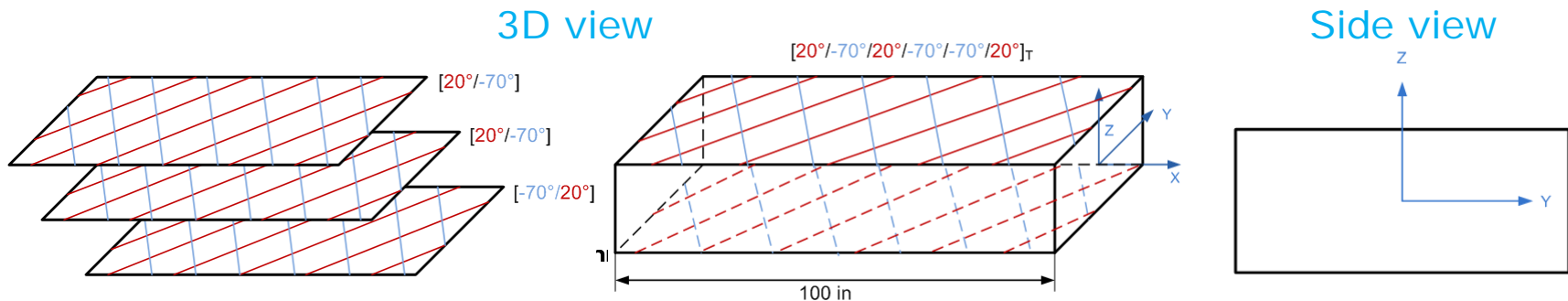
- General FEM approach is considered to develop new a Timoshenko beam model.
- 2 nodes element is fixed for structural elements.
  - 2 nodes element is used for aerodynamic elements.
  - Linear shape function is available.
  - Linear shape function needs to have more elements.
  - Time cost is increased.
- 2 nodes element with higher order of the polynomial shape function is developed.
- Steady deflections are compared.
- Natural frequencies (Hz) for box beams are compared.
- Mode shapes are compared.
- Cross-sectional stiffness and mass matrix are given from the references.

# Cases

- CASE 1: Wenbin Yu (2007)
  - Length of the beam: 7.5 in
  - Graphite-Epoxy  $[30^\circ]_T$ , rectangular box beam



- CASE 2: Hodges *et al.* (1991)
  - Length of the beam: 100 in
  - Graphite-Epoxy  $[20^\circ/-70^\circ/20^\circ/-70^\circ/-70^\circ/20^\circ]_T$ , rectangular box beam

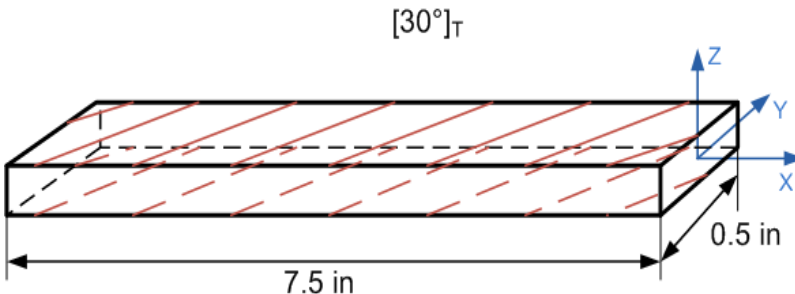




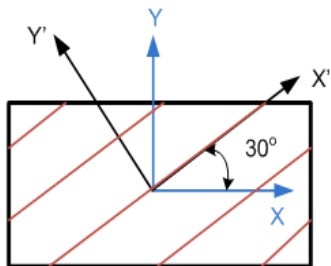
# Results (case 1)

- Graphite-Epoxy  $[30^\circ]_T$  , rectangular box beam

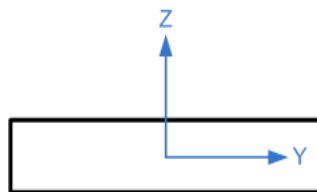
3D view



Top view



Side view

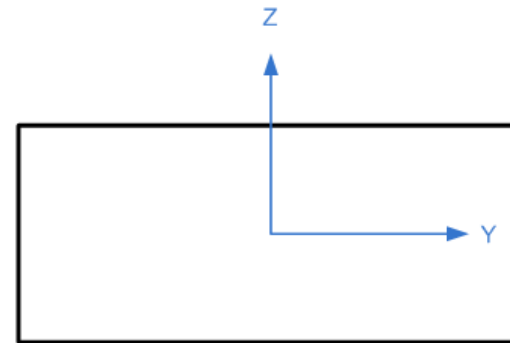
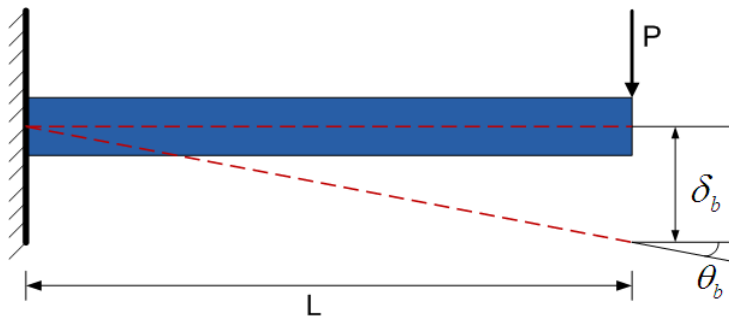


- The material properties and the dimensions of the structure

$E_{11}$	$18.73 \times 10^6$ psi
$E_{22}, E_{33}$	$1.364 \times 10^6$ psi
$G_{12}$	$0.7479 \times 10^6$ psi
$G_{13}$	$0.6242 \times 10^6$ psi
$G_{23}$	$0.3686 \times 10^6$ psi
$\nu_{12}, \nu_{13}, \nu_{24}$	0.3
$\rho$	$1.450 \times 10^{-4}$ lb.sec <sup>2</sup> /in. <sup>4</sup>
Width	0.5 in
Thickness	0.125 in
Length	7.5 in

# Static analysis with cantilever beam (case 1)

- 2 nodes with 6th order polynomial



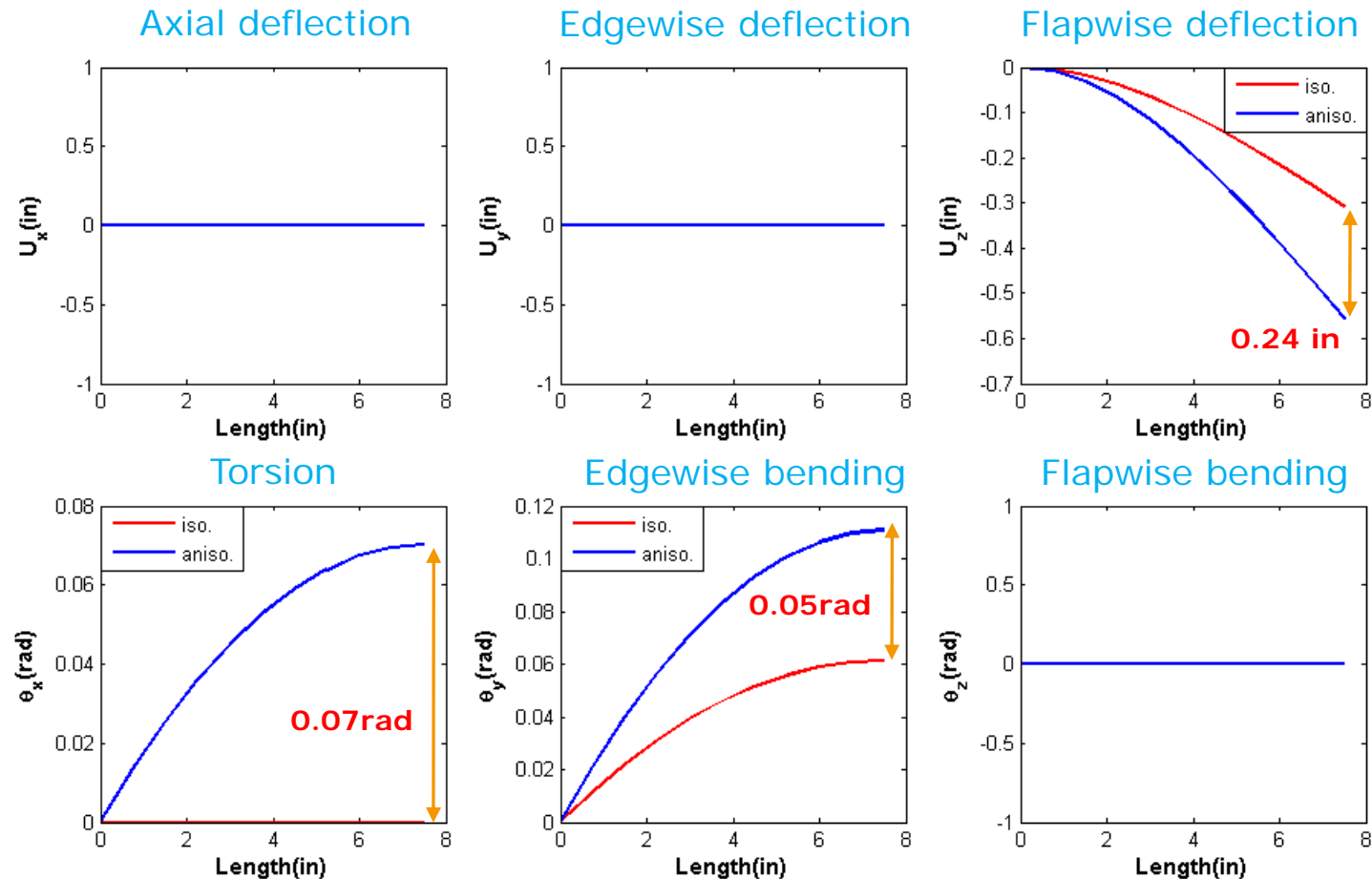
where  $L = 7.5\text{in}$ ,  $P = -1\text{lb}$

$$[s] = \begin{bmatrix} S_{11} & S_{12} & 0 & 0 & 0 & 0 \\ S_{12} & S_{22} & 0 & 0 & 0 & 0 \\ 0 & 0 & S_{33} & 0 & 0 & 0 \\ 0 & 0 & 0 & S_{44} & S_{45} & 0 \\ 0 & 0 & 0 & S_{45} & S_{55} & 0 \\ 0 & 0 & 0 & 0 & 0 & S_{66} \end{bmatrix}$$

- Anisotropic stiffness properties
  - No coupling in direction
  - Torsion-flapwise bending

# Static analysis with cantilever beam (case 1)

- 2 nodes with 6th order polynomial



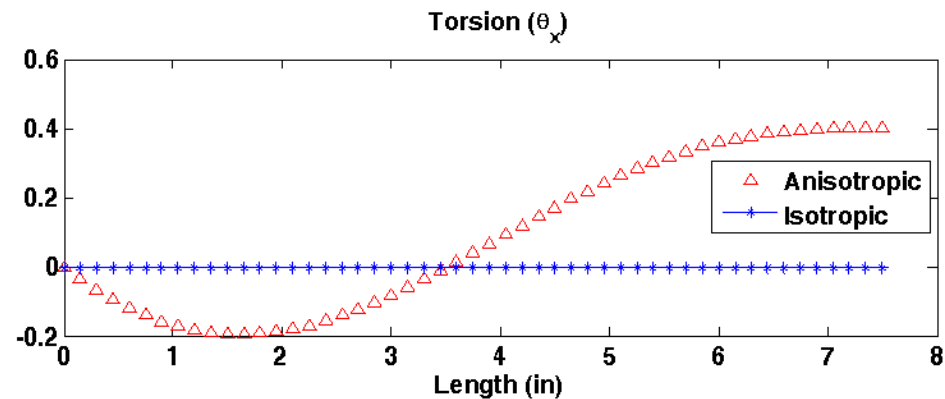
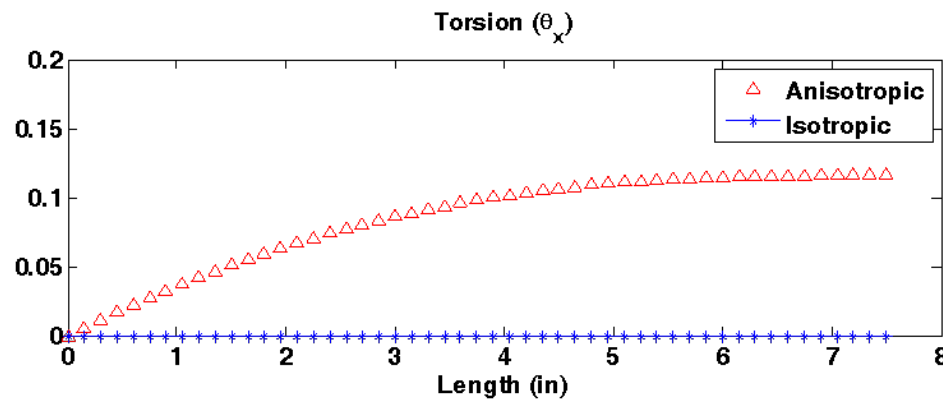
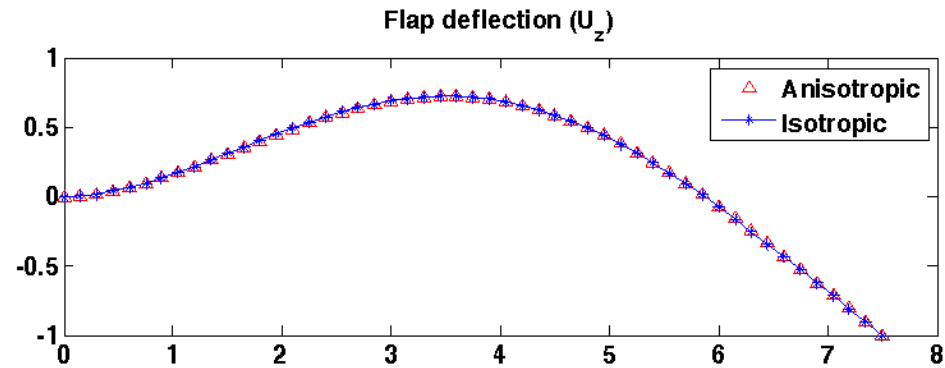
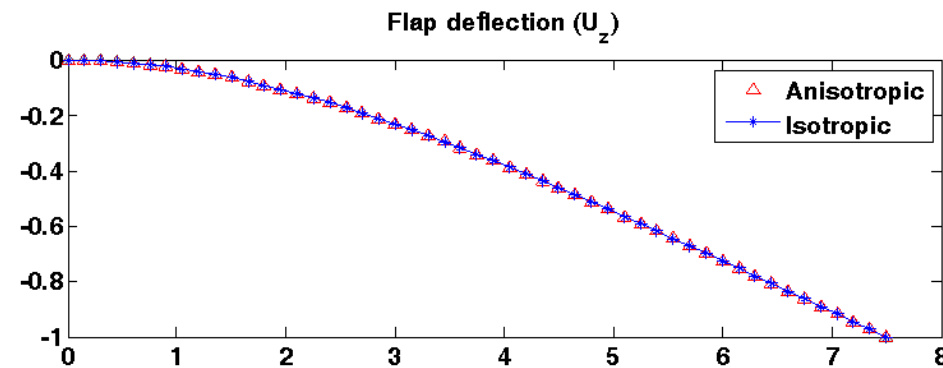
# Comparisons of the natural frequencies (case 1)

Mode	Isotropic [Hz]	Anisotropic [Hz]
1 (Flap)	70.6	52.6
2 (Edge)	210.3	209.9
3 (Flap)	436.5	327.3
4 (Flap)	1197.9	906.7
5 (Edge)	1304.8	1292.5
6 (Flap)	2282.9	1752.9

# Comparisons of the mode shapes (case 1)

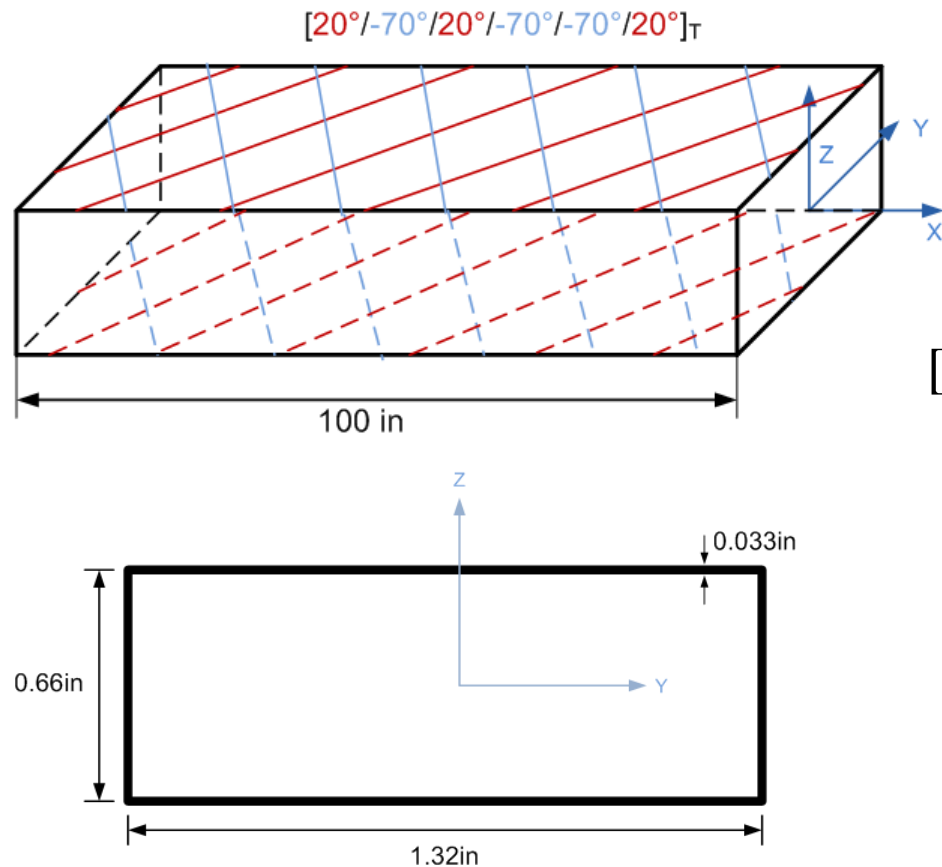
1st Flap mode

2nd Flap mode



## Results (case 2)

- Graphite-Epoxy  $[20^\circ/-70^\circ/20^\circ/-70^\circ/-70^\circ/20^\circ]_T$ , rectangular box beam

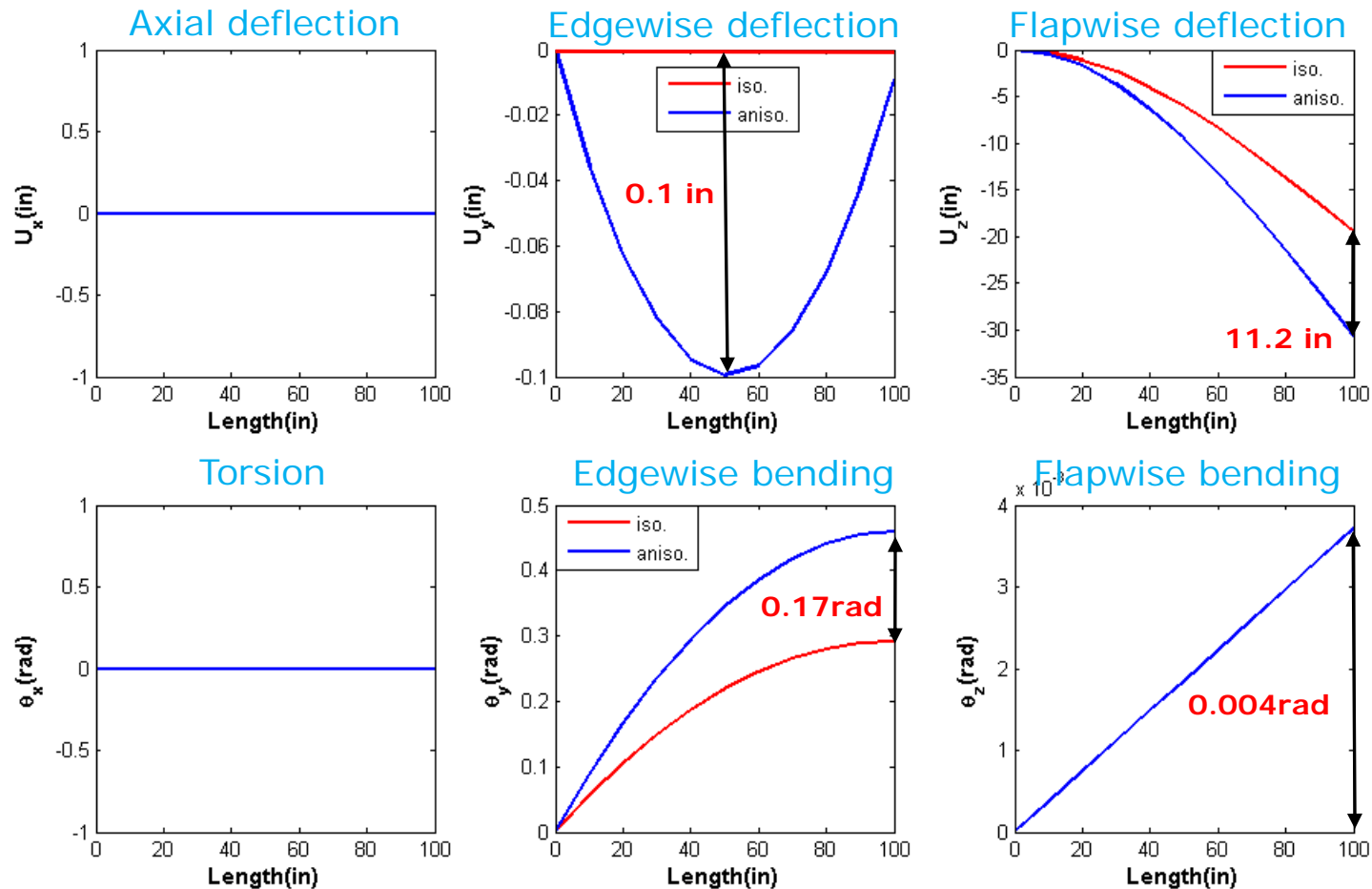


$$[s] = \begin{bmatrix} S_{11} & 0 & 0 & S_{14} & 0 & 0 \\ 0 & S_{22} & 0 & 0 & S_{25} & 0 \\ 0 & 0 & S_{33} & 0 & 0 & S_{36} \\ S_{14} & 0 & 0 & S_{44} & 0 & 0 \\ 0 & S_{25} & 0 & 0 & S_{55} & 0 \\ 0 & 0 & S_{36} & 0 & 0 & S_{66} \end{bmatrix}$$

where  $[s]$ : sectional stiffness matrix

# Static analysis with cantilever beam (case 2)

- 2 nodes with 6th order polynomial



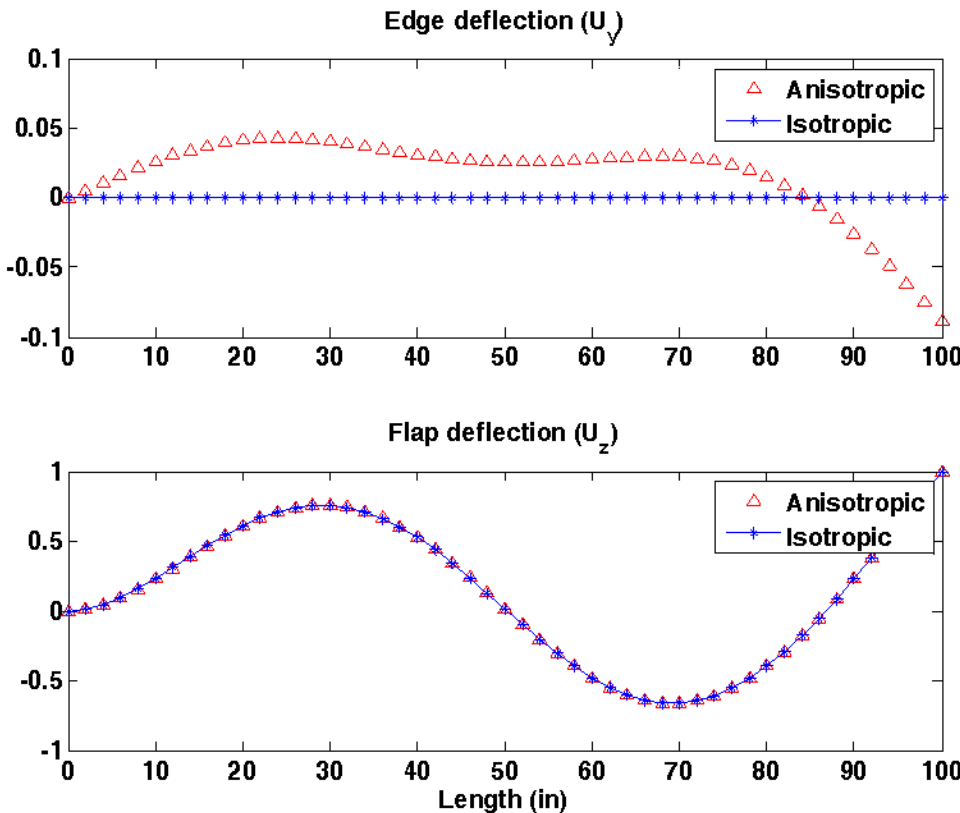
# Comparisons of the natural frequencies (case 2)

	Isotropic [Hz]	Anisotropic [Hz]
1 (Flap)	3.69	2.95
1 (Edge)	6.43	5.09
2 (Flap)	23.12	18.44
2 (Edge)	40.23	31.84
3 (Flap)	64.53	51.59
3 (Edge)	112.22	87.95

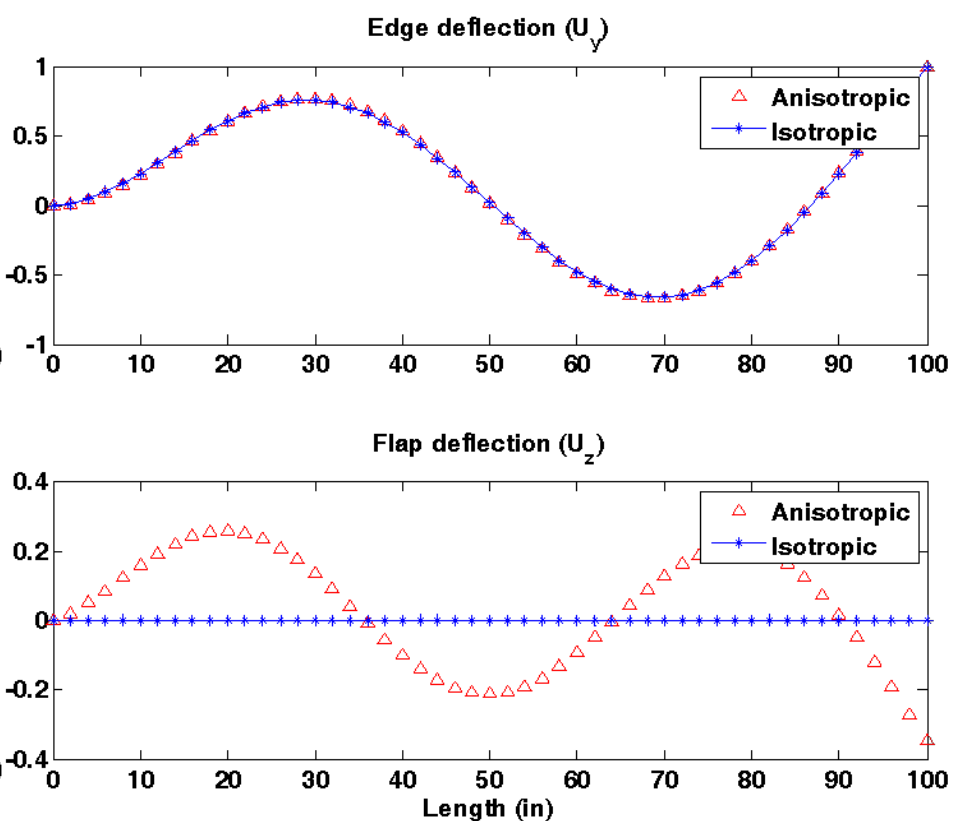


# Comparisons of the mode shapes (case 2)

3rd Flap mode



3rd Edge mode



# Conclusions

- Steady deflections for isotropic and anisotropic cases
  - Anisotropic beam deflects more than isotropic beam.
- Natural frequencies
  - Natural frequencies with isotropic material are higher than the frequencies for anisotropic material.
- Mode shapes
  - More coupling effects are illustrated when anisotropic materials are considered.
    - For the case 1, torsion mode is coupled with flap mode.
    - For the case 2, edge mode is coupled with flap mode.

# Future works

- Future works
  - New element is going to be added in HAWC2.
  - More validations
    - Simple static analysis
    - Dynamic analysis
  - Tailoring study
    - Designing composite blade
- What are the effects of anisotropic beam properties on loads ????

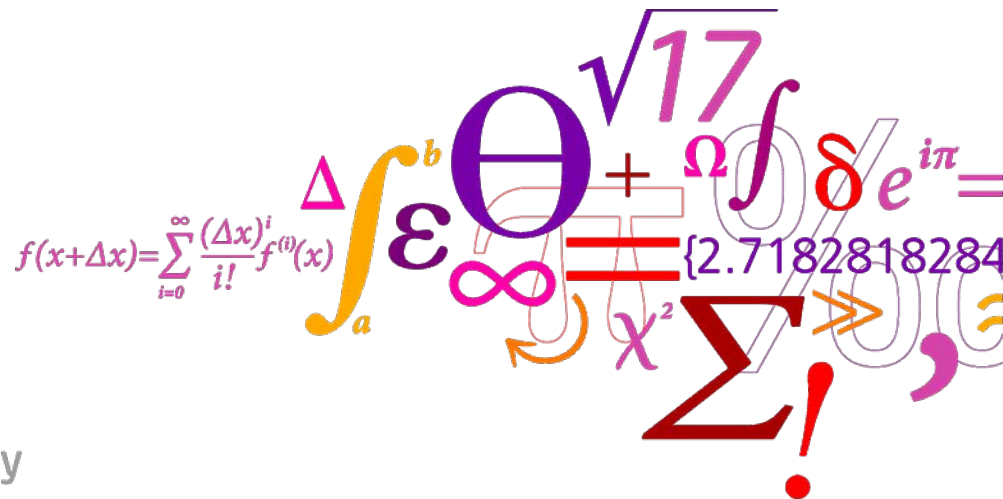
Thank you for your attention

## **2 Nonlinear beam element**

# Nonlinear beam element in HAWC2 for modeling of mooring systems

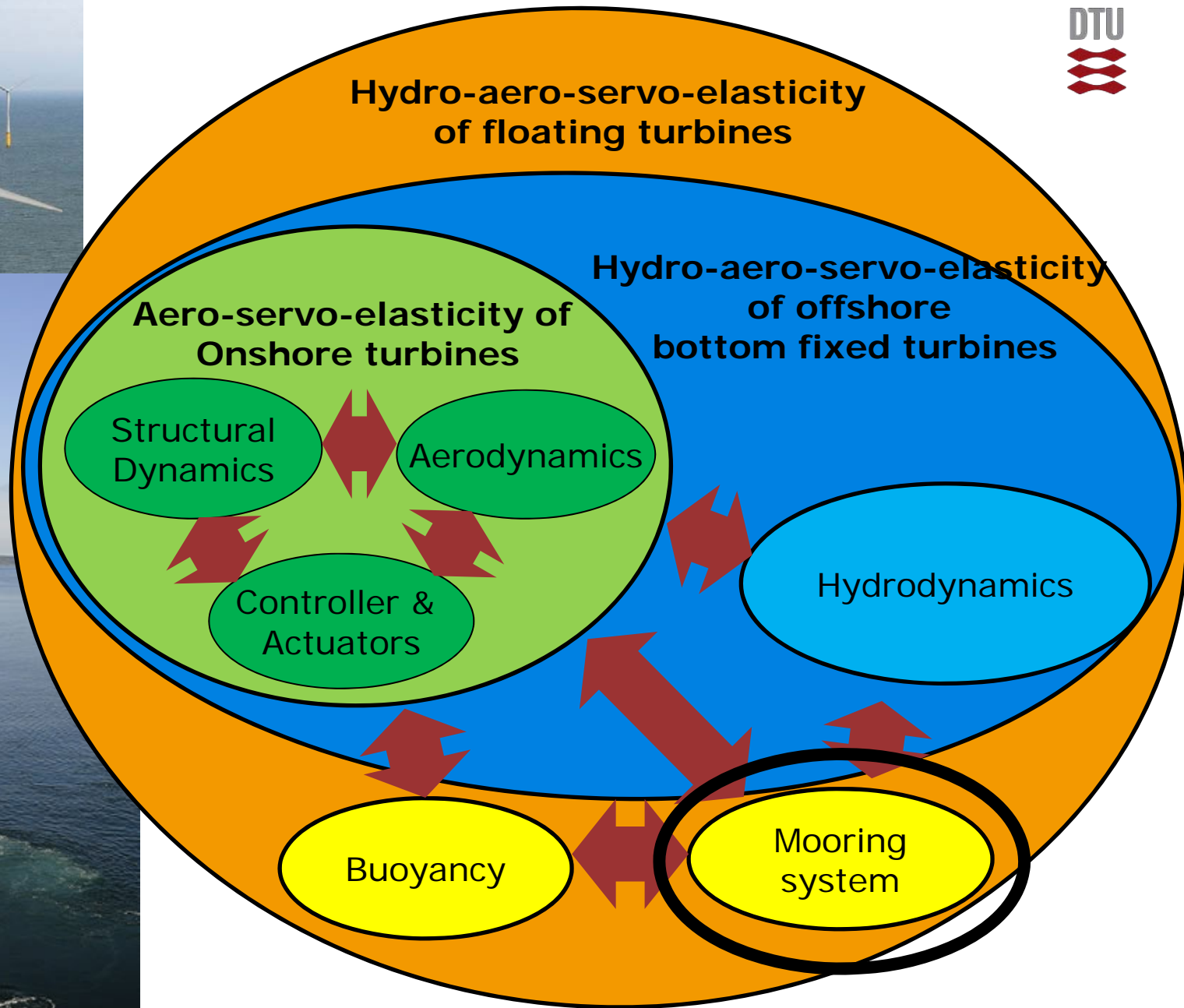
Bjarne S. Kallesøe, Risø DTU

Anders M. Hansen, Siemens Wind Power A/S



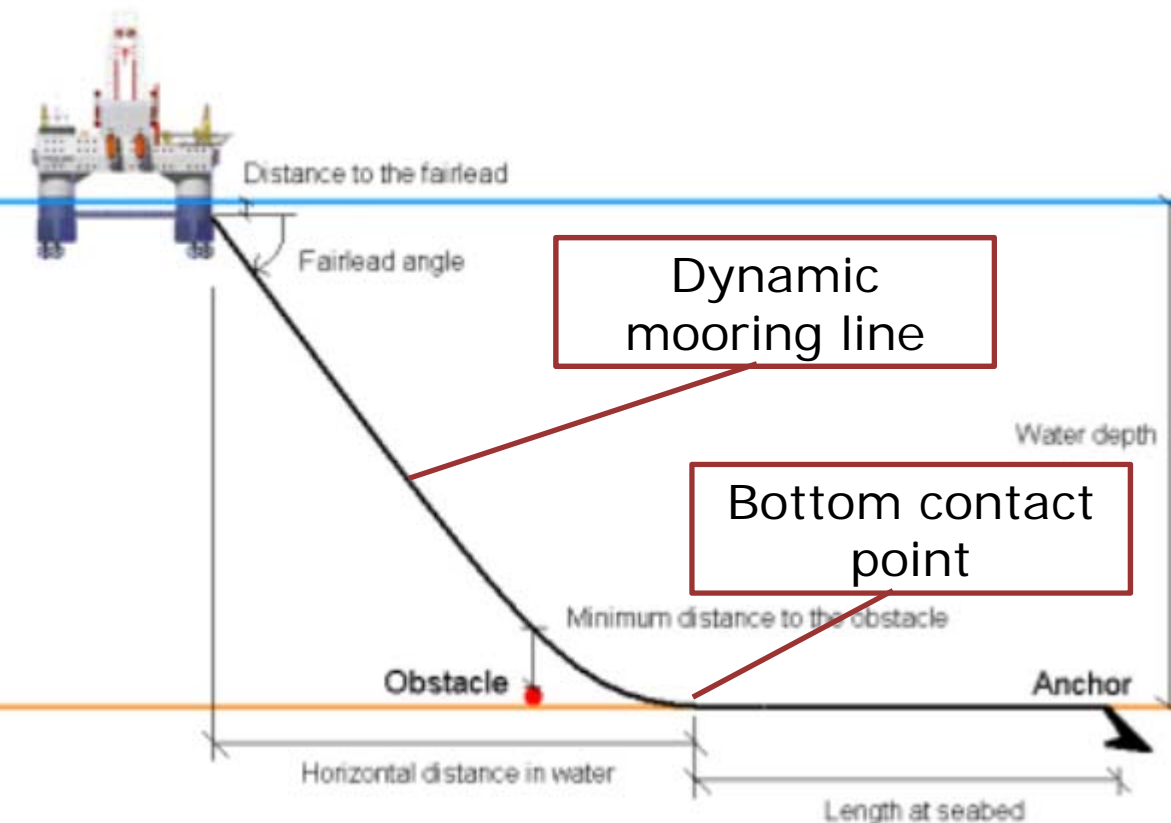
# Background and motivation

- Increasing focus on floating turbine concepts
- Mooring system an integrated part of the overall system dynamic
- Present mooring modeling in HAWC2
  - Quasi-static nonlinear stiffness based on pre-computed mooring line characteristic
  - Pros
    - Fast computations, based on well known mooring model
  - Cons
    - Quasi-static, symmetric mooring forces, complicated modeling based on external program
- Develop new mooring system model that:
  - Includes dynamic mooring lines to:
    - Analyze the effect and importance of such on overall system dynamic
    - Analyze loads on mooring systems
  - Is capable of modeling different mooring layouts





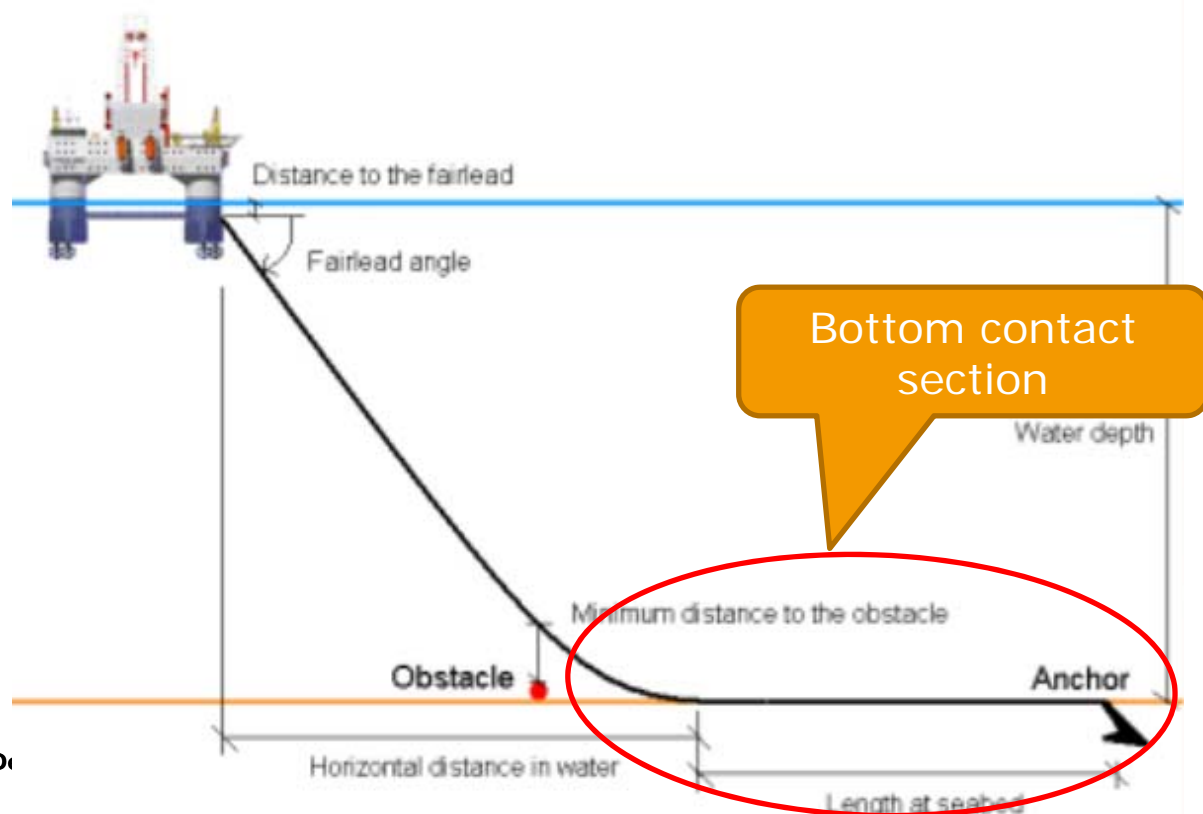
# Mooring system



- Modeling split into two sections:
  - 1) Bottom contact section; 2D inelastic quasi-static solution to determine bottom connection point
  - 2) Dynamic mooring line section; nonlinear element with longitudinal flexibility and no bending stiffness. Includes drag, buoyancy and concentrated masses

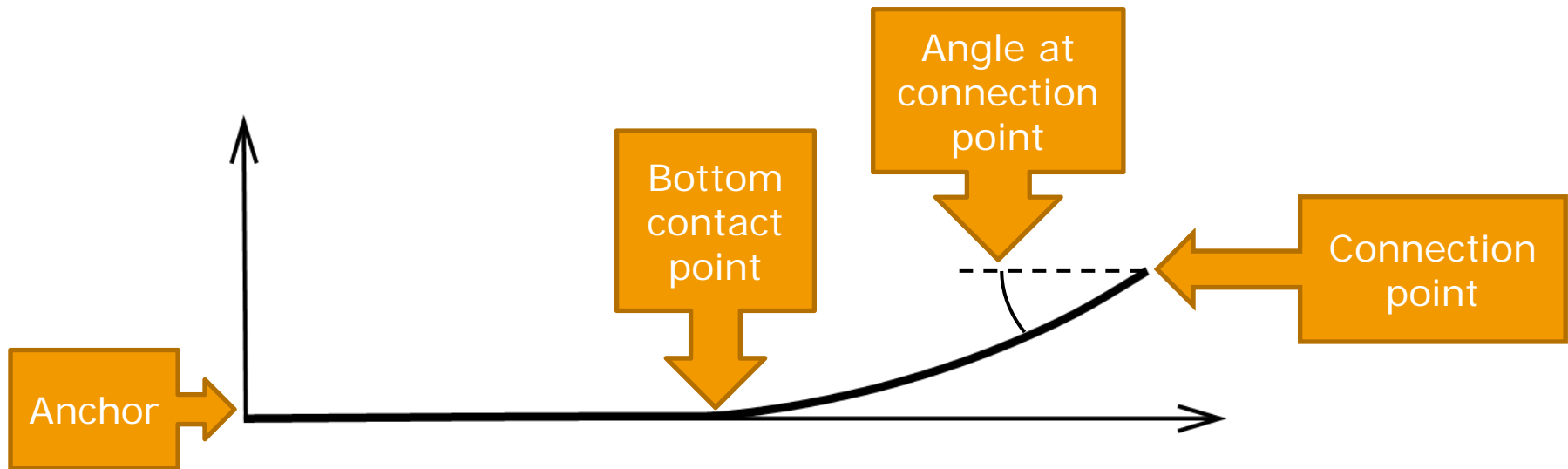
# Bottom contact section

- Bottom section model quasi-static in 2D, determine the radius to bottom contact point and the height and radius at the connection point to the mooring line
- Highly nonlinear problem



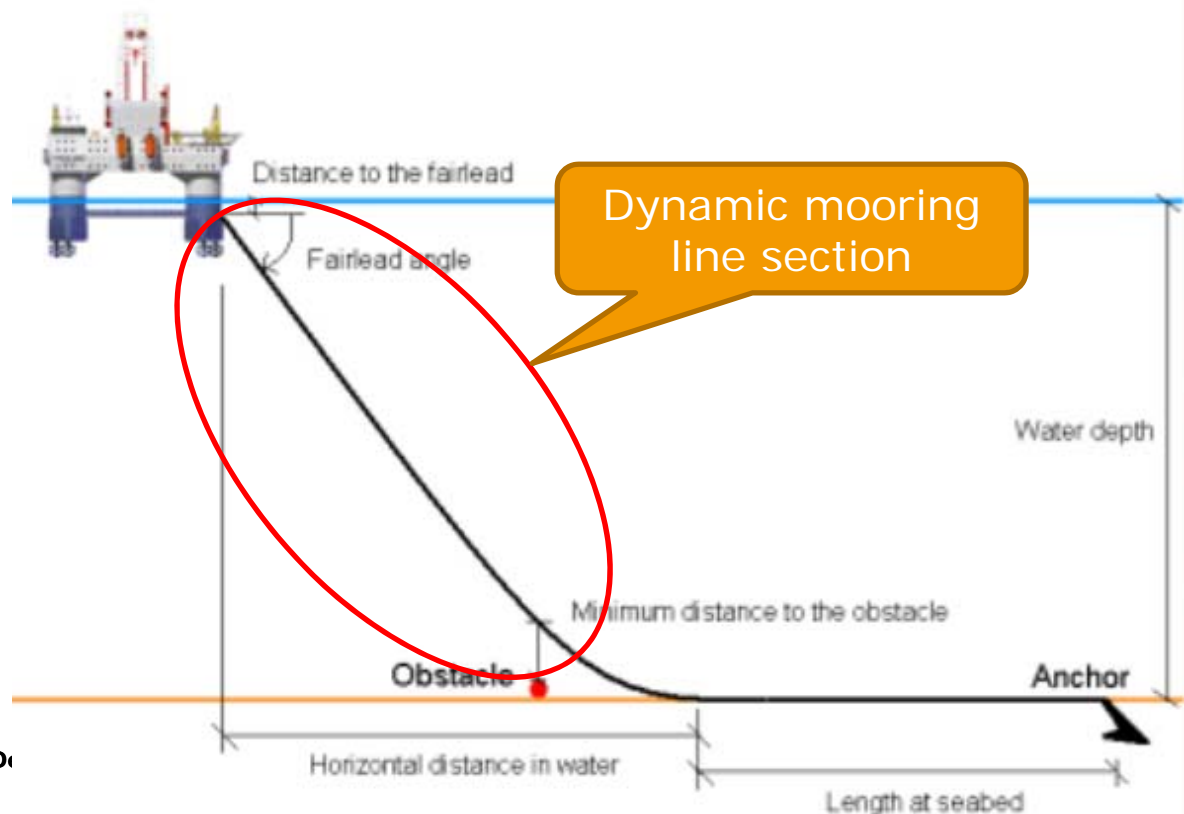
# Bottom contact section

- Problem: given a connection point from the main solver, find the bottom contact point, line force and angle at connection point
- Solution scheme
  1. Get a guess on connection point from main solver
  2. Compute the bottom contact point by an iterative solution of the quasi-static equilibrium between free anchor chain and angle at connection point
  3. Compute vertically line force component by weight of floating anchor chain
  4. Compute horizontal line force component by angle at connection point
  5. Return line forces as residual of unconstrained equations to main solver



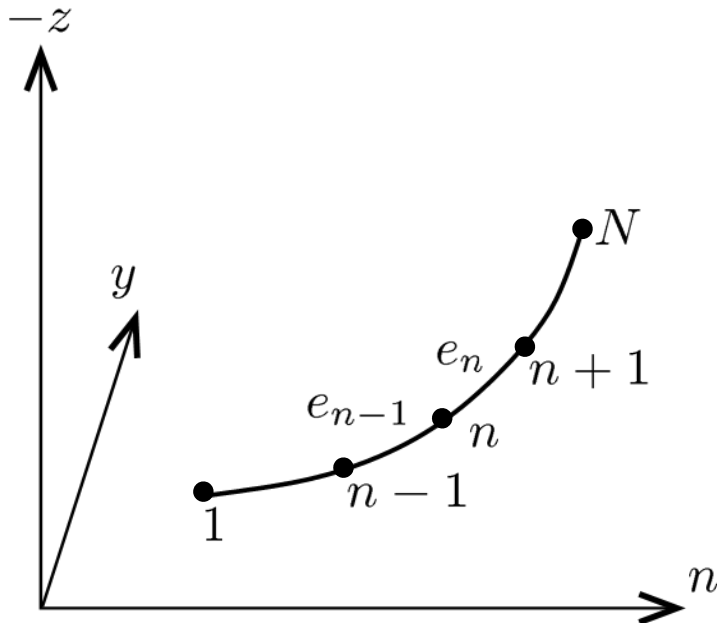
# Dynamic mooring line section

- Mooring line divided into sections with uniform stiffness, mass and hydrodynamic characteristic
- Each section divided equidistantly into a number of 2 node elements
- Concentrated masses and drag points can be added to any node



# Nonlinear stiffness term

One line segment with uniform properties



Length of element:

$$L_n = (x_{n-1} - x_n)^2 + (y_{n-1} - y_n)^2 + (z_{n-1} - z_n)^2$$

Green strain:

$$\epsilon_G = \frac{L_n^2 - L_{n,0}^2}{2L_{n,0}^2}$$

Axial force in element:

$$f = EA\epsilon_G$$

Element stiffness matrix:

$$K_e = f/L_n \begin{bmatrix} 1 & 0 & 0 & -1 & 0 & 0 \\ 0 & 1 & 0 & 0 & -1 & 0 \\ 0 & 0 & 1 & 0 & 0 & -1 \\ -1 & 0 & 0 & 1 & 0 & 0 \\ 0 & -1 & 0 & 0 & 1 & 0 \\ 0 & 0 & -1 & 0 & 0 & 1 \end{bmatrix}$$

Nodal elastic forces:

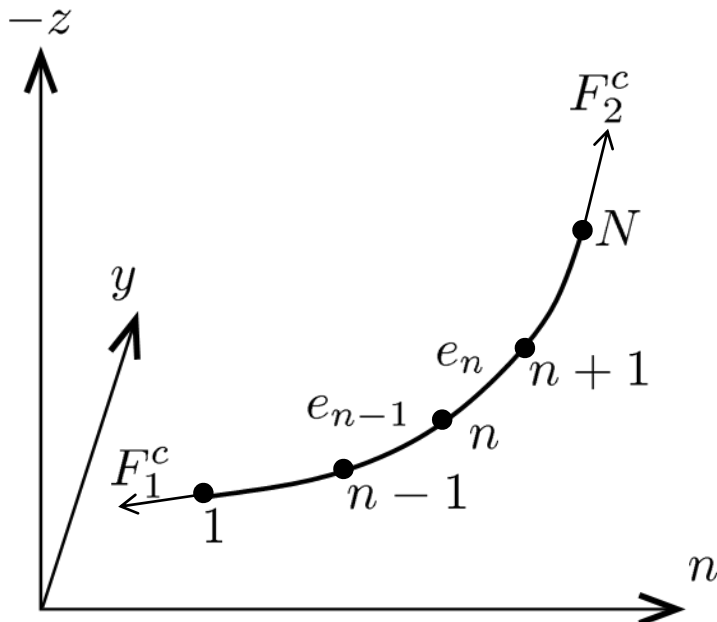
$$K_e \begin{bmatrix} \mathbf{x}_n \\ \mathbf{x}_{n+1} \end{bmatrix} = \begin{bmatrix} -f\delta \\ f\delta \end{bmatrix}, \quad \delta = \begin{bmatrix} \frac{x_{n+1} - x_n}{L_n} \\ \frac{y_{n+1} - y_n}{L_n} \\ \frac{z_{n+1} - z_n}{L_n} \end{bmatrix}$$

# Equations of motion

Unconstrained equation of motion:

$$\mathbf{M}\ddot{\mathbf{x}}(t) + \mathbf{K}(\mathbf{x}, t)\mathbf{x}(t) - F_{gravity} - F_{buoyancy} - F_{drag}(\mathbf{x}, \dot{\mathbf{x}}, t) = \text{residual}$$

One line segment with uniform properties

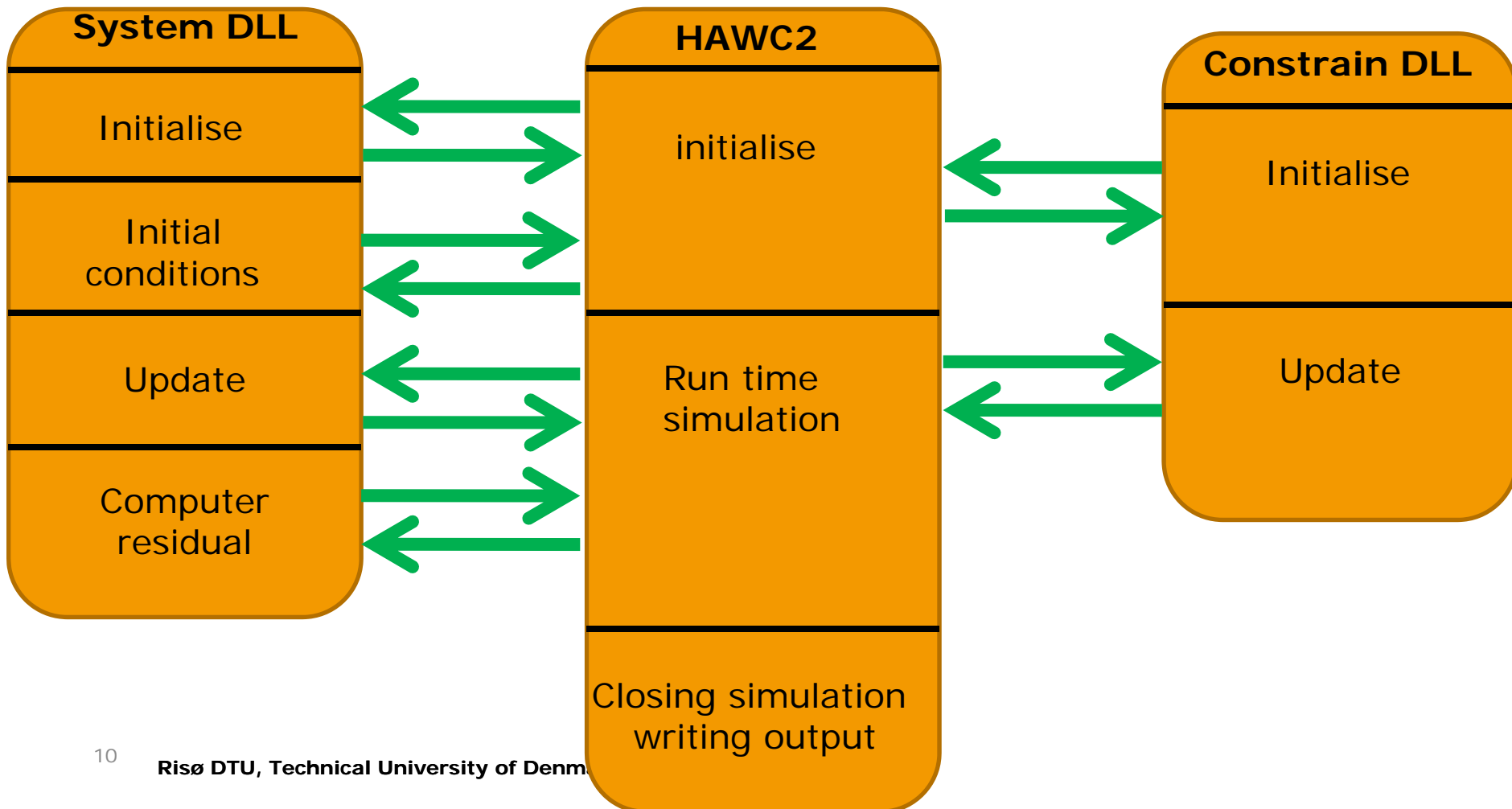


Constrain forces from constrain conditions:

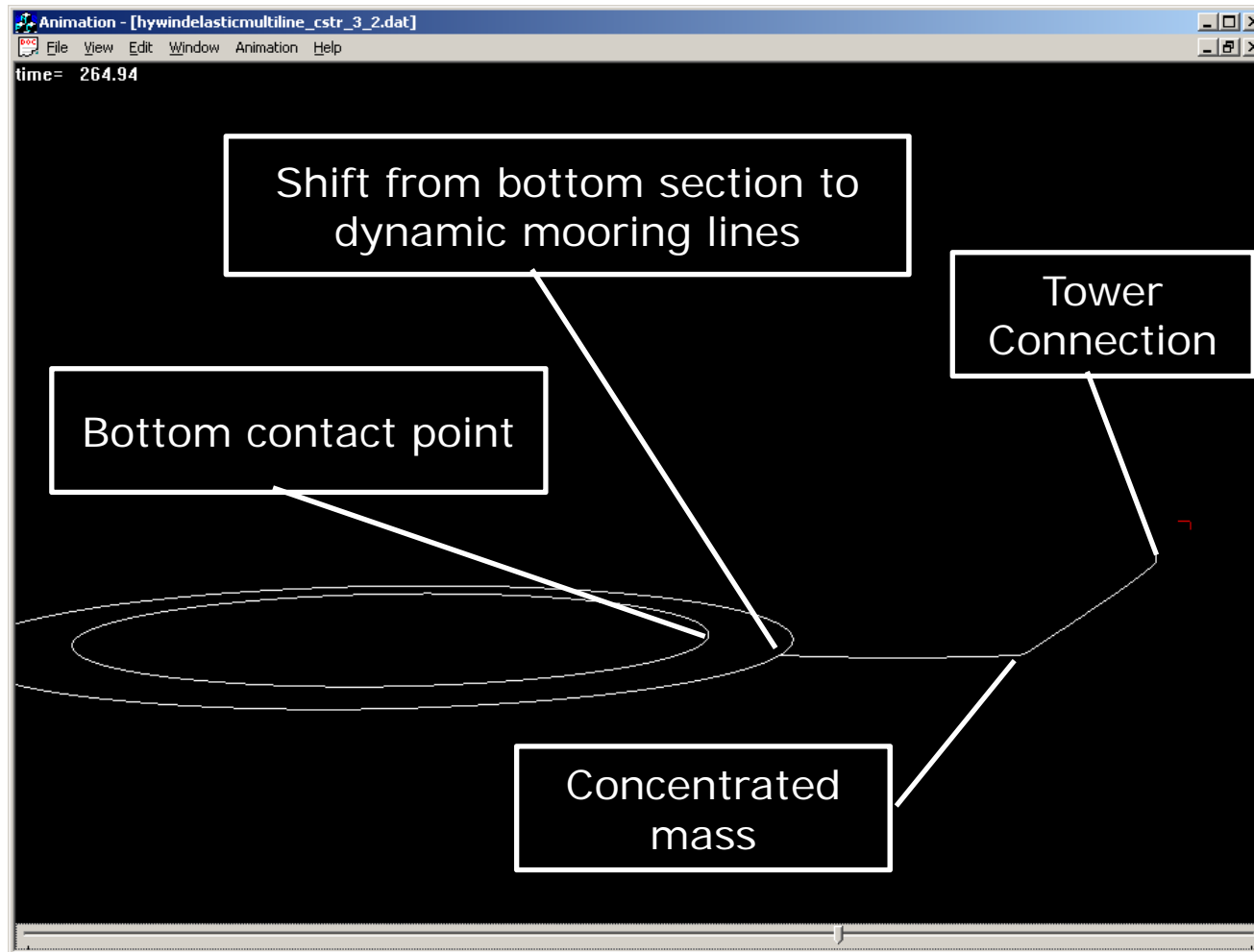
- 1) distance from end of 2D bottom contact section to node 1 of first line segment = 0
- 2) distance from node  $N$  of one line segment to node 1 of the next segment = 0
- 3) distance from node  $N$  of last line segment to node  $n$  on a HAWC2 body = 0

# Implementation in HAWC2

- The mooring system model is implemented in HAWC2 by an external system DLL interface that couples external systems with its one degrees of freedom to the HAWC2 model in a tightly coupled manner.



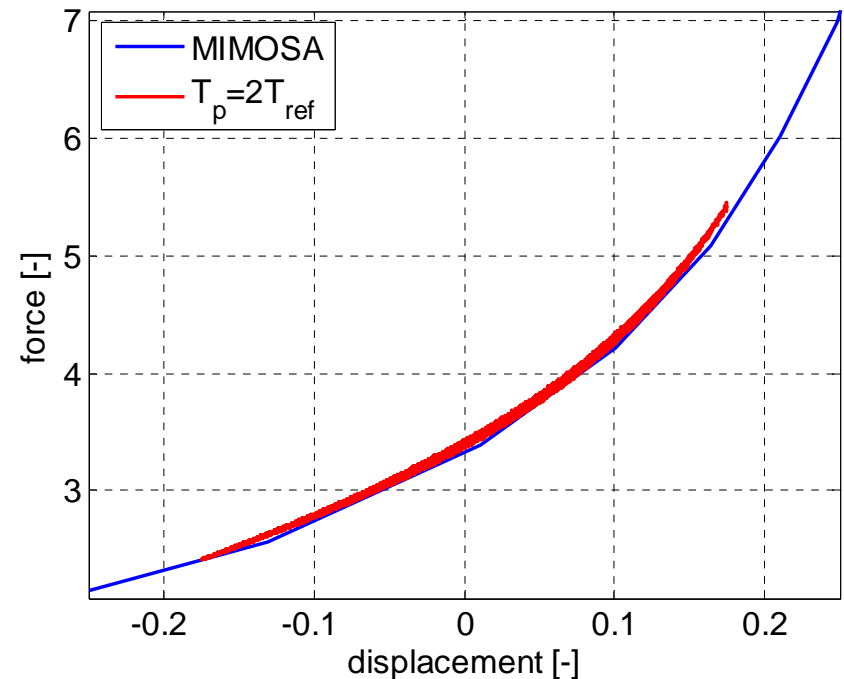
# Mooring system model with one line





## Quasi-static results (one line)

- Quasi-static results by moving tower connection point slowly back and forth
- Fits well to MIMOSA results

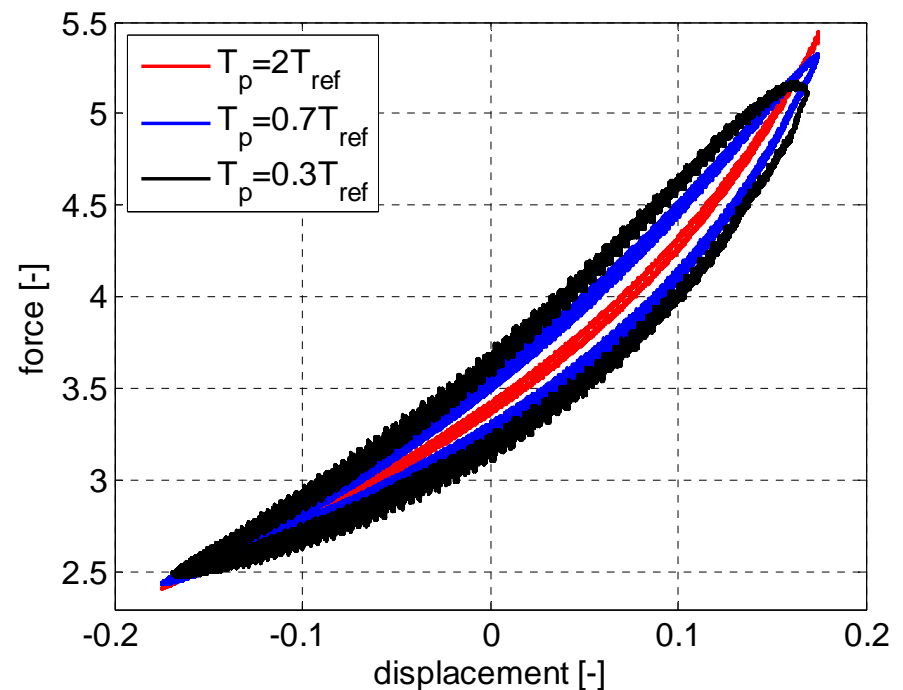


Result normalized by:

- Aerodynamic thrust at rated power
- Rotor diameter and
- Systems natural surge period

# Dynamic results (one line)

- Increasing oscillation frequency opens the loop

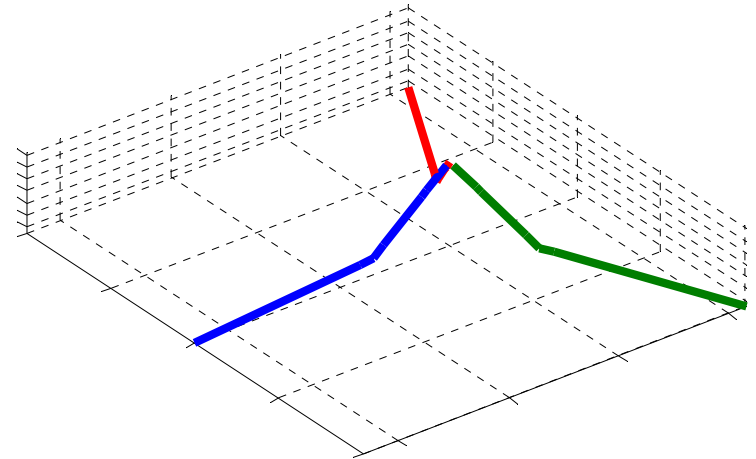


Result normalized by:

- Aerodynamic thrust at rated power
- Rotor diameter and
- Systems natural surge period

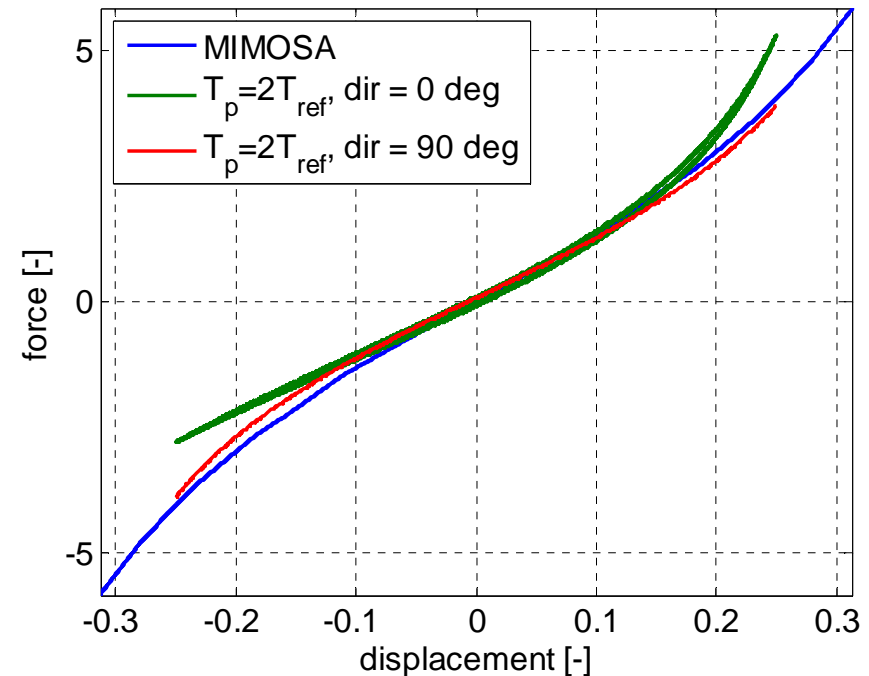
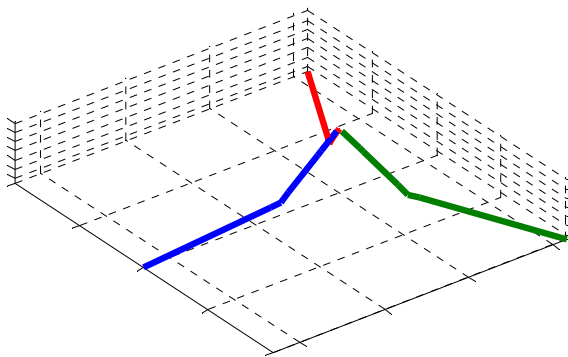
# Three line mooring system

- Mooring system as the one used in the OC3 project
- Three mooring lines, each with a concentrate mass to increase stiffness



# Quasi-static results (three lines)

- Results for 90 degrees direction fits well with MIMOSA results
- Different response for different direction because of unsymmetrical line setup; this effect is not included in the quasi-static implementation in HAWC2

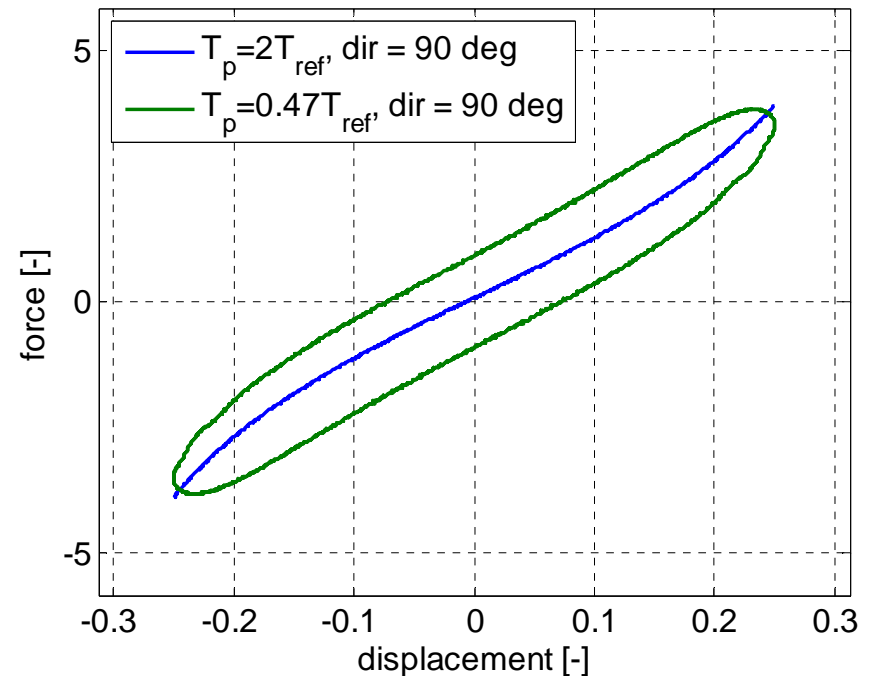


Result normalized by:

- Aerodynamic thrust at rated power
- Rotor diameter and
- Systems natural surge period

# Dynamic results (three lines)

- Increasing oscillation frequency opens the loop



Result normalized by:

- Aerodynamic thrust at rated power
- Rotor diameter and
- Natural surge period

## Conclusion

- A nonlinear element that can model a cable with no bending stiffness but longitudinal flexibility has been developed
- A 2D bottom contact section that determine a quasi-static bottom contact point for the mooring system has been developed
- Quasi-static results shows good agreement with MIMOSA results

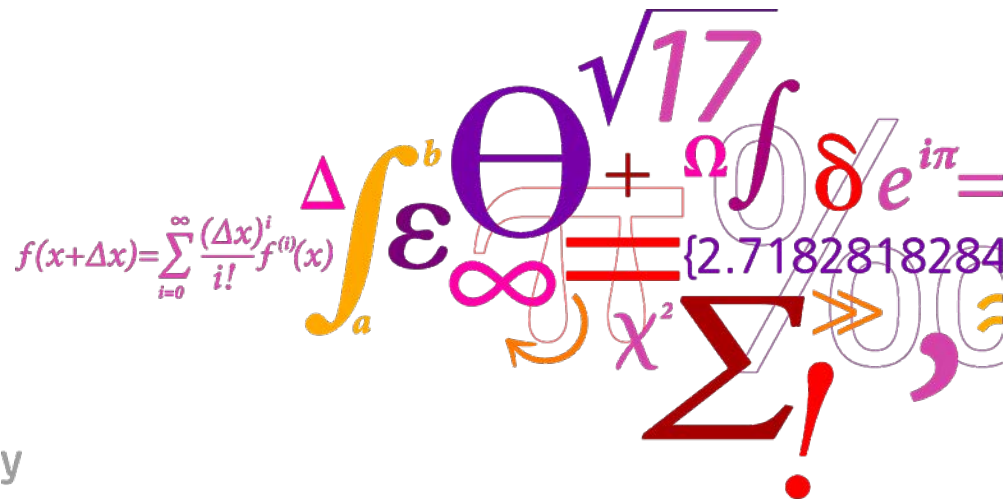
## Further work

- Run selected load cases with detailed mooring model to analysis the mooring system behavior
- Run selected load cases with different model complexities to determine necessary model complexity for different modeling purposes
  - Mooring modeling necessary to determine turbine loads
  - Turbine modeling necessary to determine mooring line loads

### **3 Enhanced BEM**

# Enhanced BEM including wake expansion and swirl

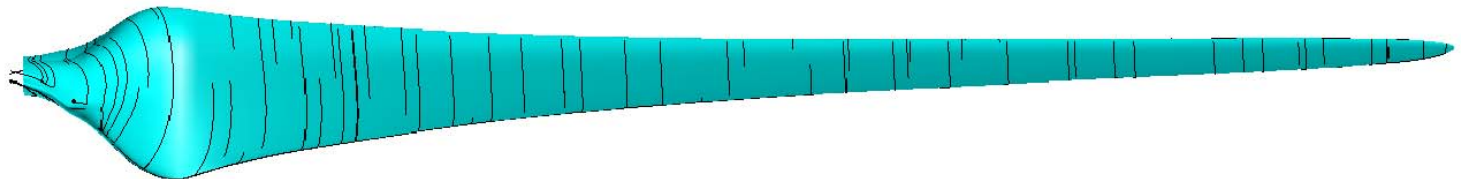
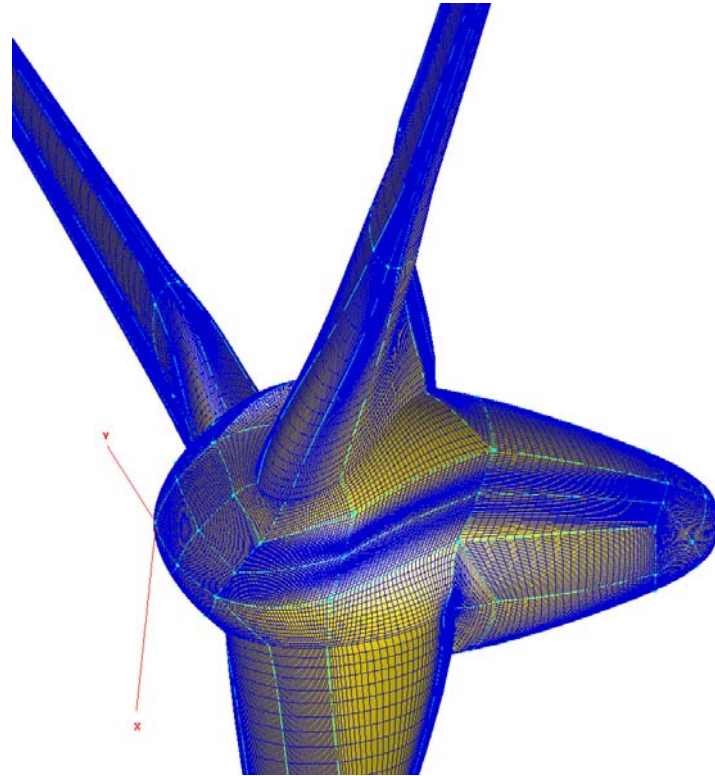
Mads Døssing, Christian Bak, Helge A. Madsen





# Background

## Reporting high aerodynamic efficiency



# Background

## Design of rotors: Max CP incl. swirl

Pressure

Axial velocity

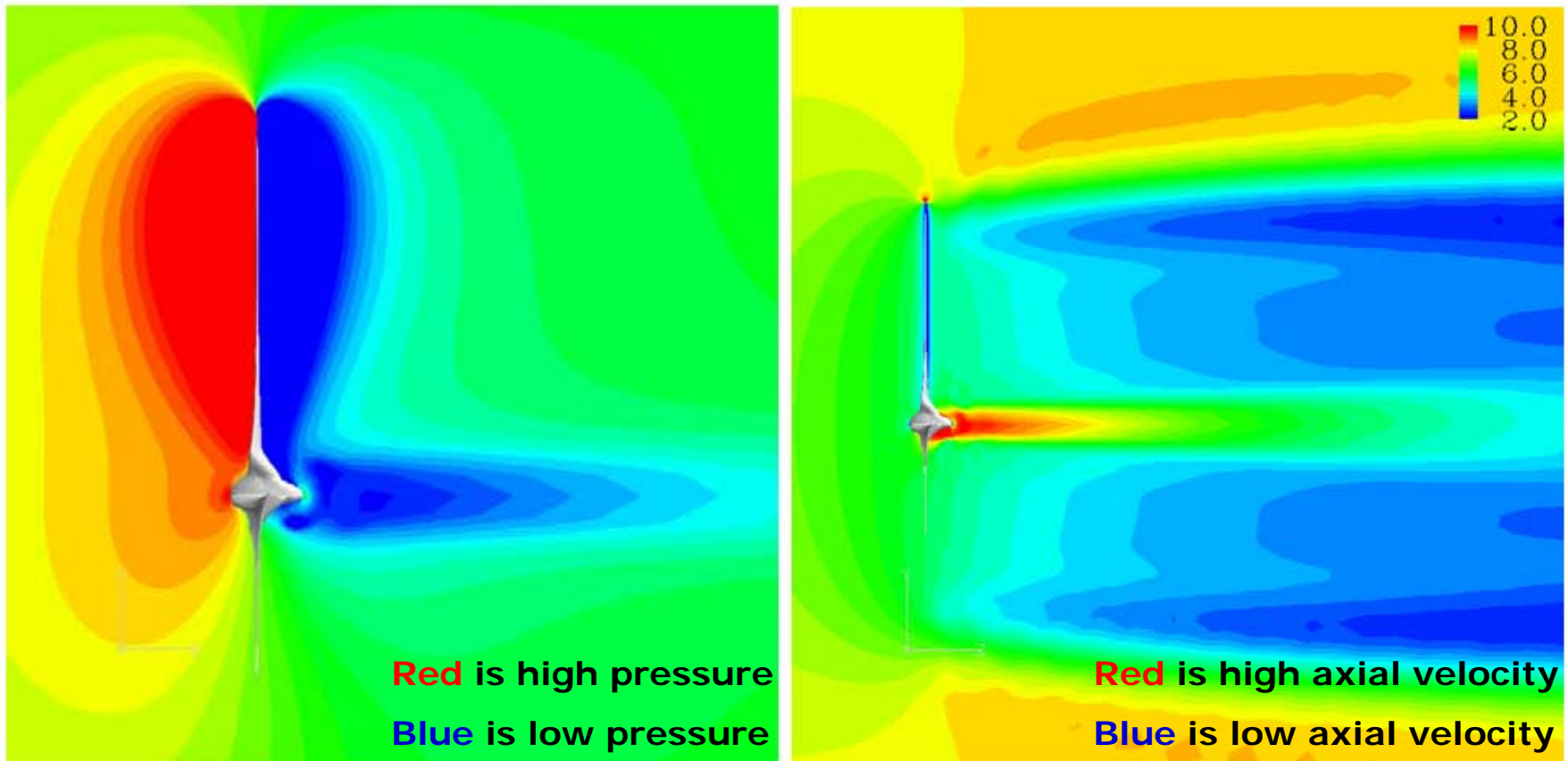


Figure 13. Contour plots of pressure (left) and axial velocity (right) in a vertical plane through the rotor.

# Background

## Design of rotors: Max CP incl. swirl

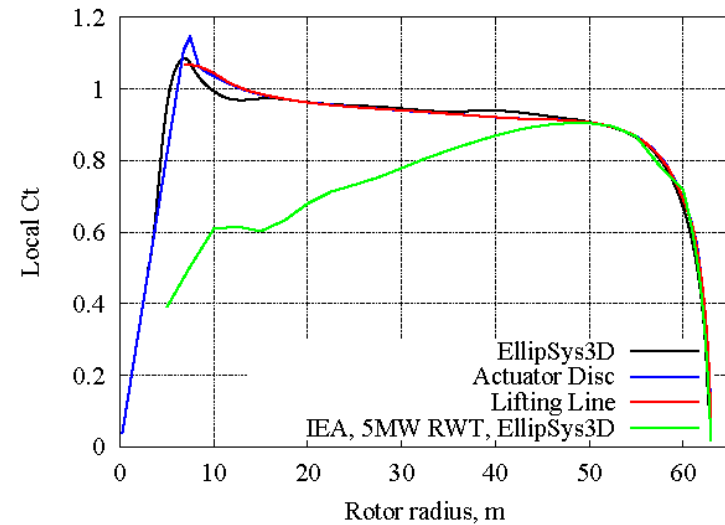
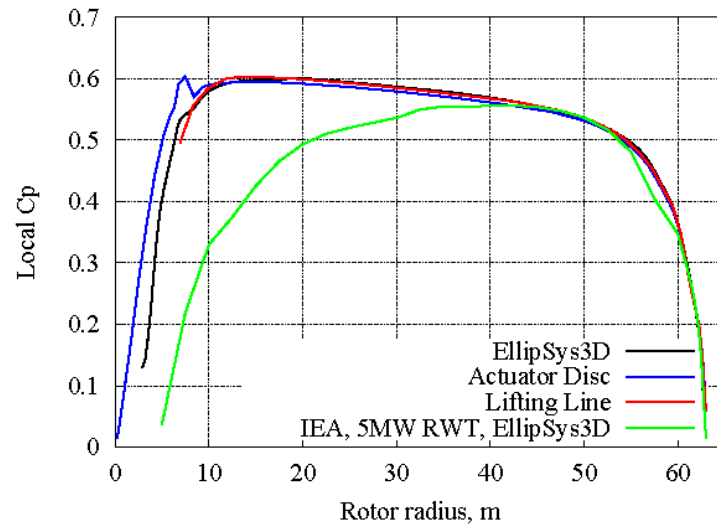


Table 1: Mechanical power and Thrust force for the present rotor. The IEA, 5MW RWT is included for comparison

	Mechanical power, $P$	Thrust force, $T$	$CP$	$CT$
	[MW]	[kN]		
EllipSys3D	2.015	426	0.515	0.872
Lifting Line	2.011	424	0.514	0.868
Actuator Disc	1.995	425	0.510	0.870
IEA, 5MW RWT EllipSys3D	1.867	382	0.477	0.782

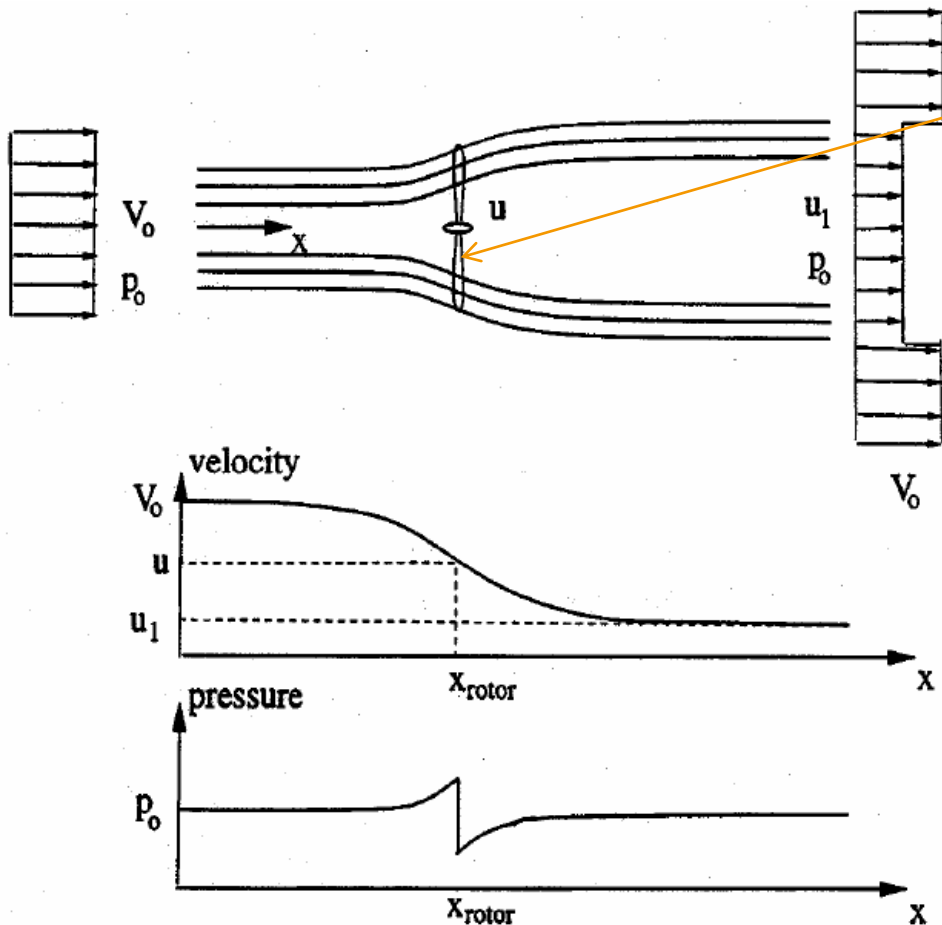
# BEM correction

## Axial velocity in rotorplane

NEW

$$v_a = (1 - a + \Delta v_w - \Delta v_e)V_0$$

$\Delta v_w$  correction for wake rotation  
 $\Delta v_e$  correction for wake expansion  
 $a$  axial induction factor



# BEM correction

## The model

- Expansion

$$\Delta v_e = \Delta v1_e - \Delta v2_e$$

$$\Delta v1_e = f(r, v_r) = l_1(r)v_r^3 + l_2(r)v_r^2 + l_3(r)v_r$$

$$\Delta v2_e = f(v_r(r/R = 0.9)) = k_1v_r^2 + k_2v_r + k_3$$

$$v_r = \frac{1}{2.24} \frac{C_{Tav}}{4\pi} \ln \left[ \frac{0.04^2 + (r+1)^2}{0.04^2 + (r-1)^2} \right]$$

$$C_{Tav} = \frac{\int_0^r C_T 2\pi r dr}{\pi r^2}$$

- Swirl

$$\Delta v_w = 0.7 p_w$$

$$p_w = \int_1^r \frac{v_t^2}{r} dr$$

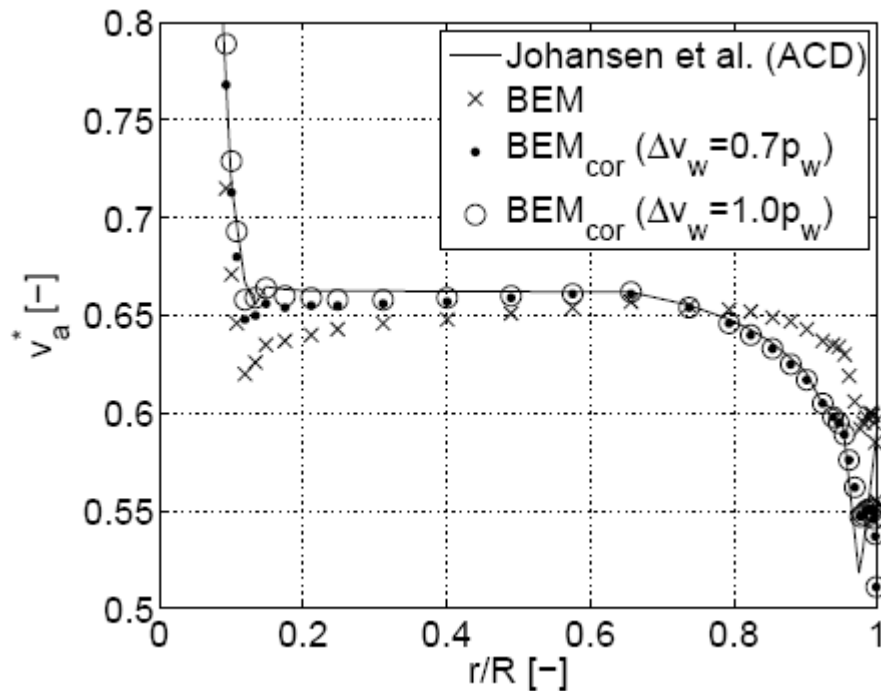
$$v_t = 2a' \lambda_r$$

H. Madsen, C. Bak, M. Døssing, R. Mikkelsen, S. Øye, "**Validation and modification of the Blade Element Momentum theory based on comparisons with actuator disc simulations**", WIND ENERGY *Wind Energ.* 2010; **13:373–389**

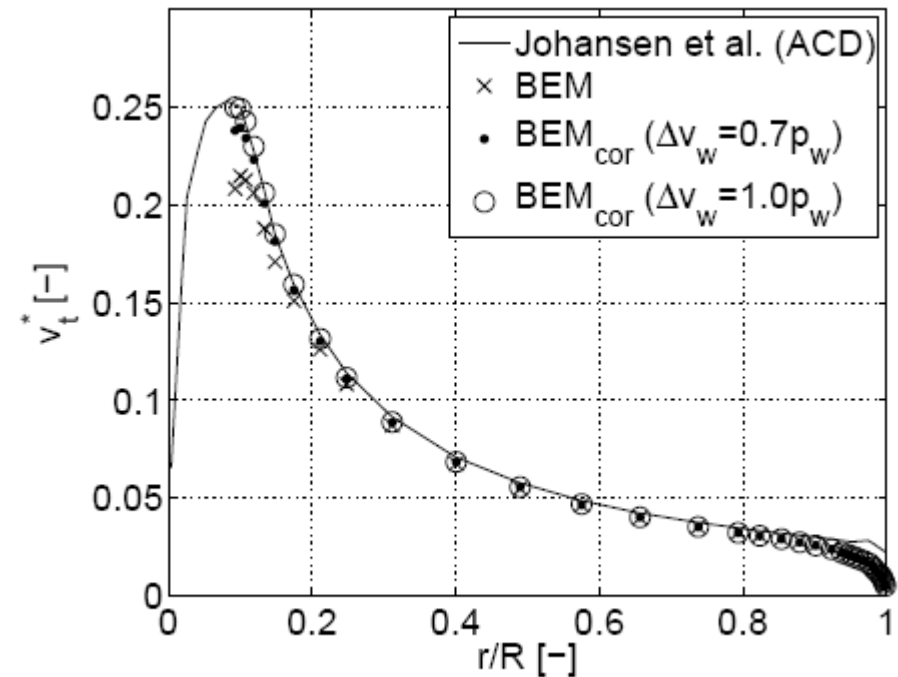
# Application of BEM corrections

- How does the BEM corrections influence the rotor performance?
- Rotor designs are carried out to
  - investigate the influence of the the BEM corrections and
  - investigate how rotors should be designed when corrections for swirl and expansion are included

# Validation of implementation in HAWTOPT



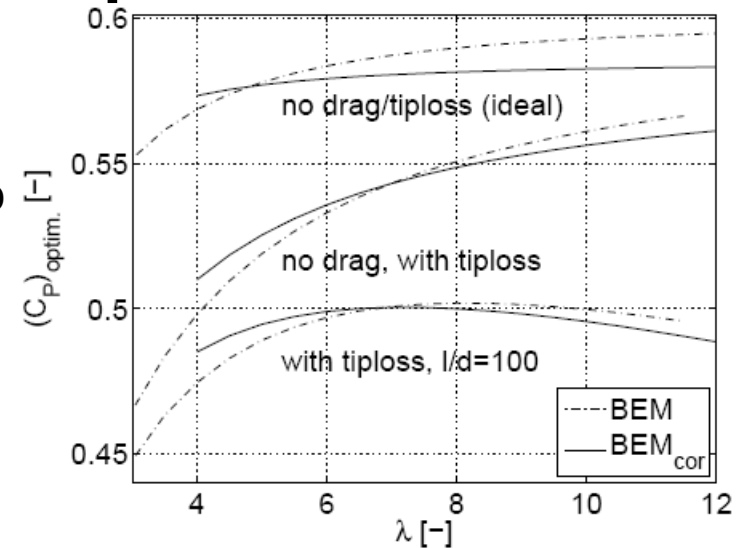
Axial velocity



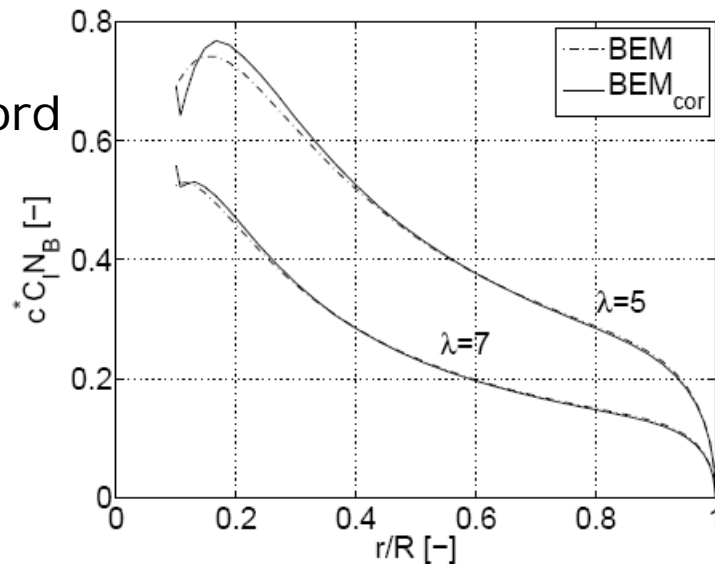
tangential velocity

# Rotors optimized for maximum power

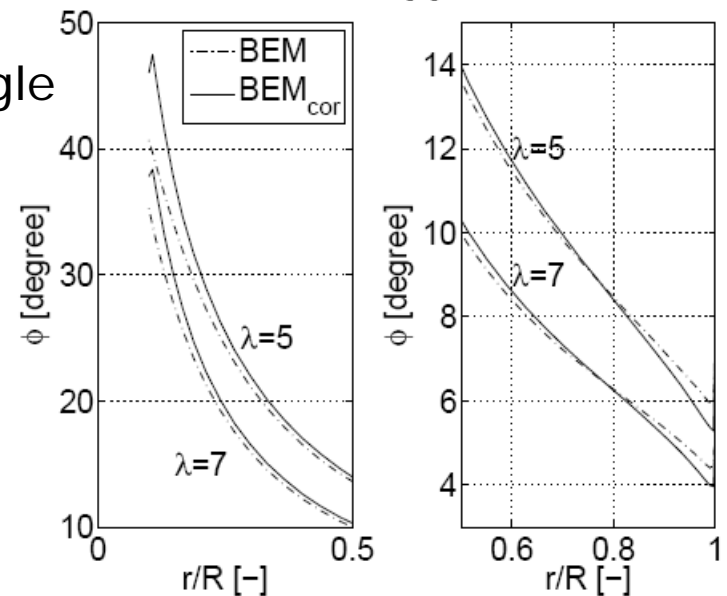
Tip speed ratio



Chord



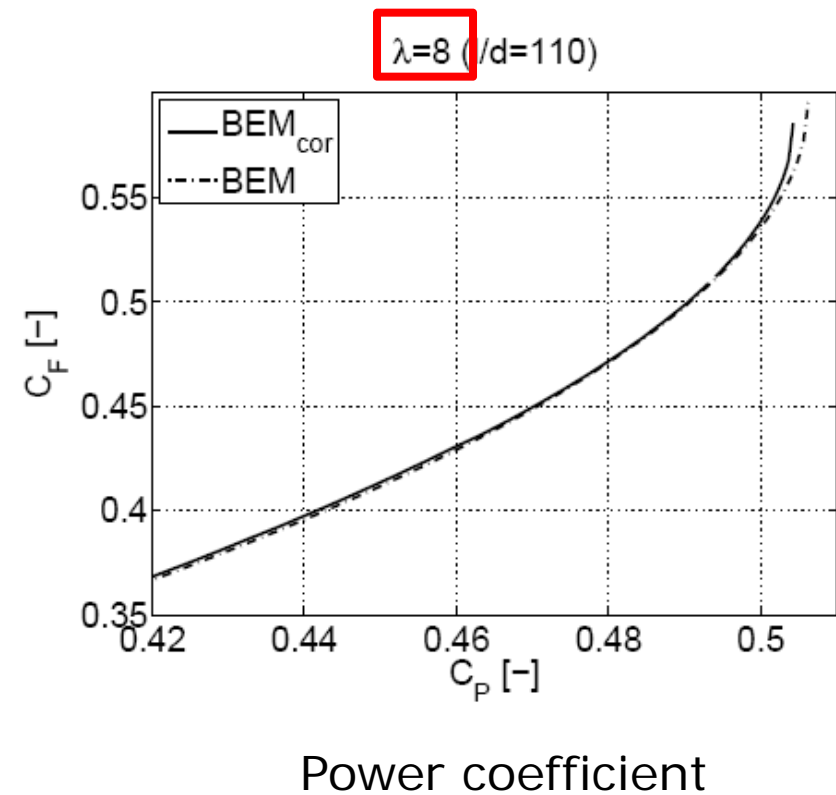
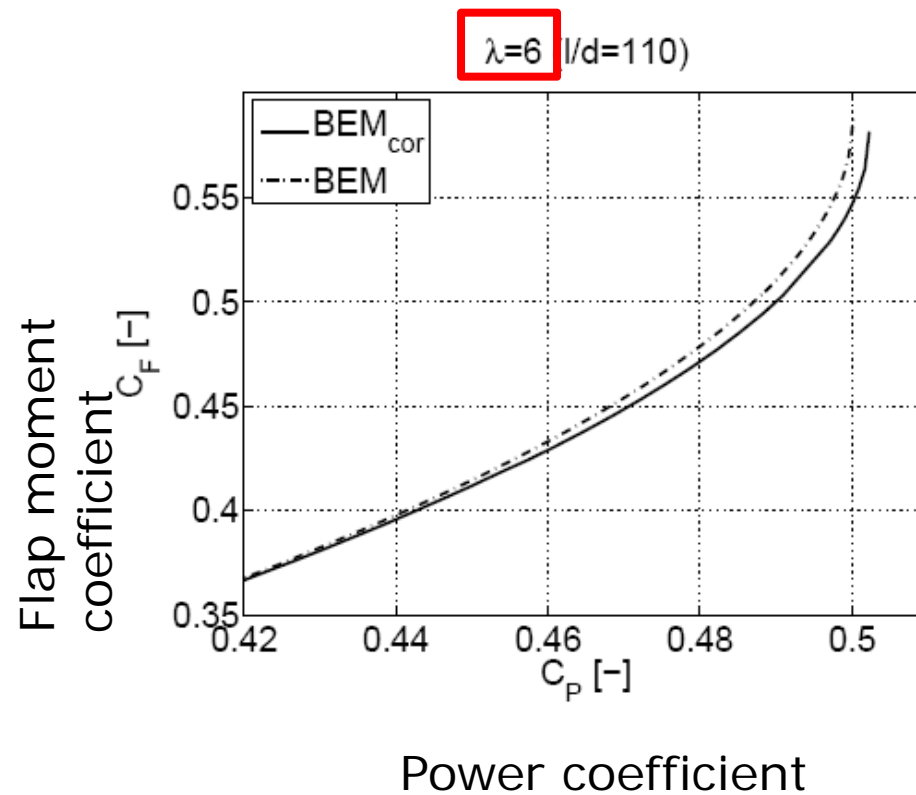
Inflow angle





# Root bending moments

## Optimization for low thrust at reduced CP

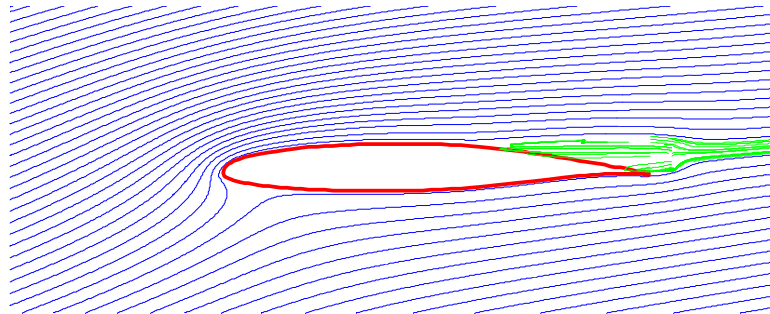


# Conclusion

- Rotor designs are carried out using BEM with correction for swirl and expansion
- No significant differences in designs are seen if  $\lambda_{\text{design}}$  is appr. 7-8, when comparing traditional BEM to corrected BEM.
- If  $\lambda_{\text{design}}$  is below 7-8
  - Chord lengths and twist close to the root should be increased
  - Power efficiency increased
- If  $\lambda_{\text{design}}$  is beyond 7-8
  - Power efficiency decreased

## **4 Unsteady viscous-inviscid airfoil code**

# Unsteady Viscous-Inviscid Interactive Airfoil Code for Wind Turbines



Néstor Ramos García  
Jens Nørkær Sørensen  
Wen Zhong Shen

$$(EIv'')'' = q - \rho A \ddot{v}$$

$$\Delta \int_a^b \epsilon \Theta + \Omega \int \delta e^{i\pi} = \{2.718281828\}$$

$$\infty = \chi^2 \Sigma!$$

# PRESENTATION LAYOUT

- INTRODUCTION
- VISCOUS-INVISCID INTERACTION
- INTEGRAL BOUNDARY LAYER SOLVER via VI INTERACTION
  - STEADY 2D.
  - UNSTEADY 2D, SINGLE WAKE.
  - STEADY QUASI3D
- POTENTIAL DOUBLE WAKE SOLVER
- CONCLUSIONS

# INTRODUCTION

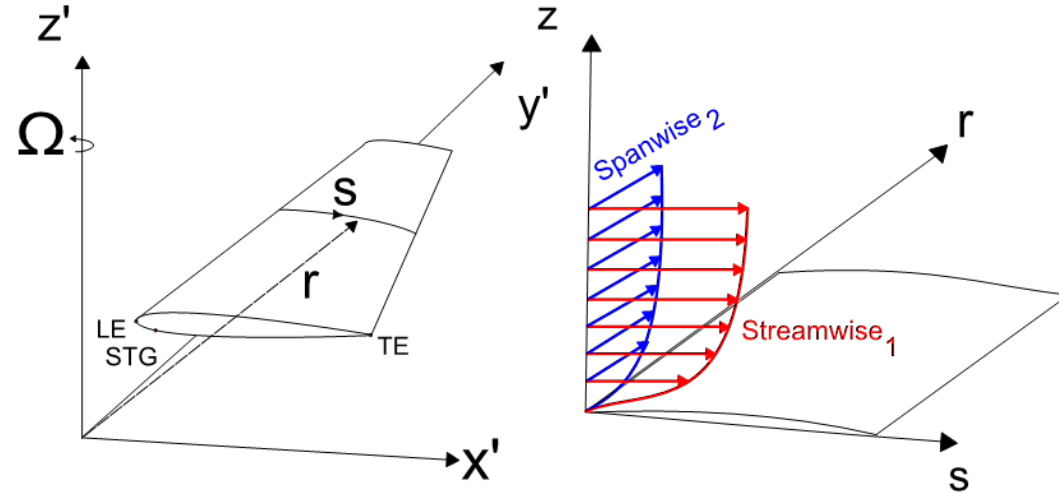
- **Blade-Element Momentum** theory is often used for the design of wind turbines. Required Input: Lift and Drag force coefficients.
- Computer resources are getting more powerful with the years, but it is still **behind our limits to realize an active design of airfoils and blades using Navier-Stokes solvers**. High cost in computational time.
- The first HAWT Aerodynamics Specialists meeting, Wichita State University, 1983, concluded:
  - **Inboard regions** are producing **more power than predicted**.
  - Rotor is producing **more power at high angles of attack** due to secondary outward flow, caused by centrifugal pumping.



- A code has been developed during the last three years that can fit our needs:
  - It has to compute accurately steady/unsteady **airfoil forces**.
  - It has to be **fast** in order to use it as a **design method**.
  - It has to take into account **rotational effects**. Centrifugal and Coriolis forces.
- The code uses the already known concept of UNSTEADY VISCOUS-INVISCID STRONG INTERACTION via transpiration velocity.
  - **Inviscid** flow → Unsteady potential flow, **panel method**.
  - **Viscous** flow → Quasi 3-D integral **BL equations** + **Closures**.

# QUASI-3D BOUNDARY LAYER EQUATIONS

- The boundary layer equations are used with all the necessary assumptions in order to reduce them into the integral quasi-3D ones.



## Integral $\theta$ -momentum

$$\frac{\partial \theta_1}{\partial s} = -\frac{\theta_1}{u_e} \frac{\partial u_e}{\partial s} (2 + H) + \frac{C_f}{2} + s_w p_r \frac{2Ro \cdot ls}{u_{2D} c} \delta_2 - \frac{1}{u_e} \frac{\partial u_e}{\partial s} (2\theta_2 - \delta_2) - \frac{ls}{c} (2\theta_2 - \delta_2)$$

## Integral $r$ -momentum

$$\frac{\partial \theta_2}{\partial s} = -\frac{2\theta_2}{u_e} \frac{\partial u_e}{\partial s} + \tan \beta_w \frac{C_f}{2} + \frac{ls}{c} \left( \theta_1 + \delta_1 - \delta - \delta_3 + s_w p_r \frac{2Ro}{u_{2D}} (\delta - \delta_1) \right) - \frac{1}{u_e} \frac{\partial u_e}{\partial r} (2\delta_3 + \delta)$$

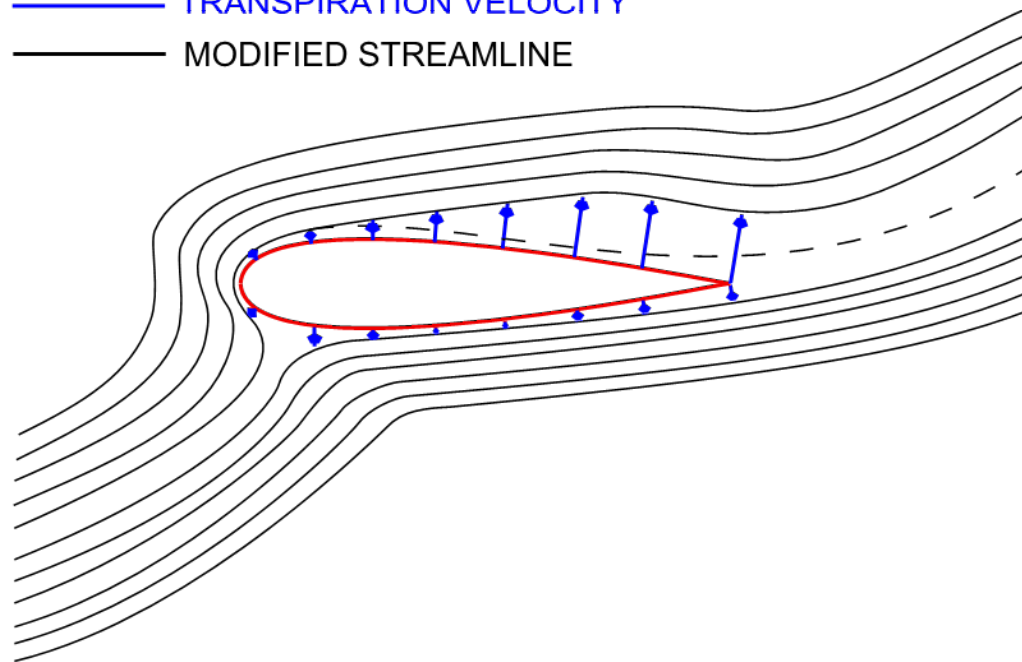
**A set of 3D turbulent closure equations are used in order to close the system (semi-empirical)**



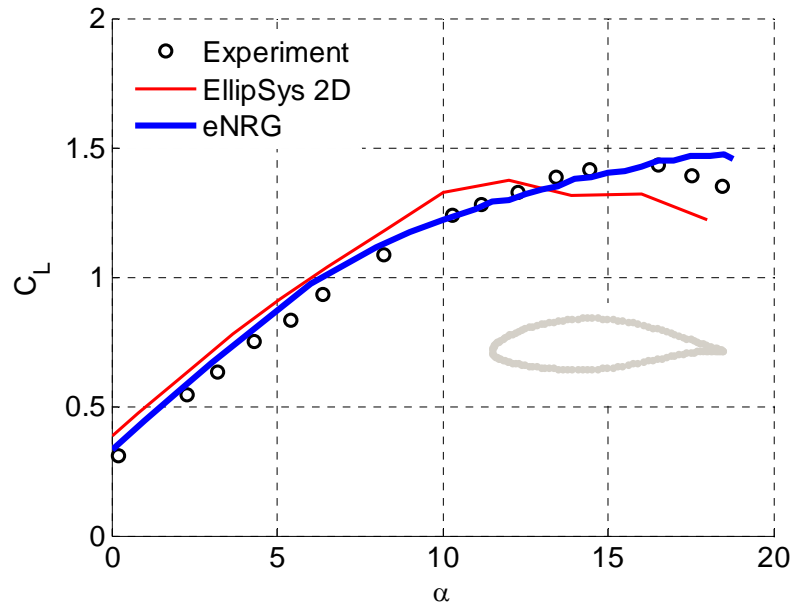
- **ASSUMPTION OF AN EQUIVALENT FLOW**, where the effects of real flow can be added. Transpiration velocity will take into account the effects of the real flow in the potential flow solver.

$$v_T = \frac{d}{dx} \int_0^{\infty} (u_e - u) dz = \frac{d}{dx} (u_e \delta_1)$$

— — — ORIGINAL STREAMLINE  
— — — TRANSPIRATION VELOCITY  
— — — MODIFIED STREAMLINE

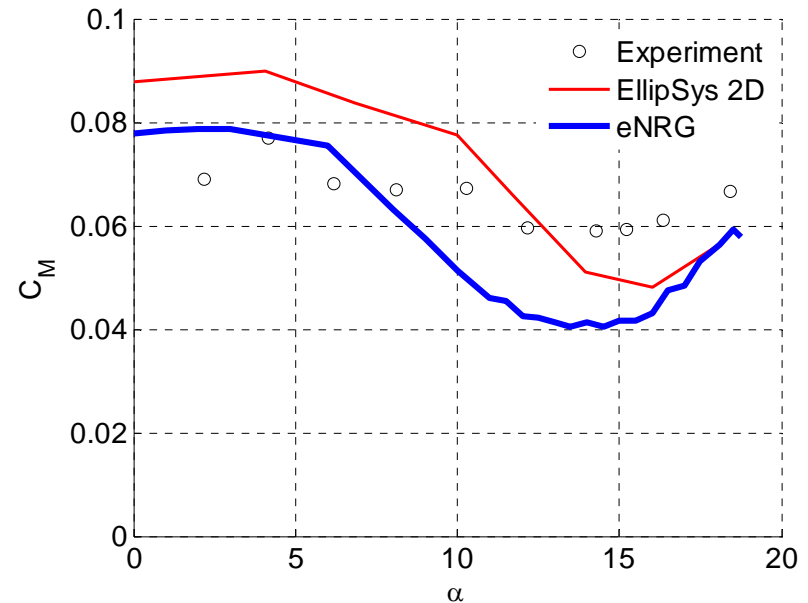
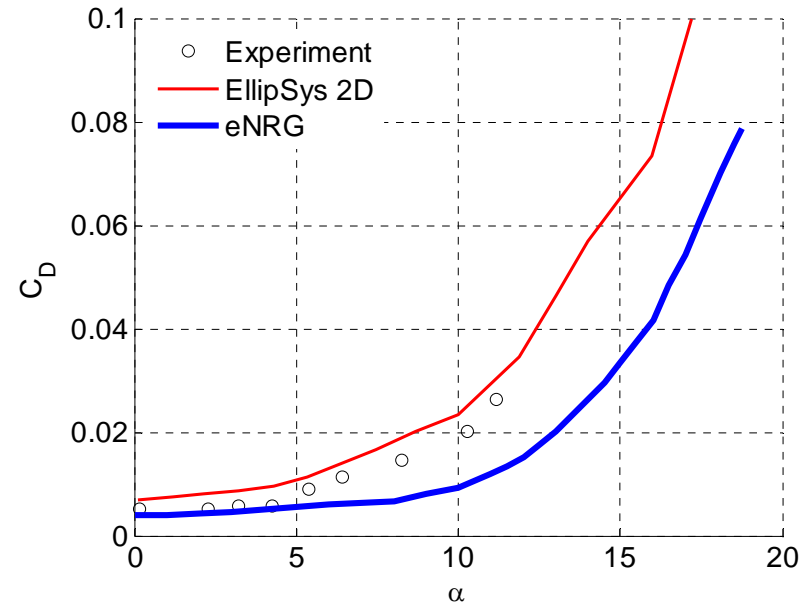


# STEADY VISCOUS INVISCID SOLVER

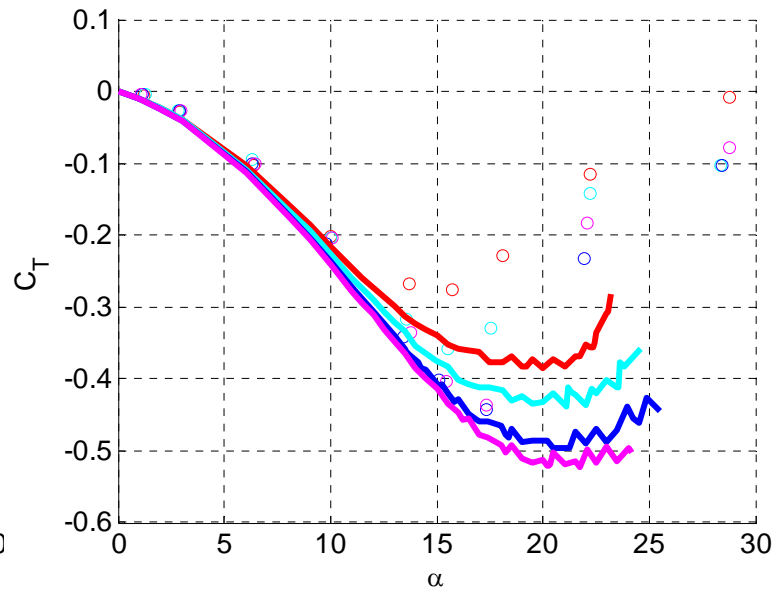
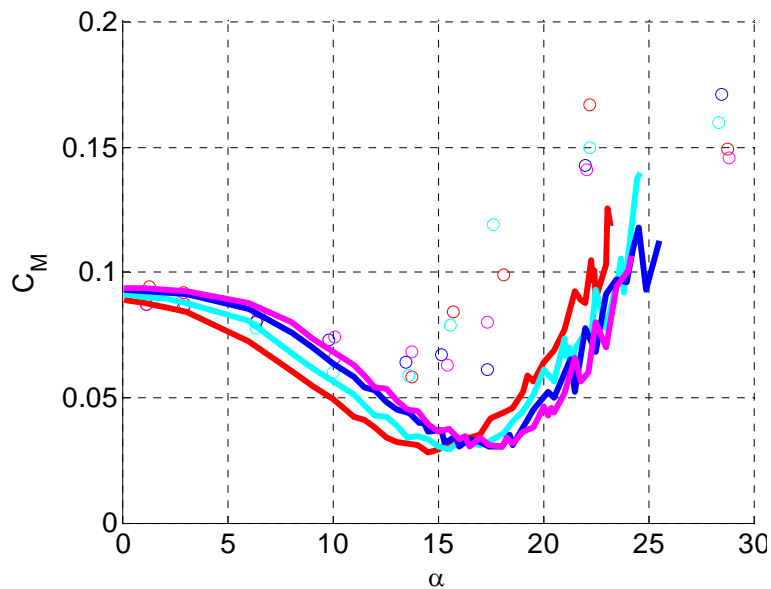
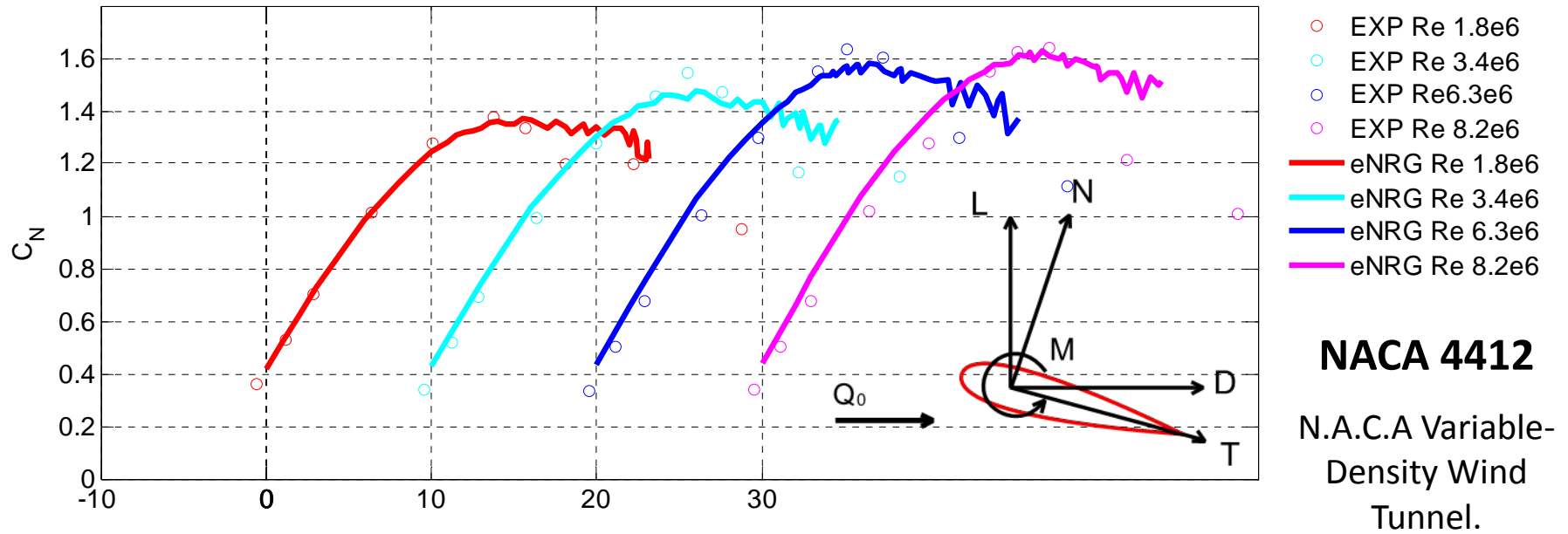


Comparison in between: **Experiments**, **EllipSys2D**, and the **VI code**: lift, drag and pitch moment coefficients in function of the angle of attack for the *NACA 65415* at  $Re = 3e6$

The measurements were performed at NASA's low-turbulence pressure tunnel and reported in the book by Abbott and von Doenhoff.



# STEADY VI, REYNOLDS VARIATION



# UNSTEADY VISCOUS INVISCID SOLVER SINGLE WAKE

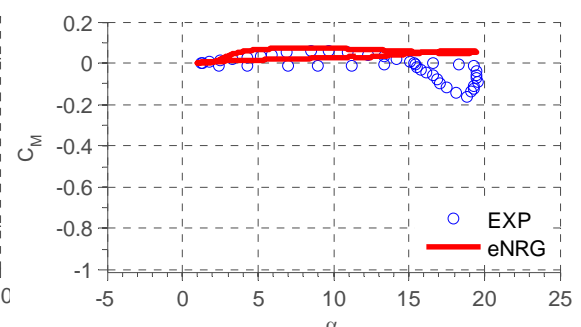
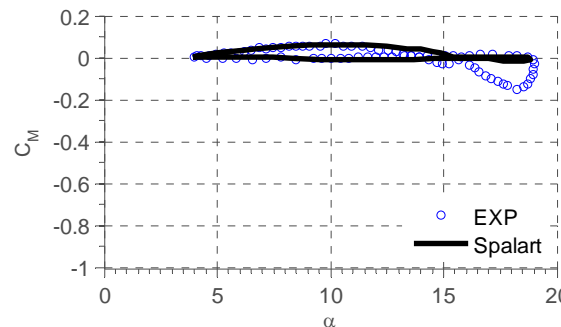
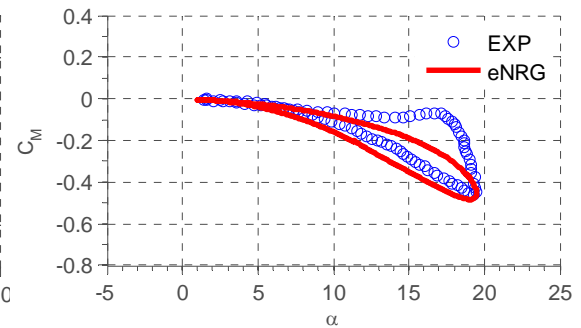
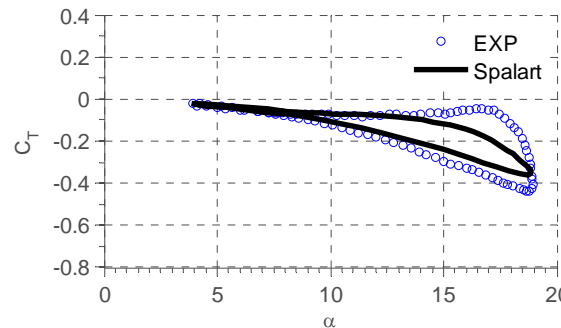
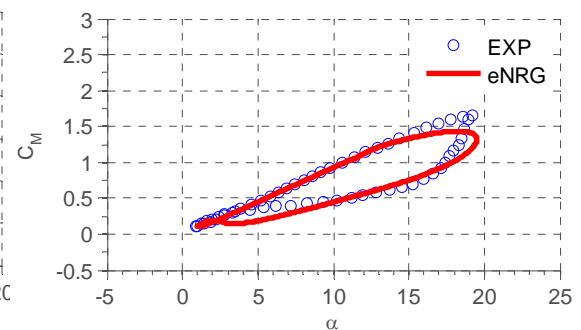
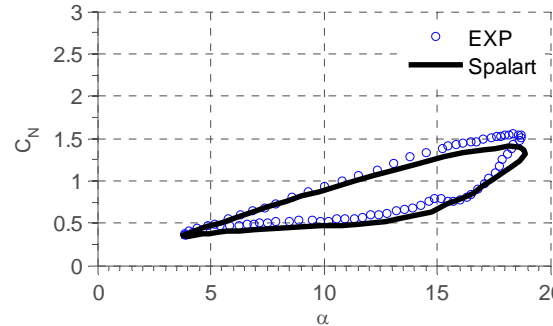
# UNSTEADY VISCOUS COMPUTATIONS, SINGLE WAKE

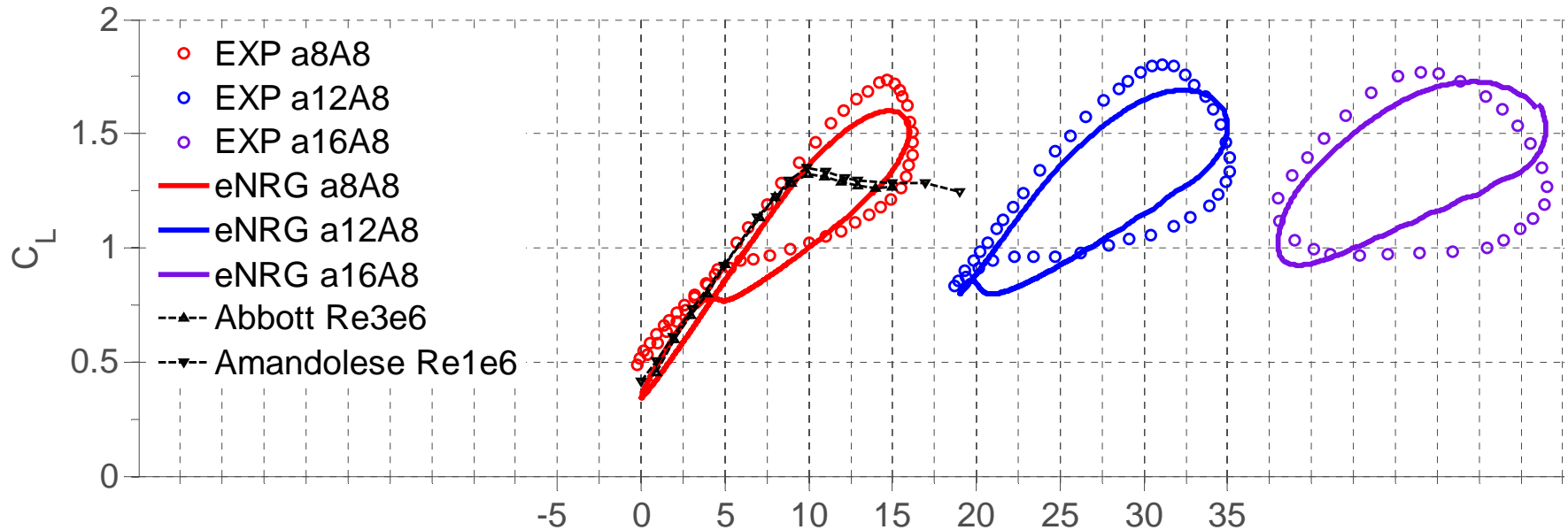
- NACA 0015
- $Re = 1.5e6$
- $k = 0.1$
- $\alpha = 13.37^\circ$   $A = 7.55$

- Unsteady experiments, University of Glasgow, G.U Aero Report 9221.

- Vorticity formulated Navier-Stokes equation running a Spallart Allmaras turbulent model. *J.N. Sørensen and P.J. Nygreen, Computers & Fluids 30 (2001).*

- Unsteady Viscous-Inviscid strong coupling code.





- **NACA 63421**
- **$k = 0.0785$**

- EXP, Unsteady experiments, *Institut AéroTechnique, S4 wind tunnel,  $TI = 1.1$ .*
- eNRG, Unsteady Viscous-Inviscid strong coupling code.

# Q3D STEADY VISCOUS INVISCID SOLVER



- Dimensional variables of interest in rotational study:  $c, r, \Omega, V_w$
- In order to proceed with a parametric study of the rotational effects in a wind turbine blade, two variables are defined:

1. The ratio between the chord length and the radial position,

$$ls = \frac{c}{r}$$

2. The ratio between the rotational speed and the relative velocity,

$$RO = \frac{\Omega r}{U_{rel}}$$

Where  $\Omega$  is the blade angular velocity,  $U_{rel}$  is defined typically,

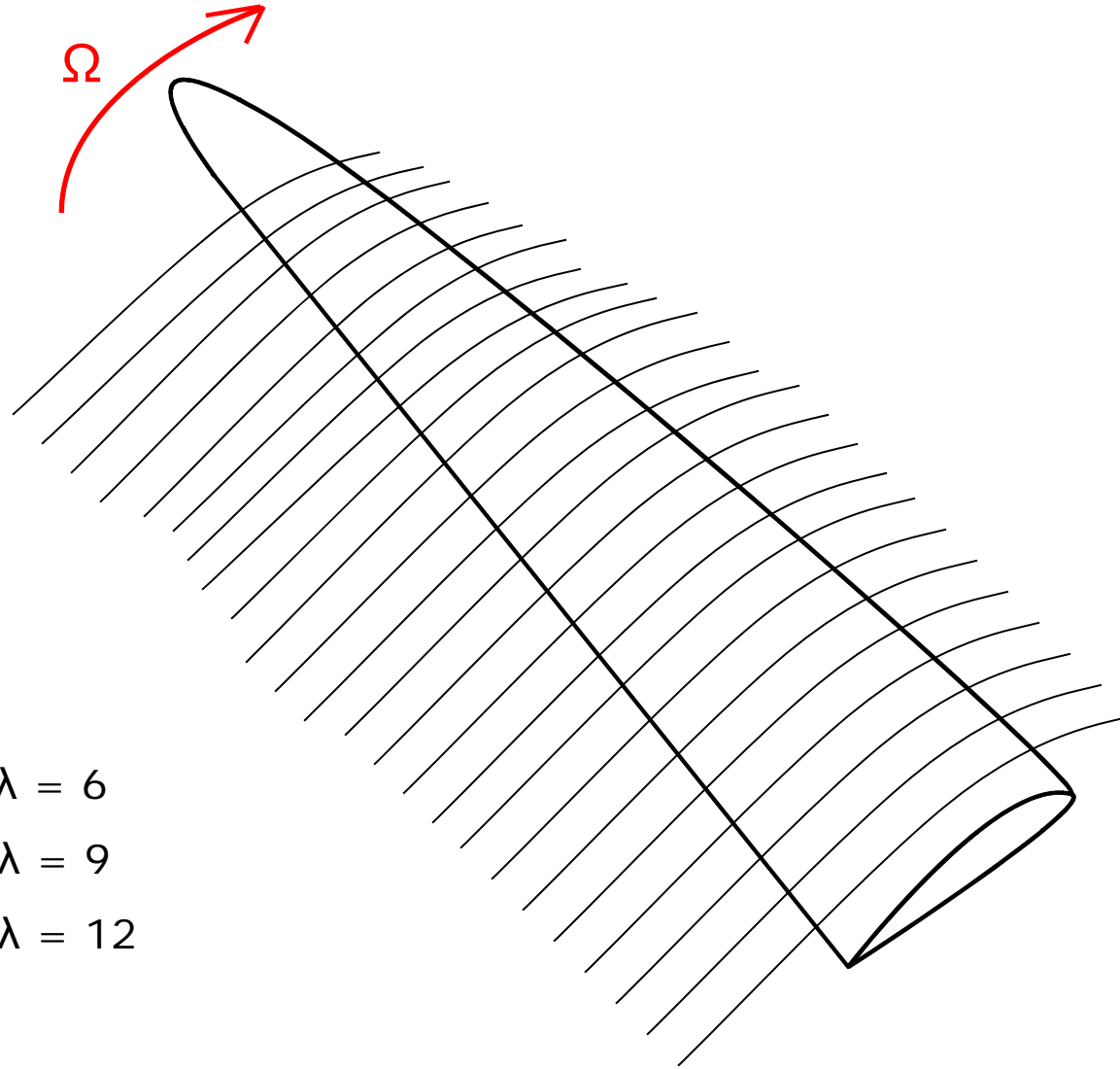
$$U_{rel} = \sqrt{((1+a')\Omega r)^2 + ((1-a)V_w)^2}$$

The four dimensional variables of interest are reduced to two adimensional parameters  $ls$  &  $RO$ , base for our parametric study.

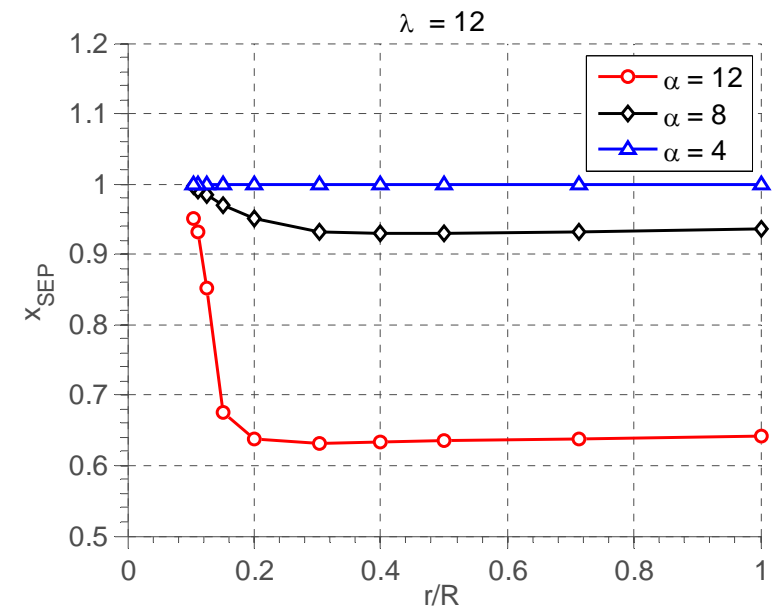
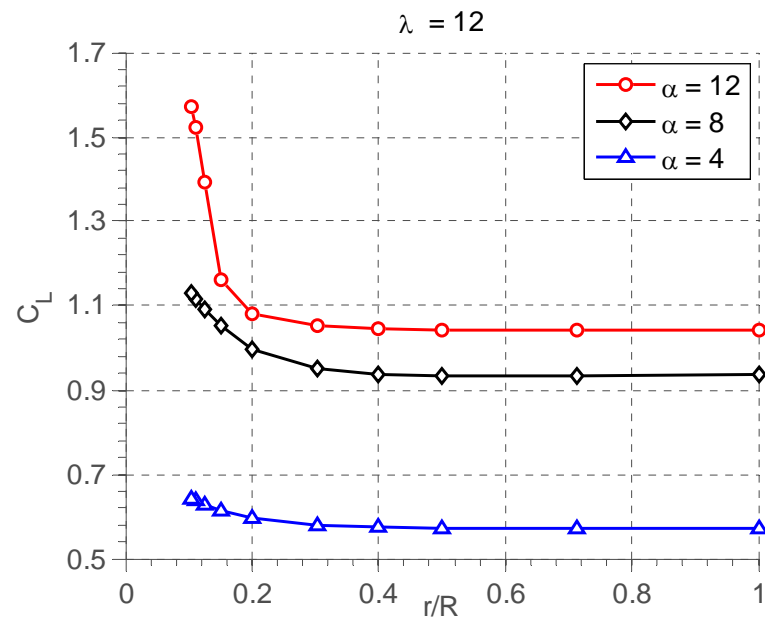
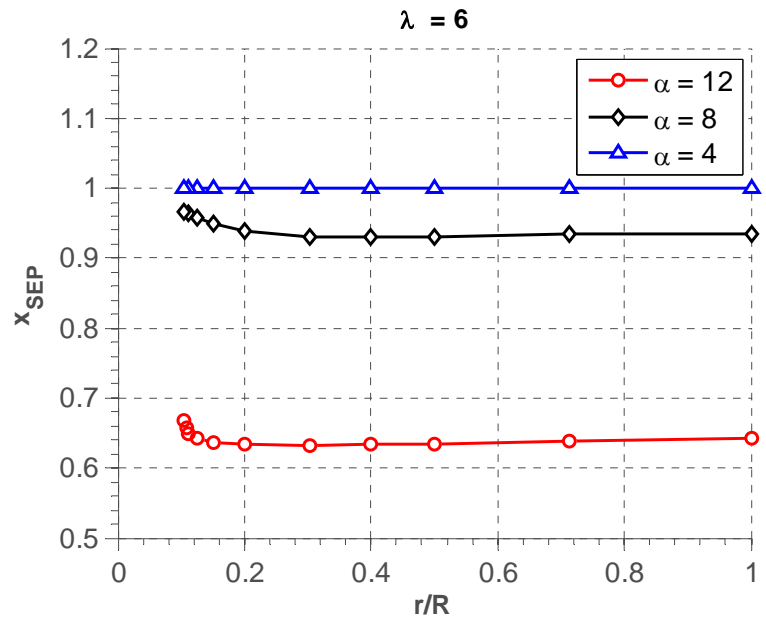
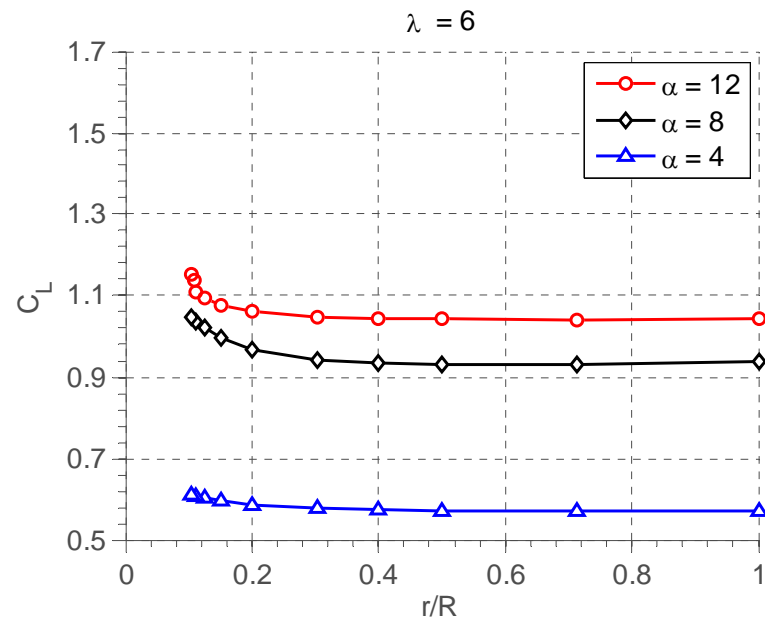
# QUASI-3D BOUNDARY LAYER

- Artificial rotor.
- S809 Airfoil.
- $Re$  1e6.
- $R = 10$  m.
- $\Omega = 70$  rpm.

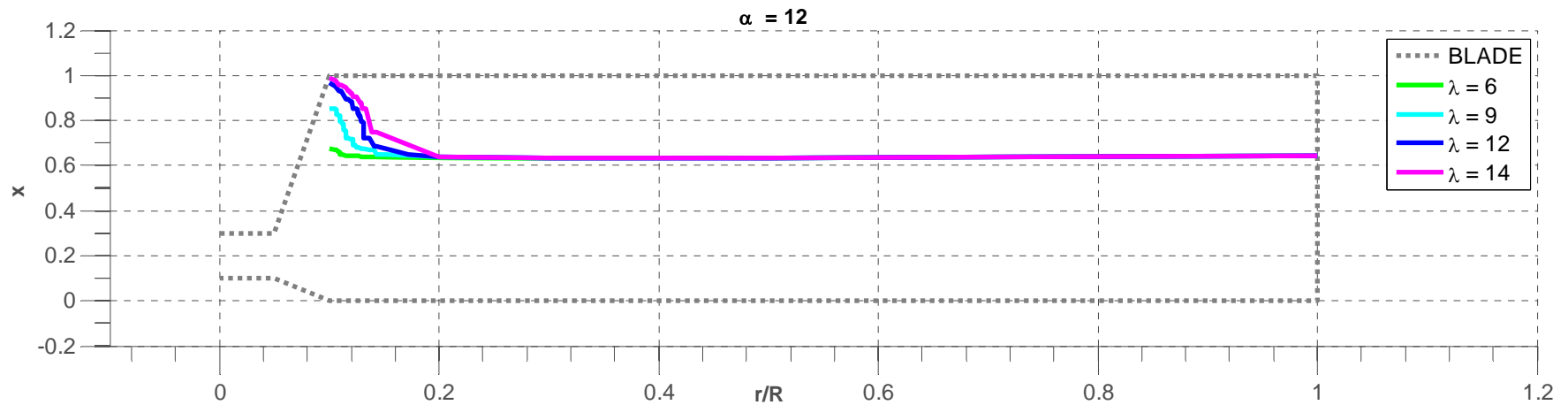
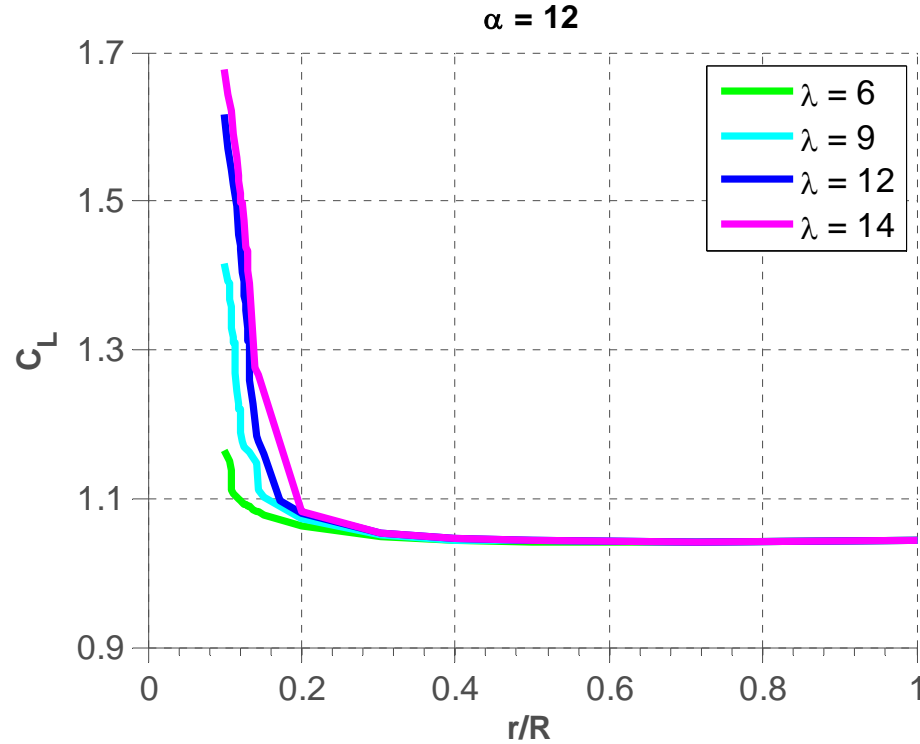
- Tip speed ratio,  $\lambda = \frac{\Omega R}{Q_w}$ 
  - $Q_w = 12.20$  m/s  $\rightarrow \lambda = 6$
  - $Q_w = 8.14$  m/s  $\rightarrow \lambda = 9$
  - $Q_w = 6.11$  m/s  $\rightarrow \lambda = 12$



# QUASI-3D BOUNDARY LAYER

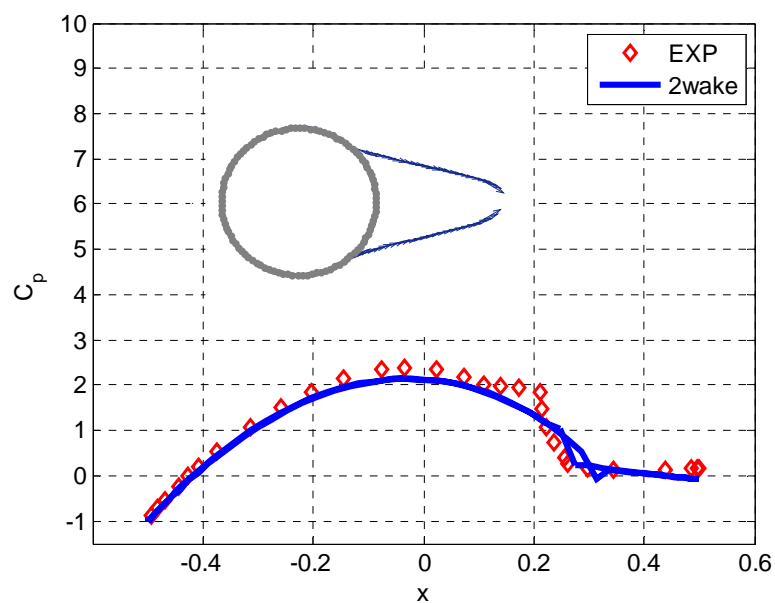
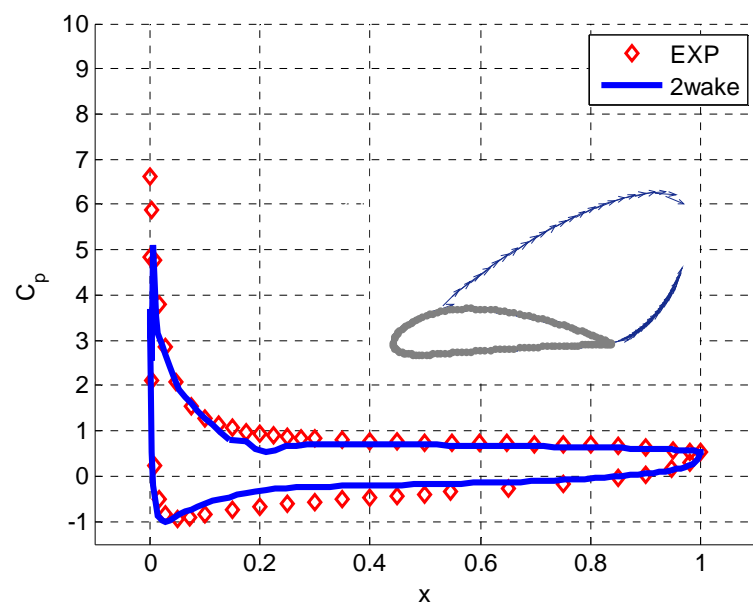
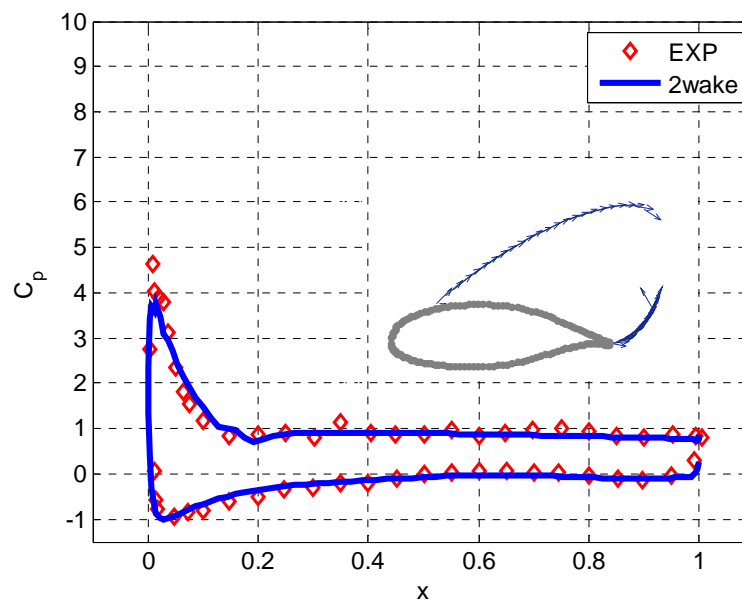
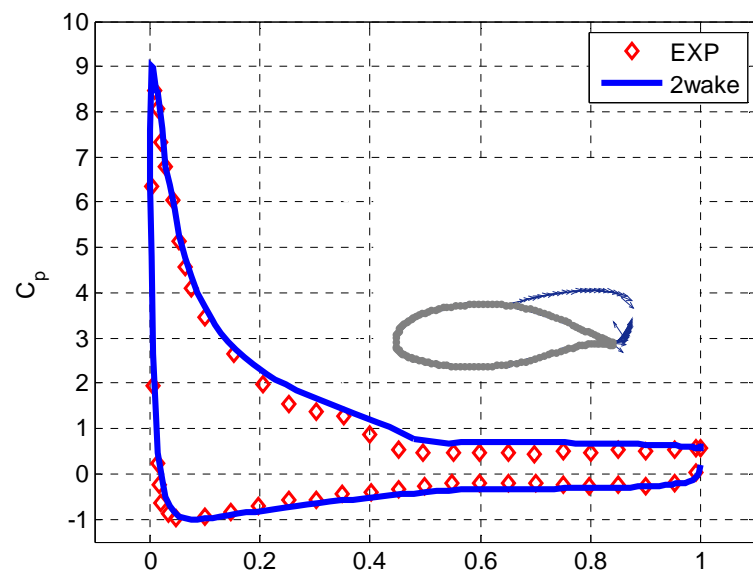


# QUASI-3D BOUNDARY LAYER

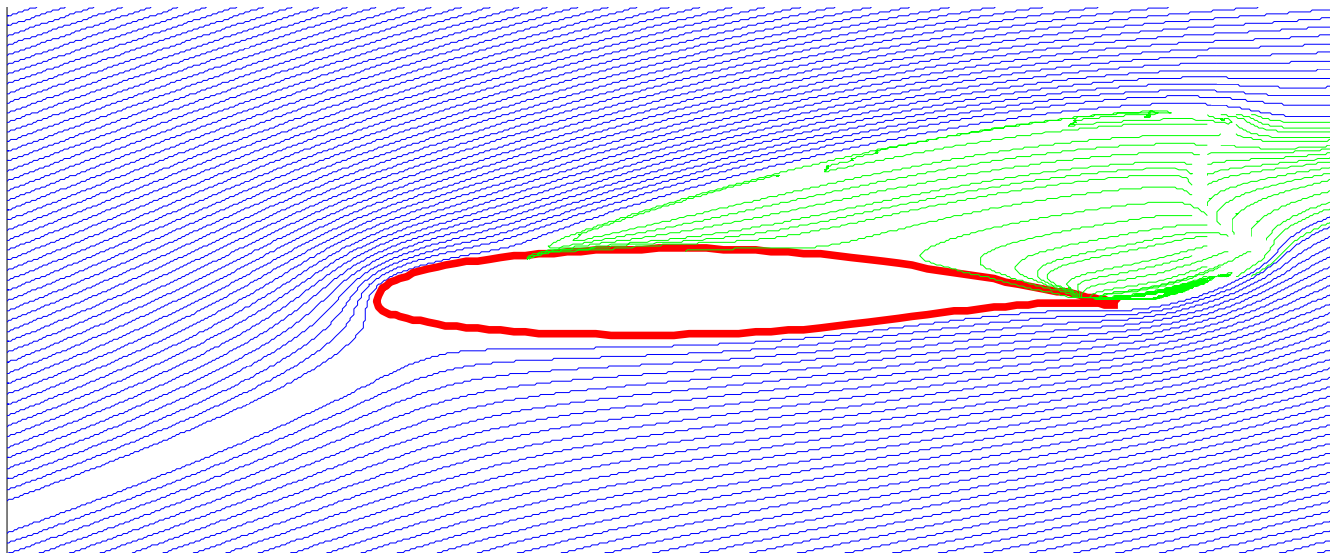
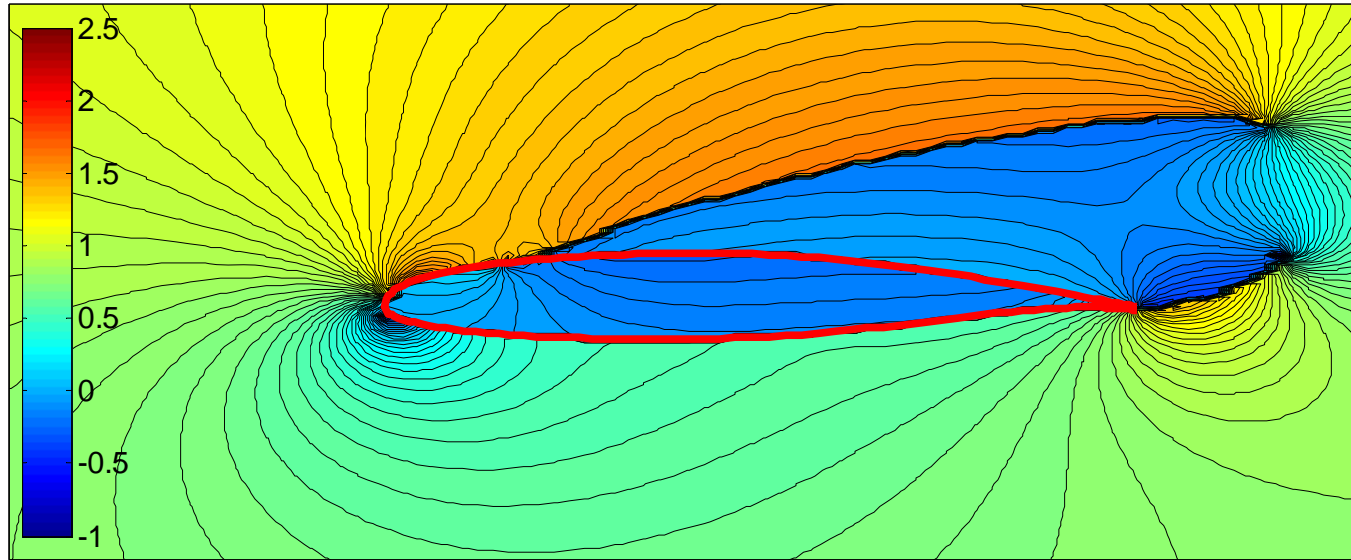


# DOUBLE WAKE POTENTIAL SOLVER

# DOUBLE WAKE MODEL



# DOUBLE WAKE MODEL

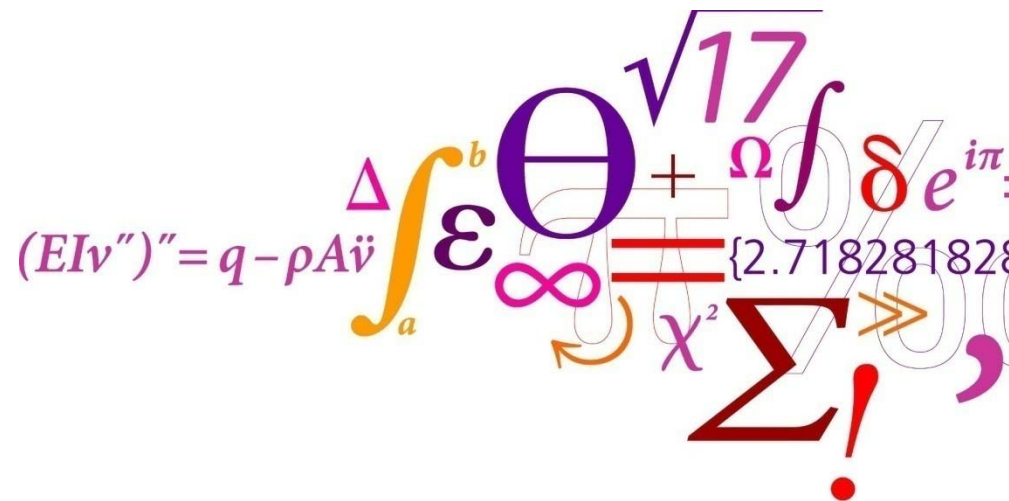


# CONCLUSIONS

- **VISCOUS INVISCID SOLVER IMPLEMENTED**
  - **STEADY 2D**
  - **UNSTEADY 2D**
  - **STEADY Q3D**
  - **STEADY / UNSTEADY 2D/Q3D WITH FLAP**
- **DOUBLE WAKE POTENTIAL SOLVER IMPLEMENTED**
  - **DEEP STALL CONDITIONS**



THANK YOU FOR YOUR ATTENTION.



## **5 PIV measurements on model scale turbine**

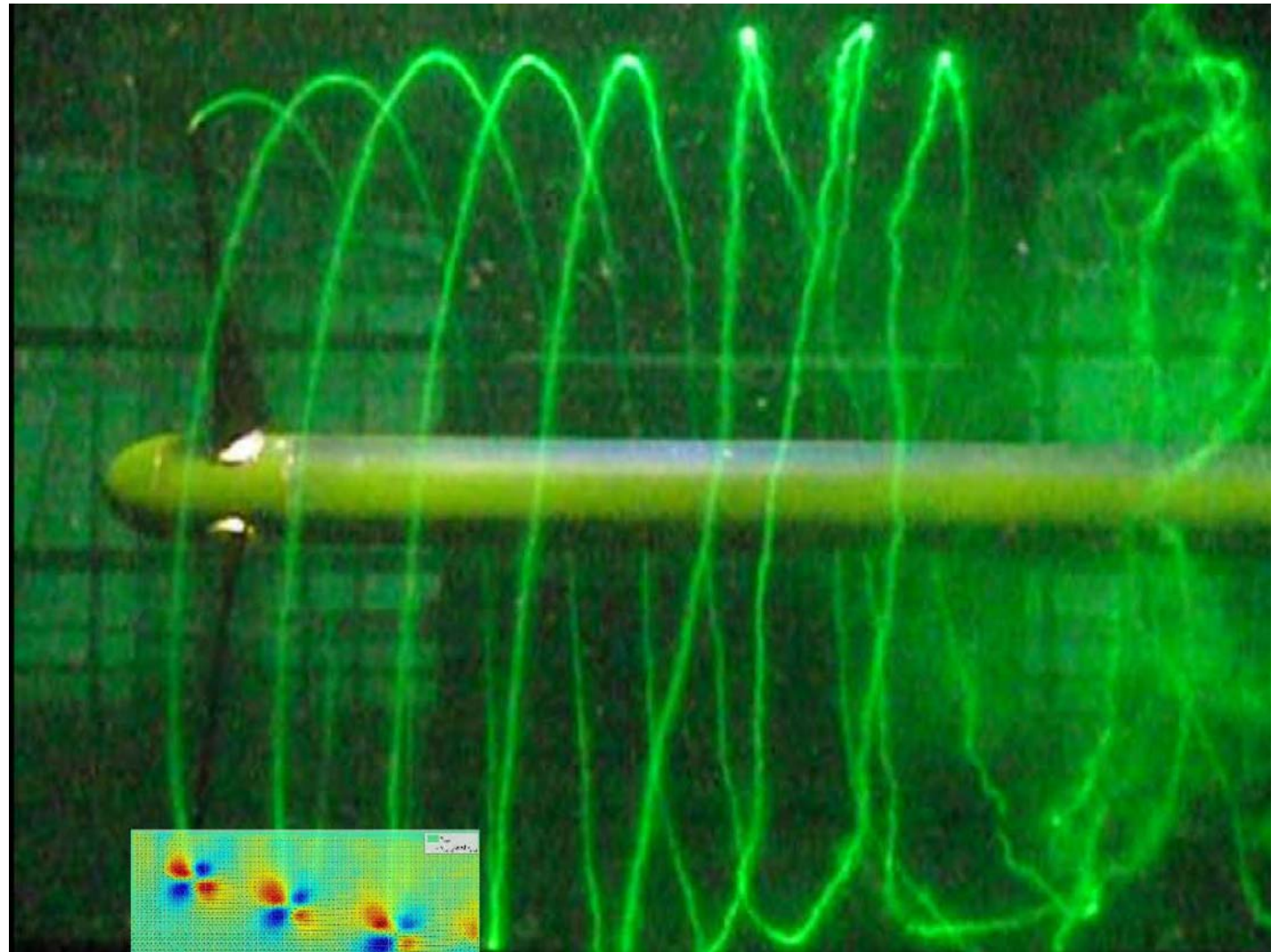
# PIV measurements on a wind turbine in a water flume

by

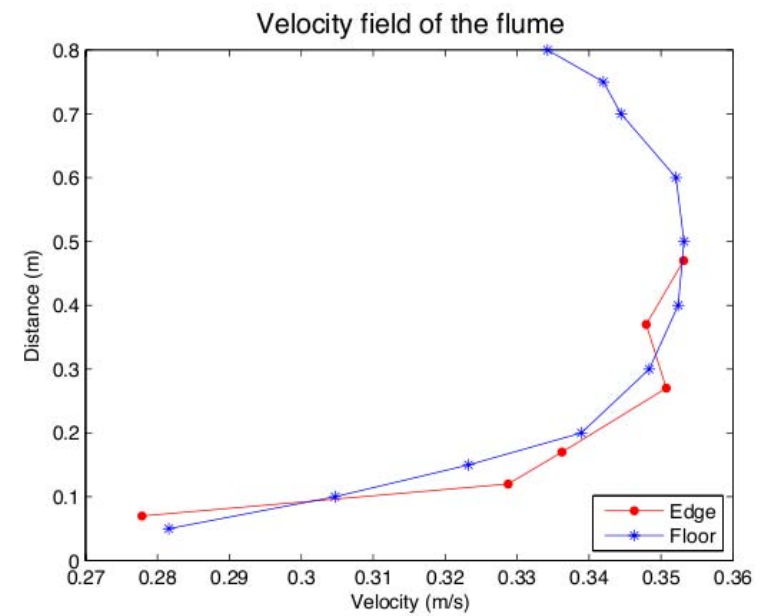
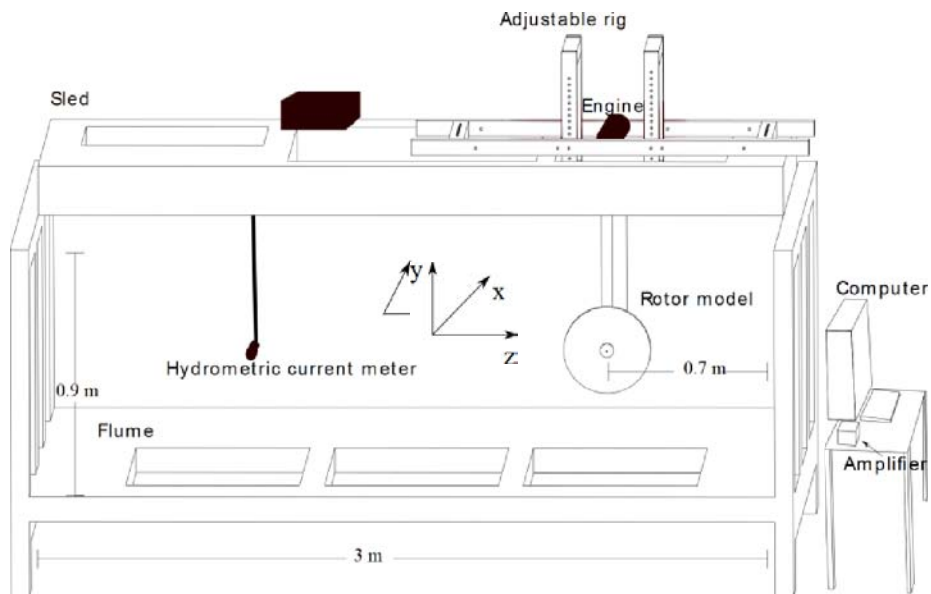
Robert Mikkelsen, Svend Petersen, Kasper Damkjær

## Content

- Setup in flume
- Some results
- Summary

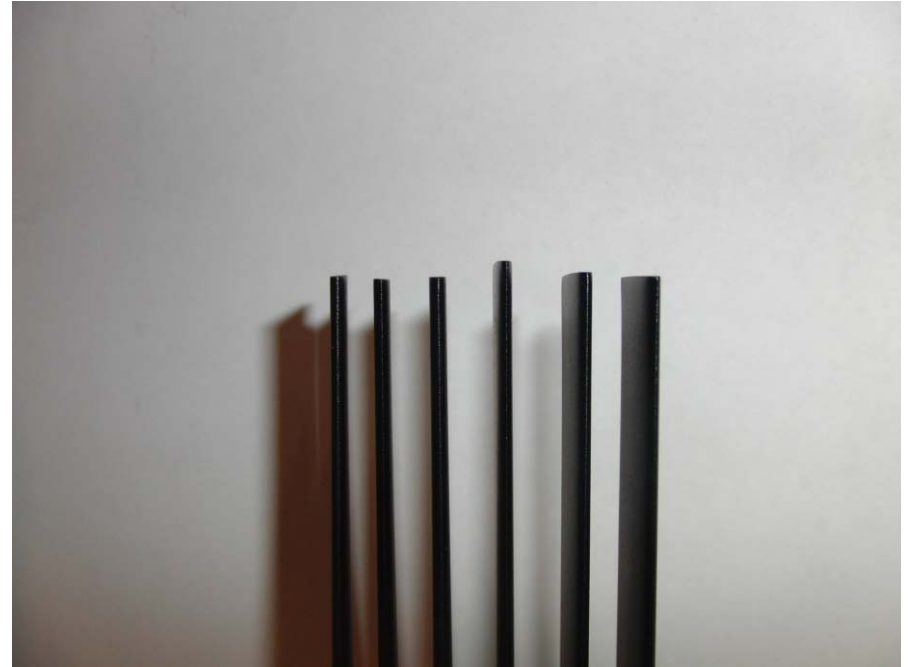
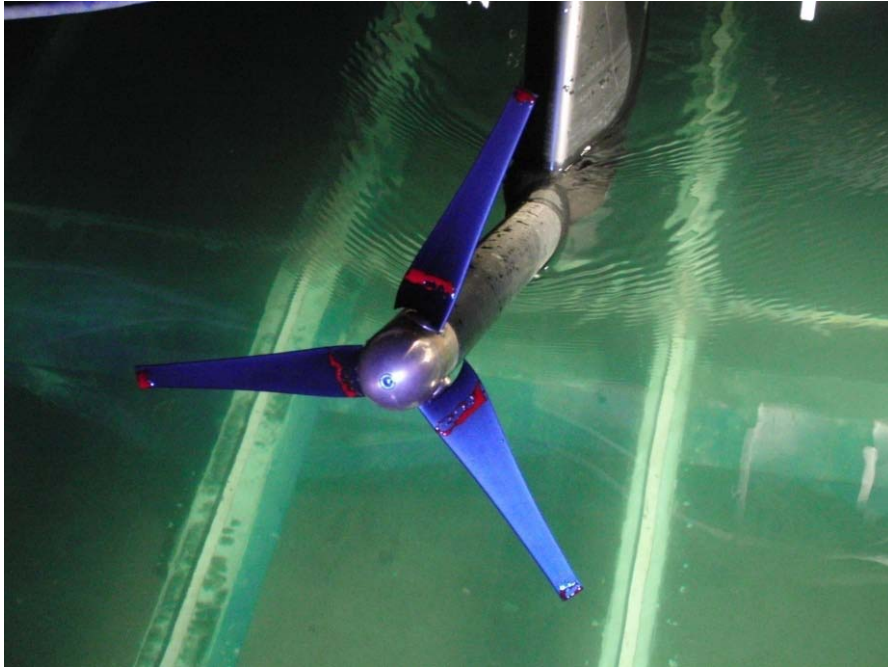


# Flume



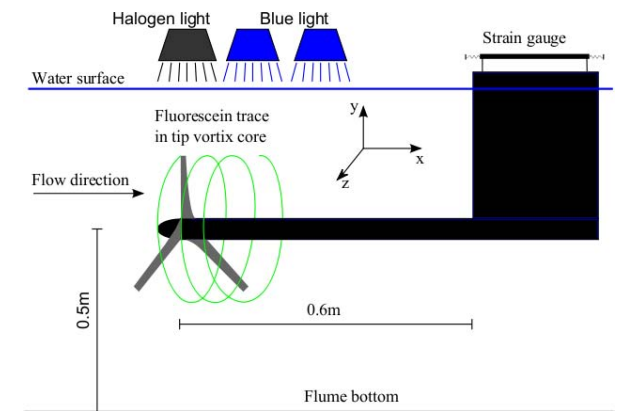
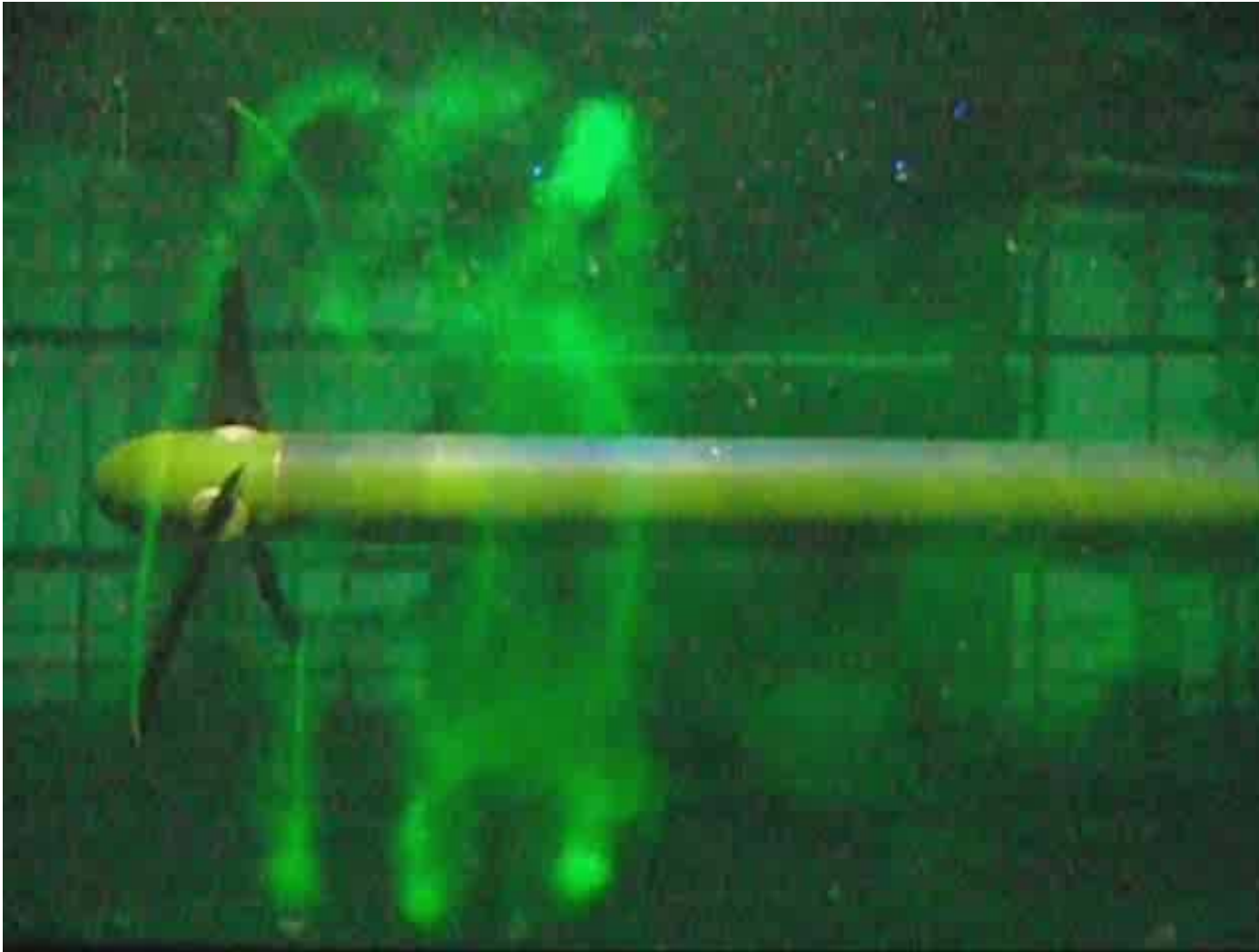


# The turbine – Glauert opt. $\lambda=5$

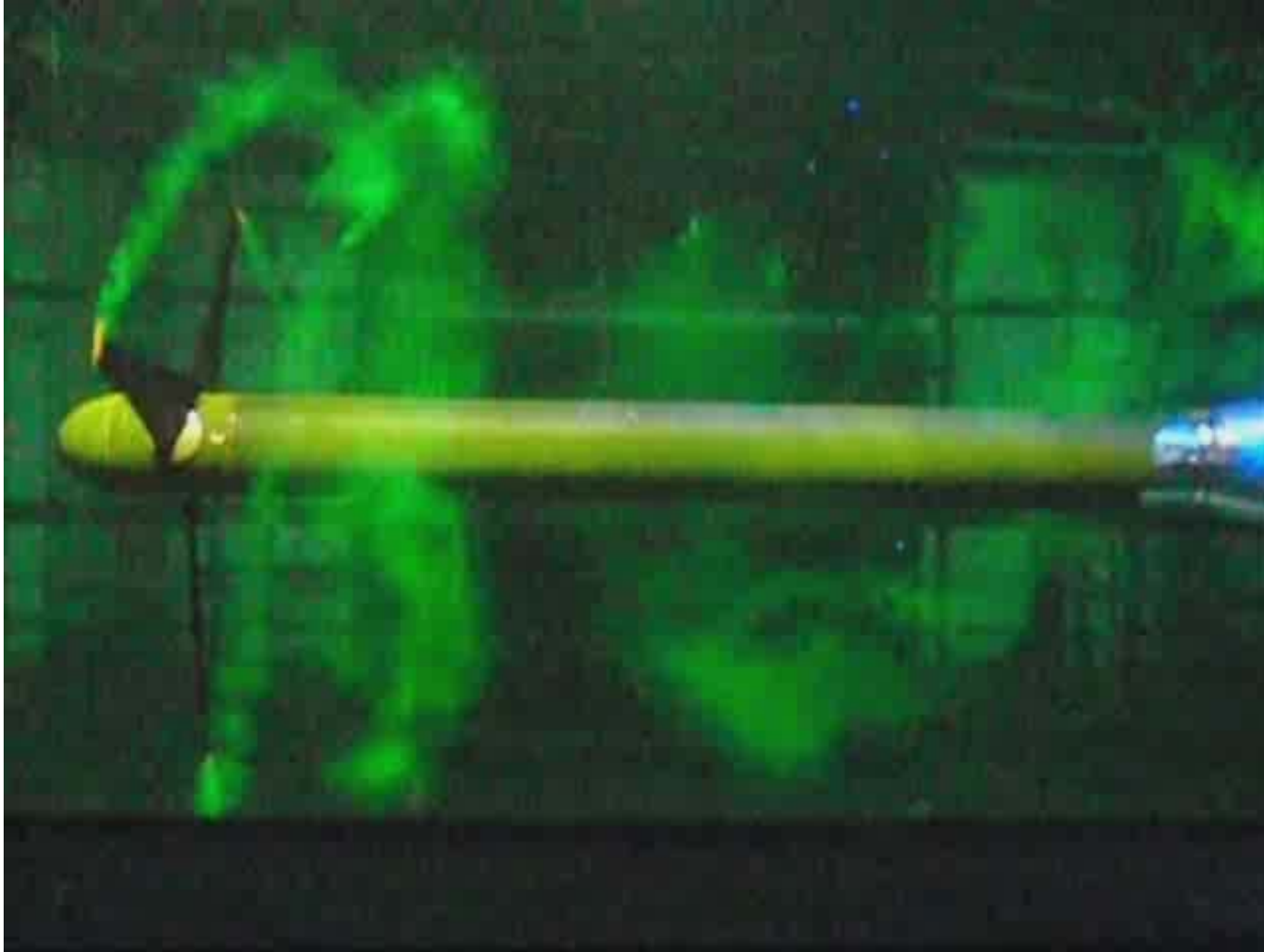


- $D=0.35\text{m}$
- SD7003 aerofoil

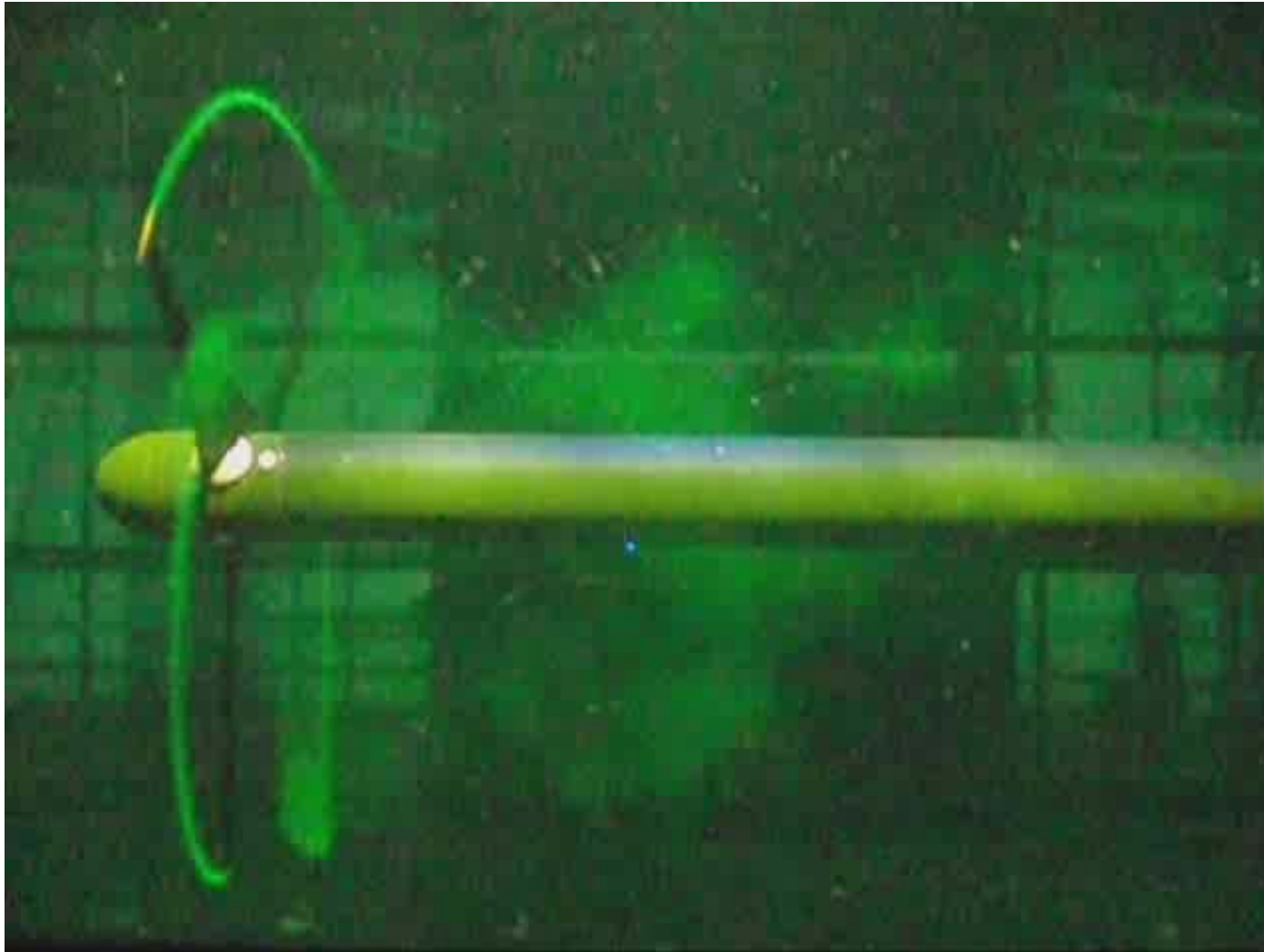
# Fluorescein on tips - TSR 5



# Fluorescein on tips -TSR 4

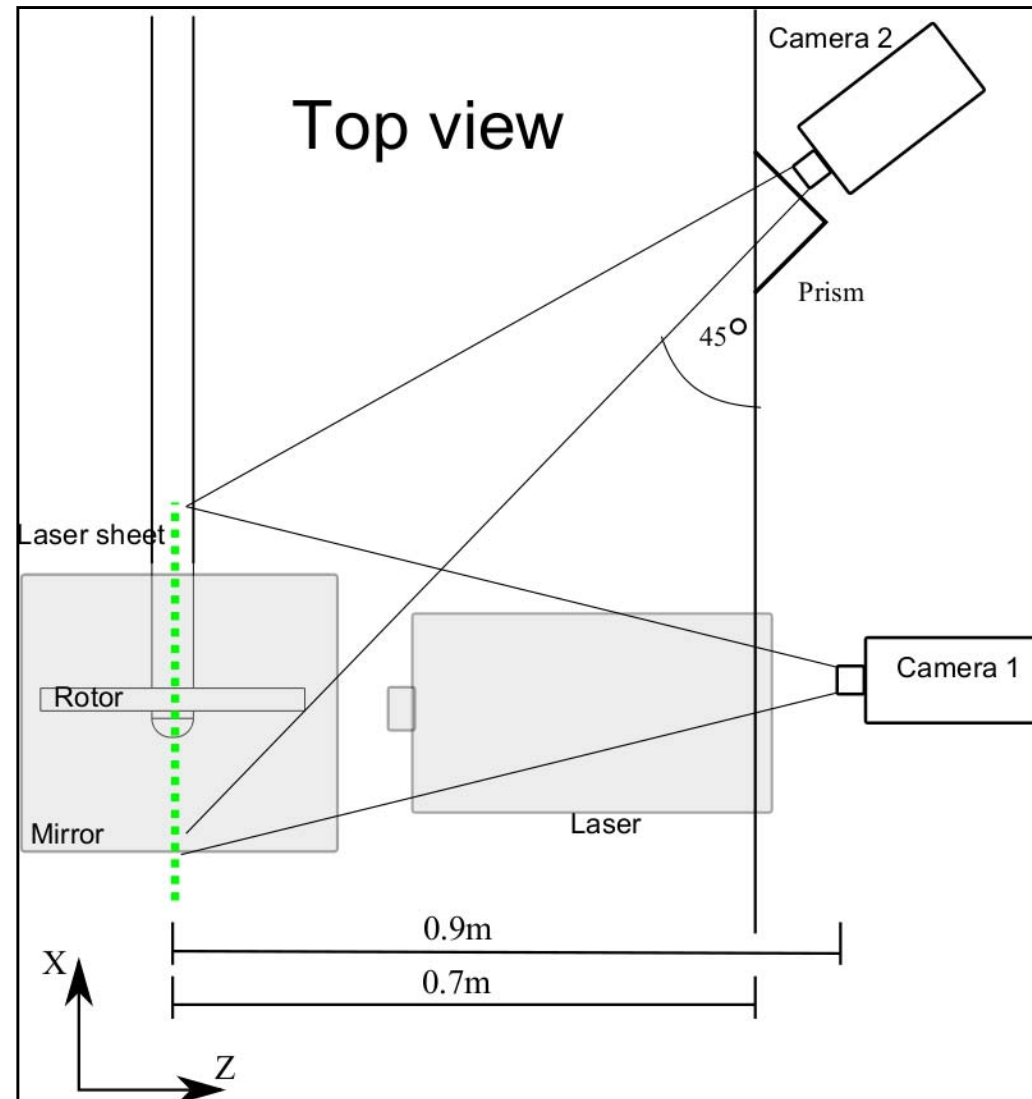
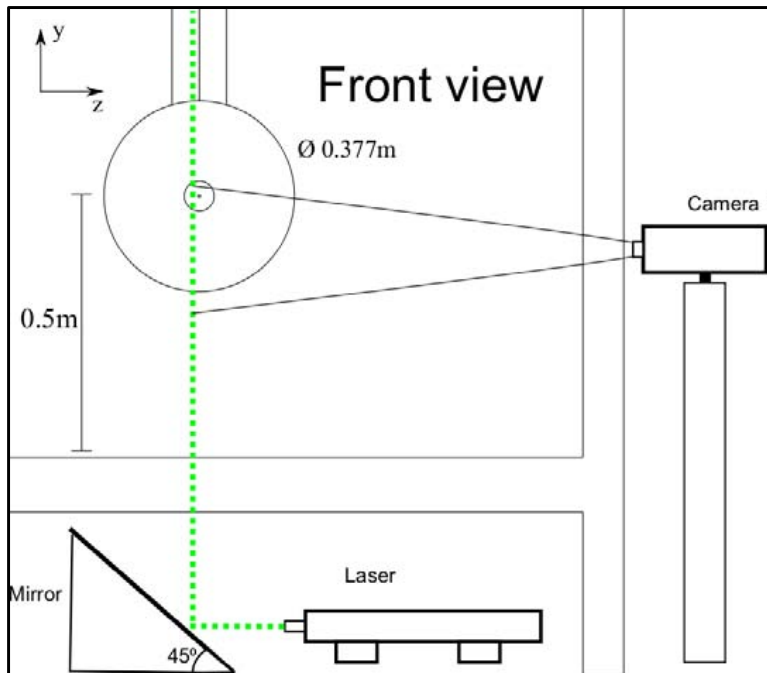


# Fluorescein on tips - TSR 7

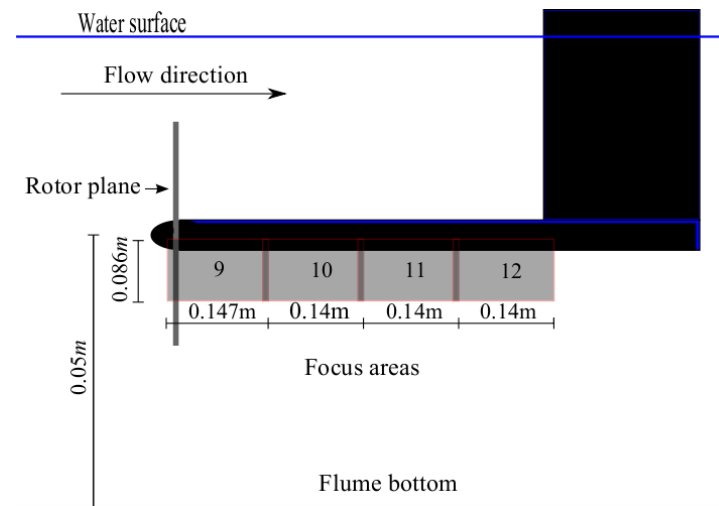
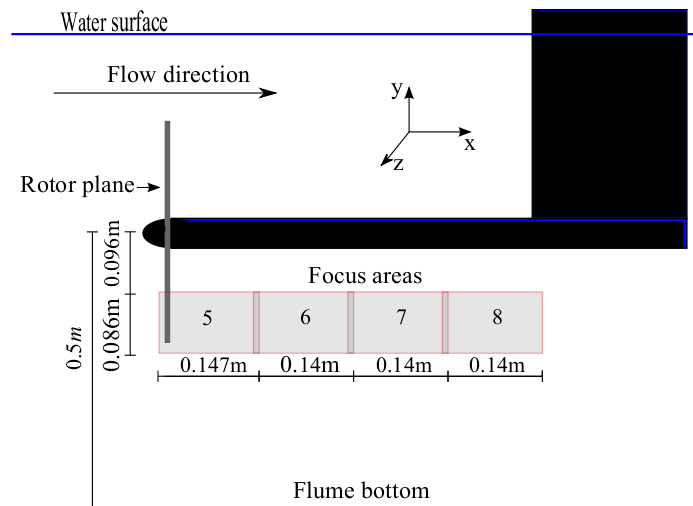
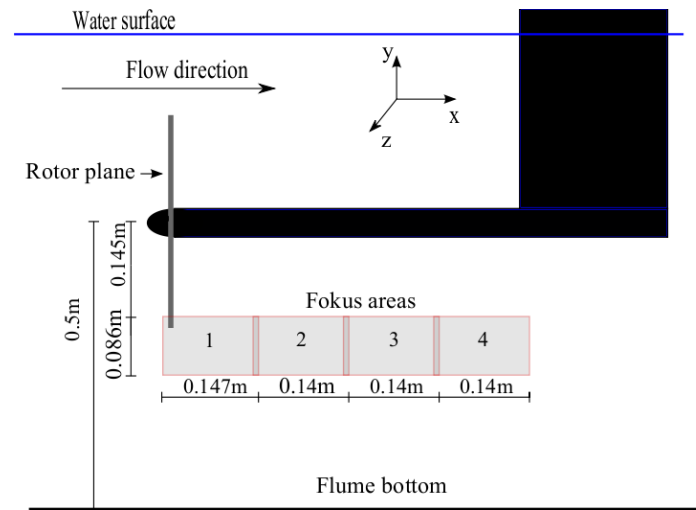
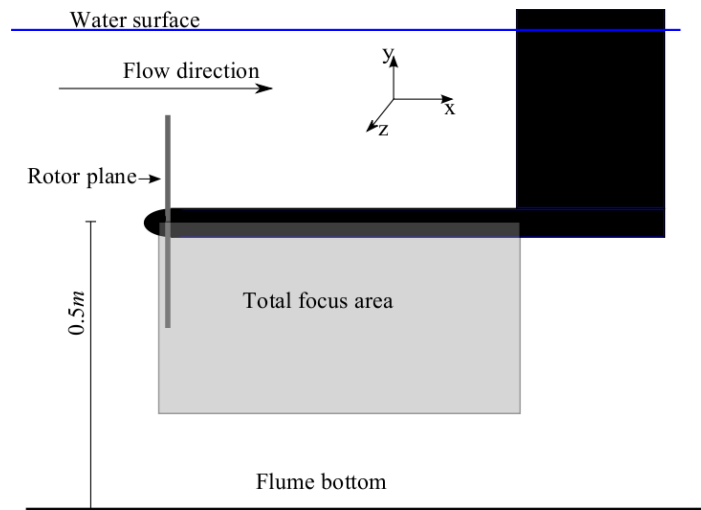




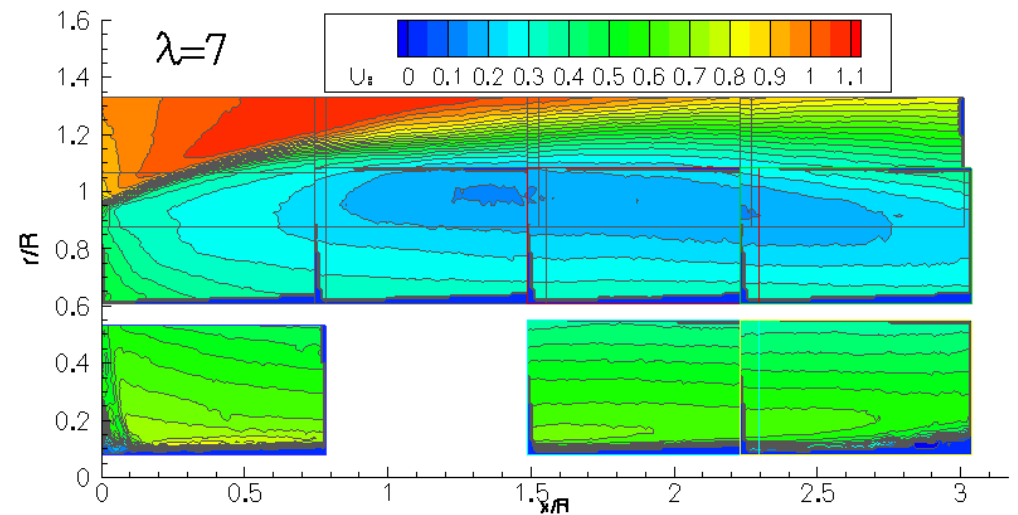
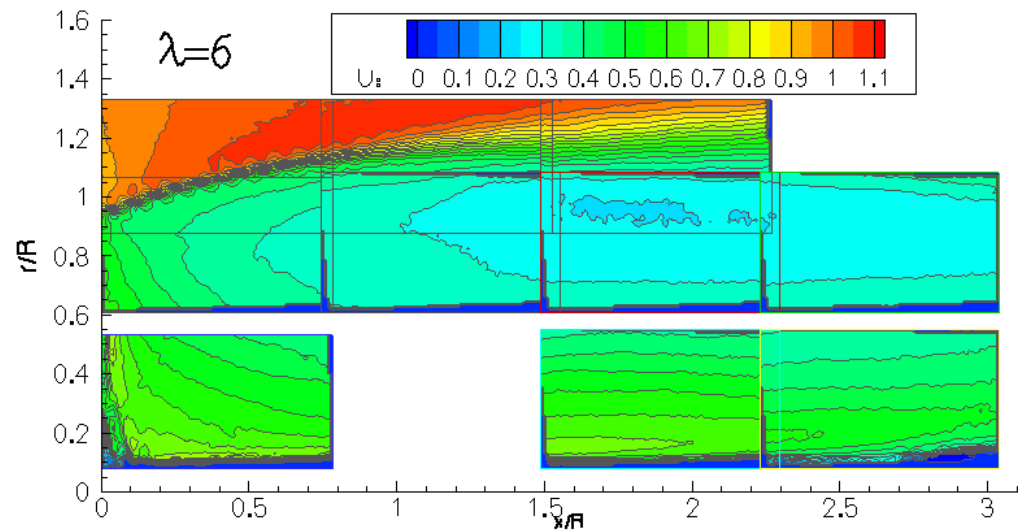
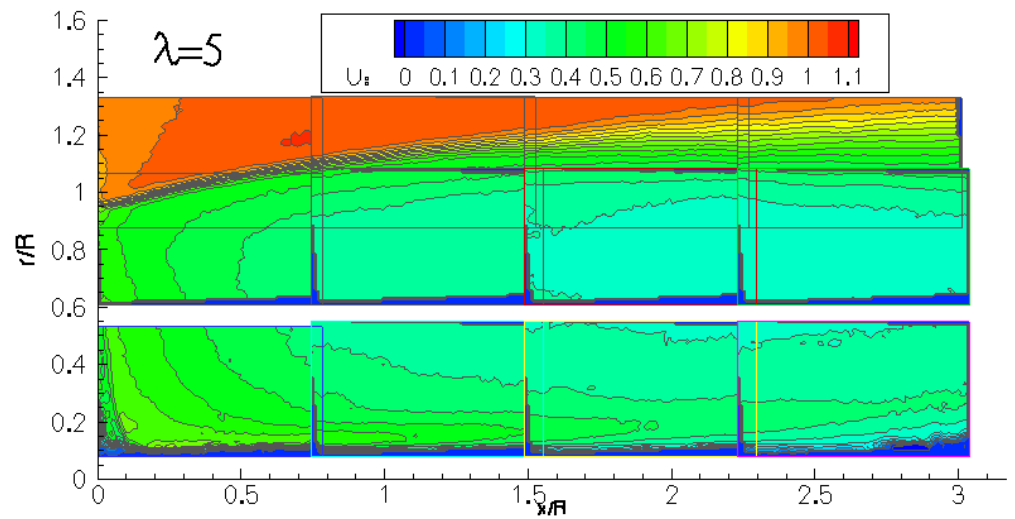
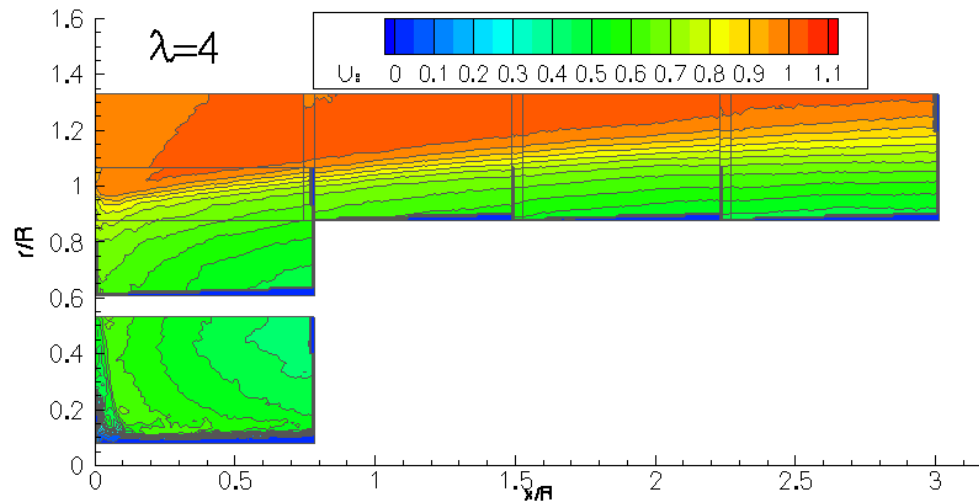
# PIV set-up



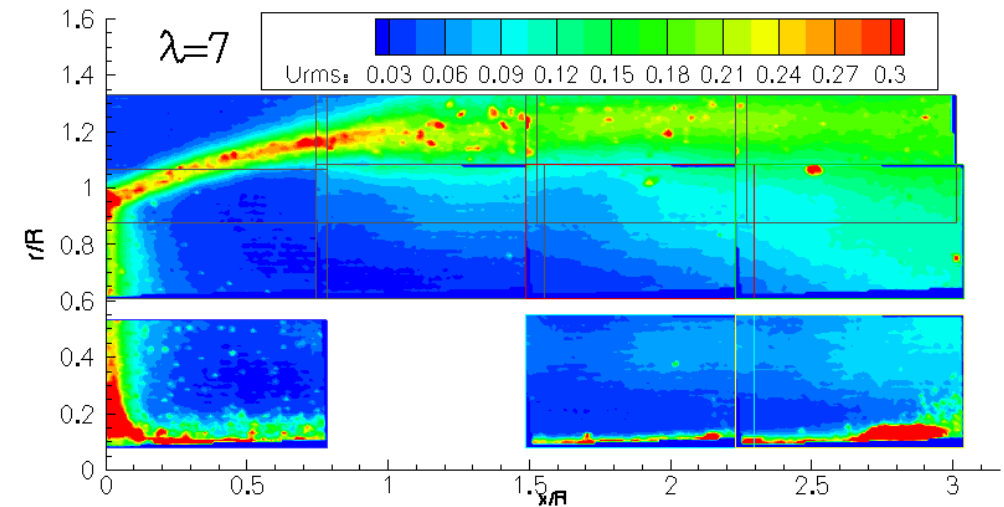
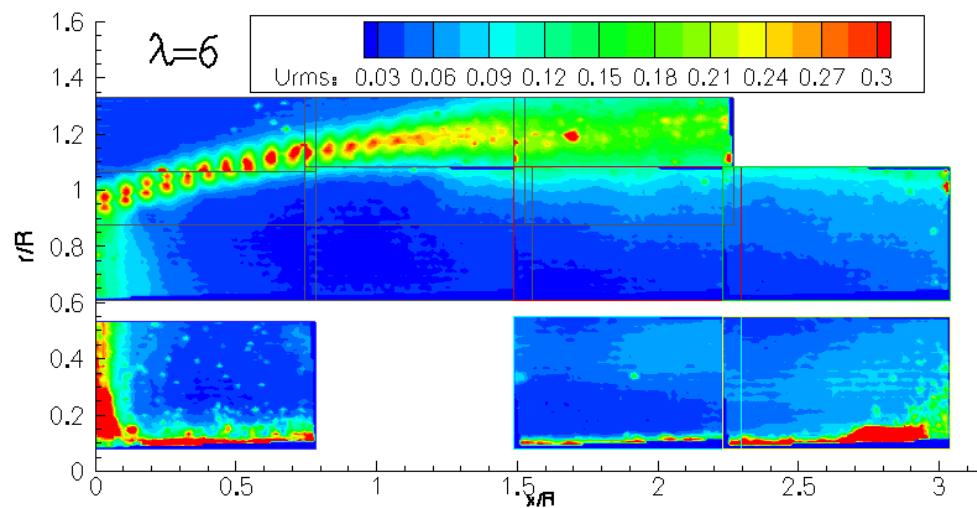
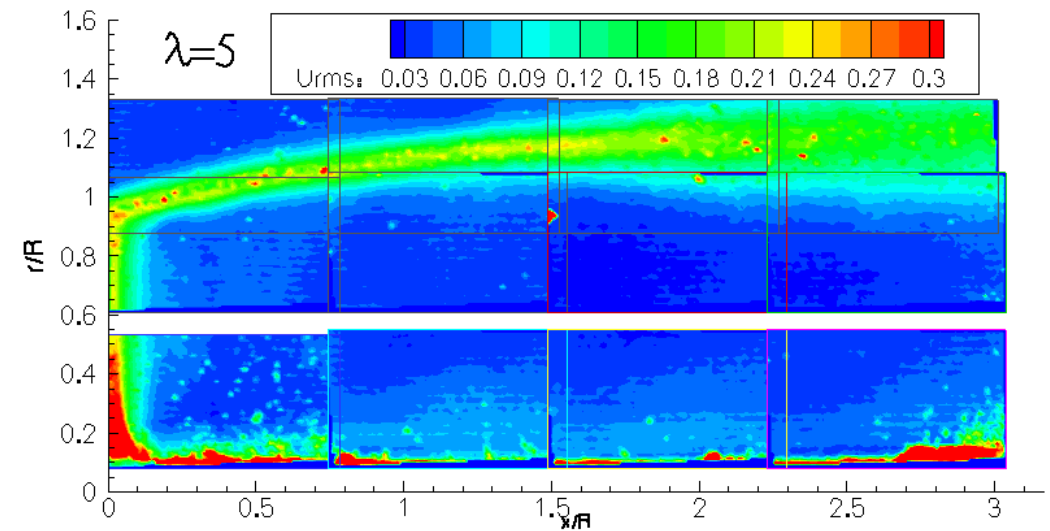
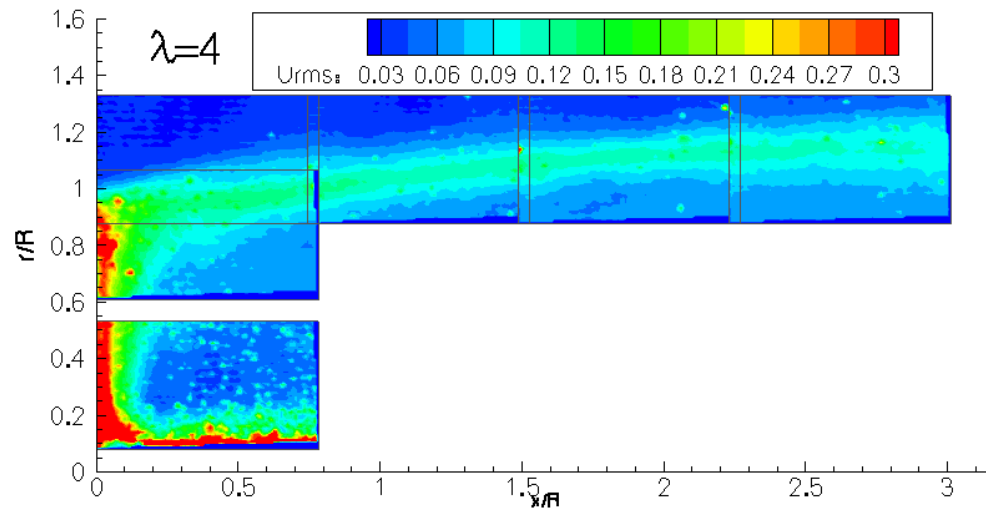
# Focus areas



# PIV, Mean(500) Axial Velocity, TSR 4-7

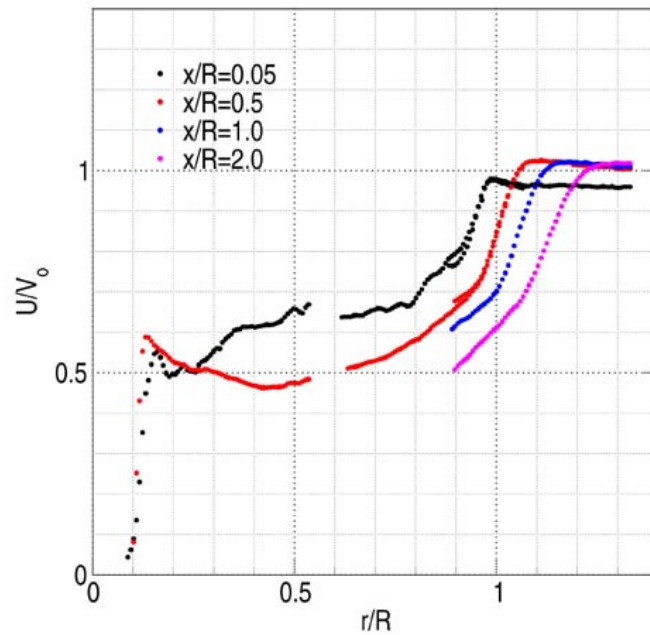


# PIV, Mean Axial Velocity Urms TSR 4-7

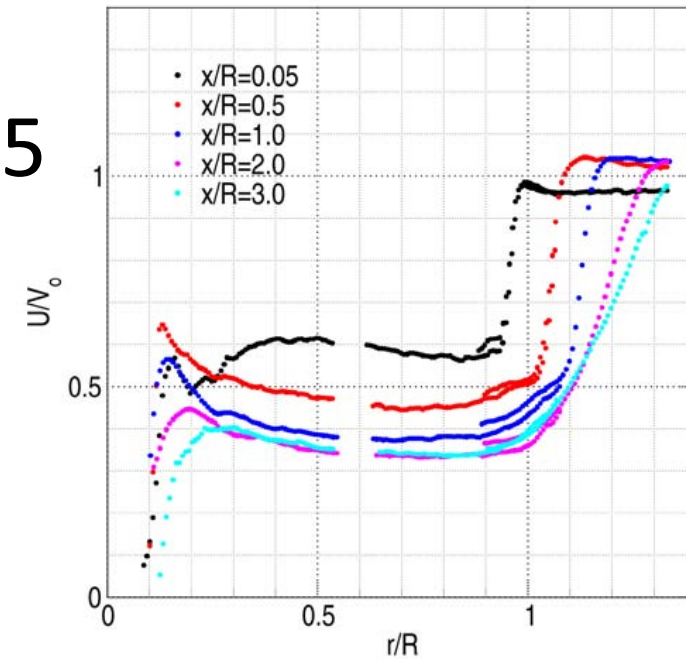


# PIV, Mean Axial Velocity $U$ TSR 4-7

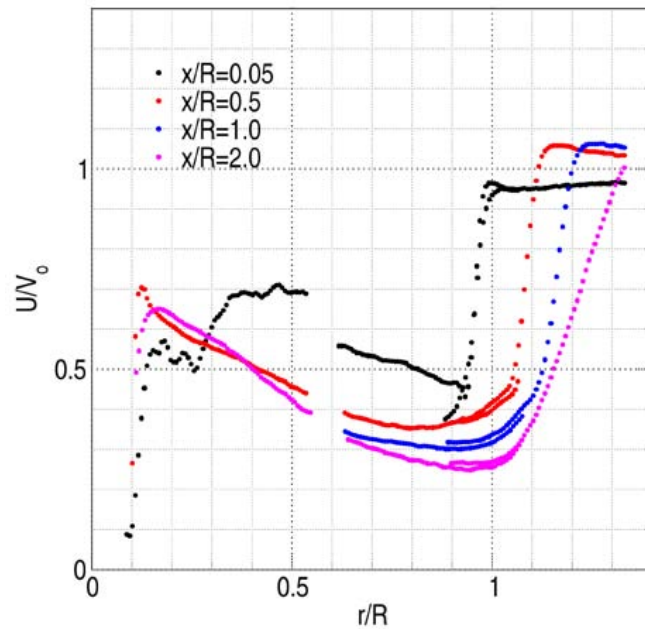
4



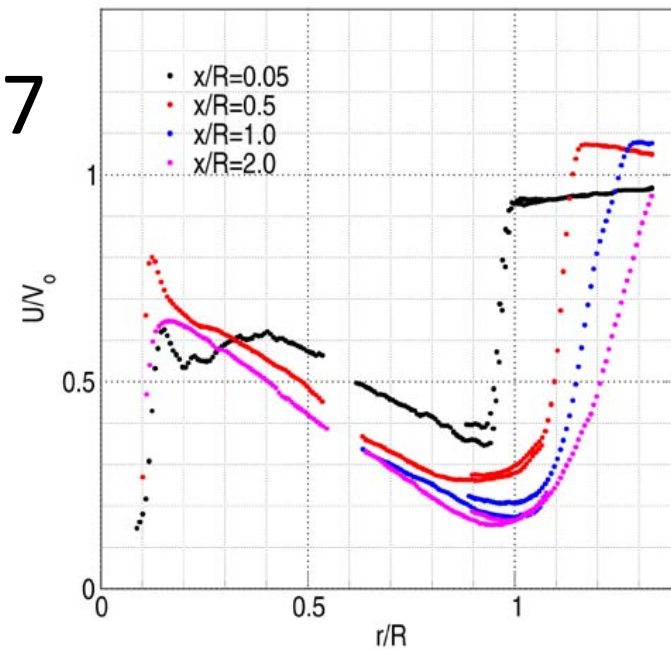
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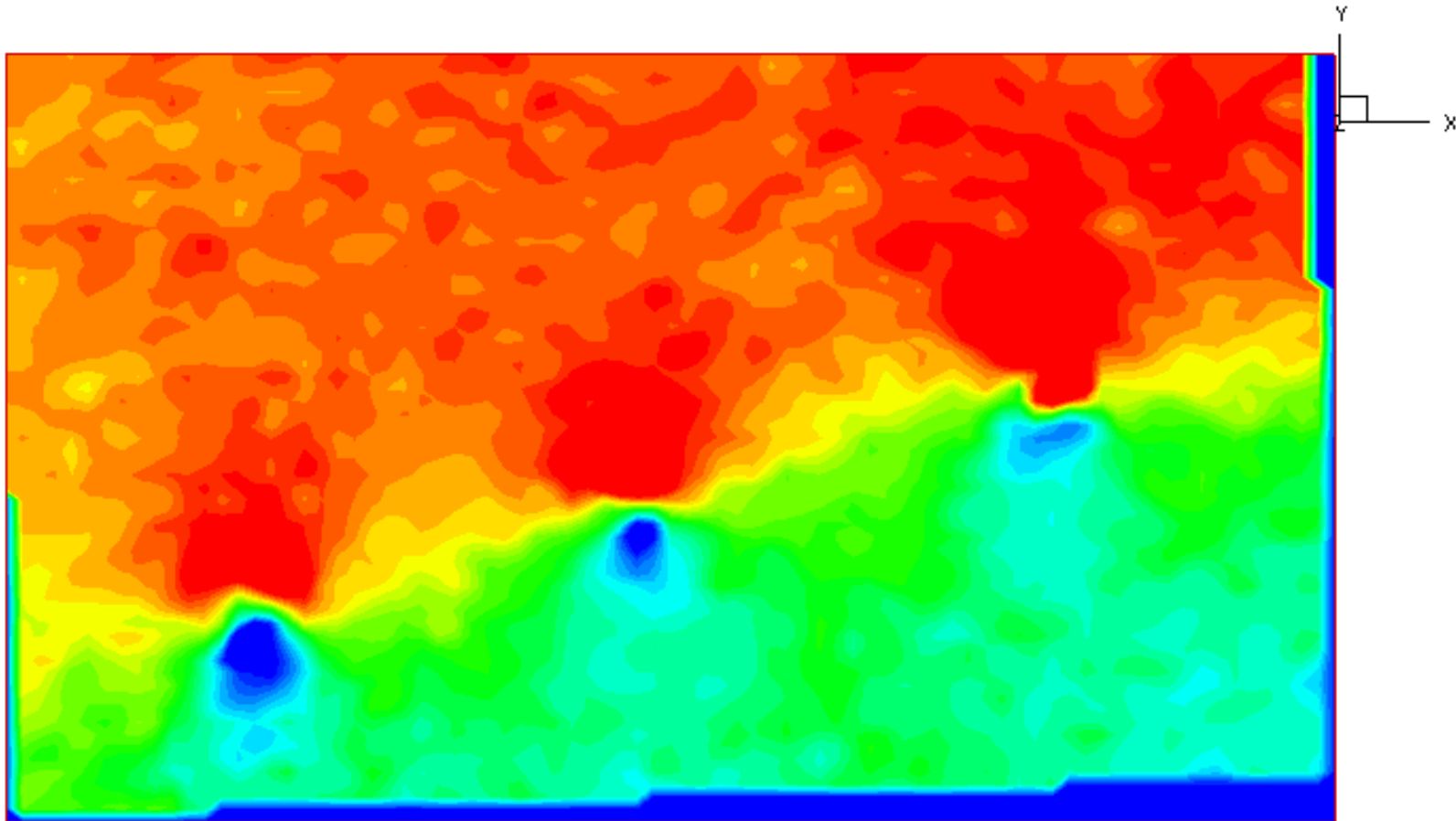
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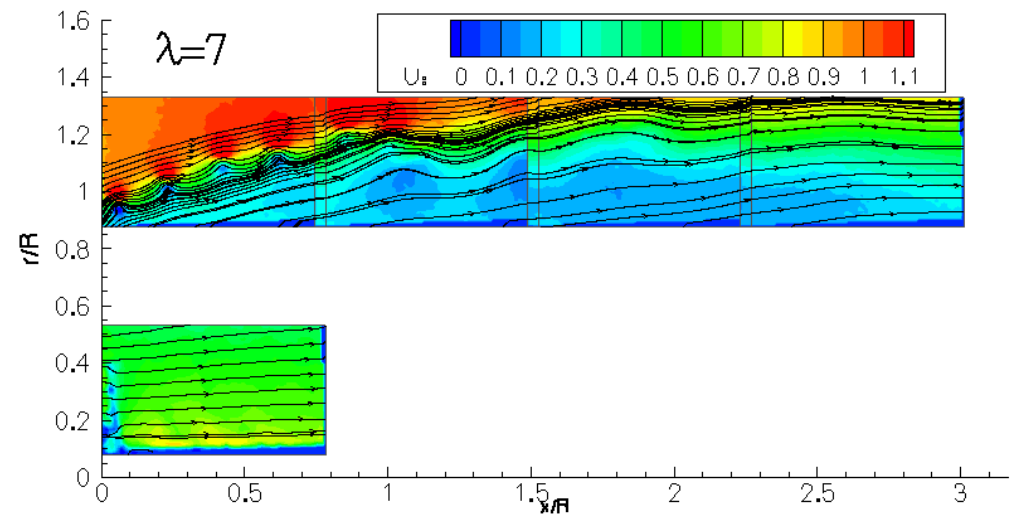
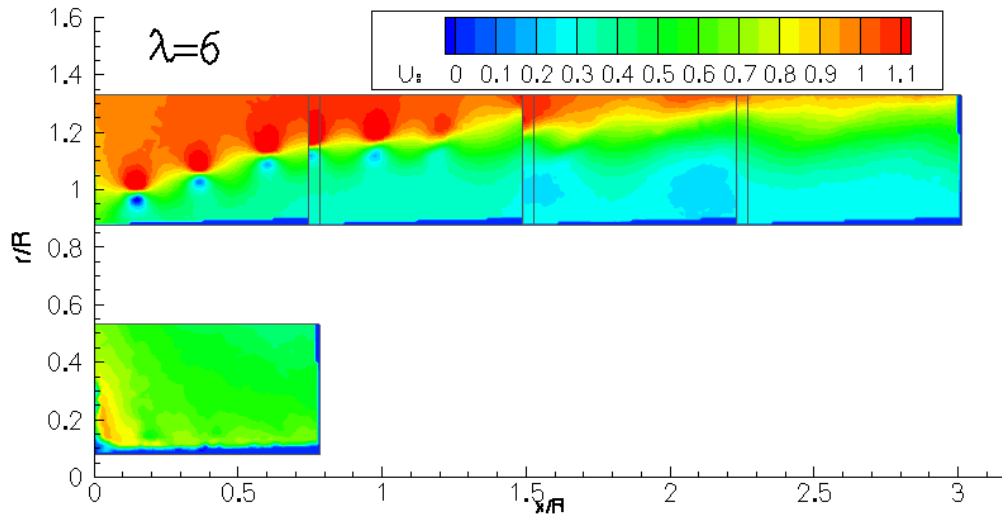
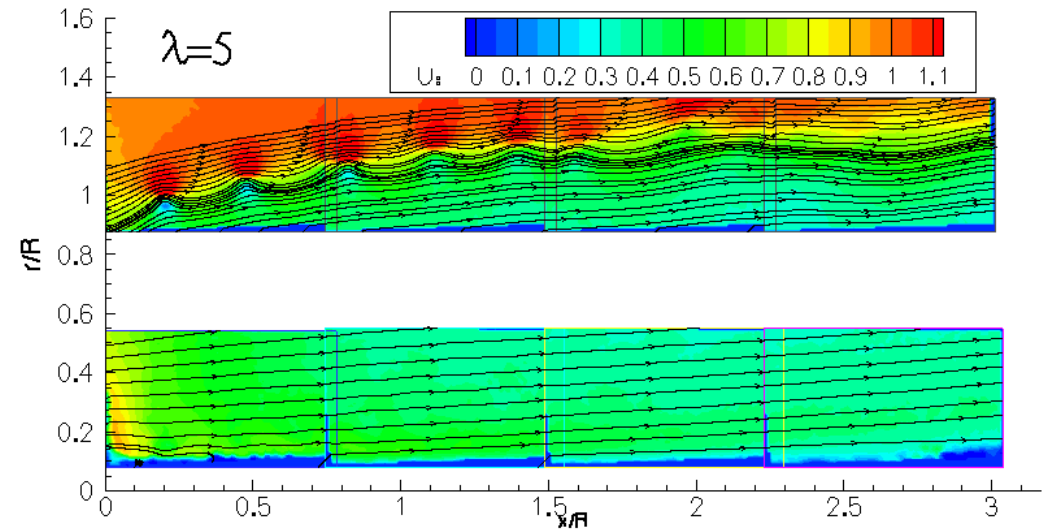
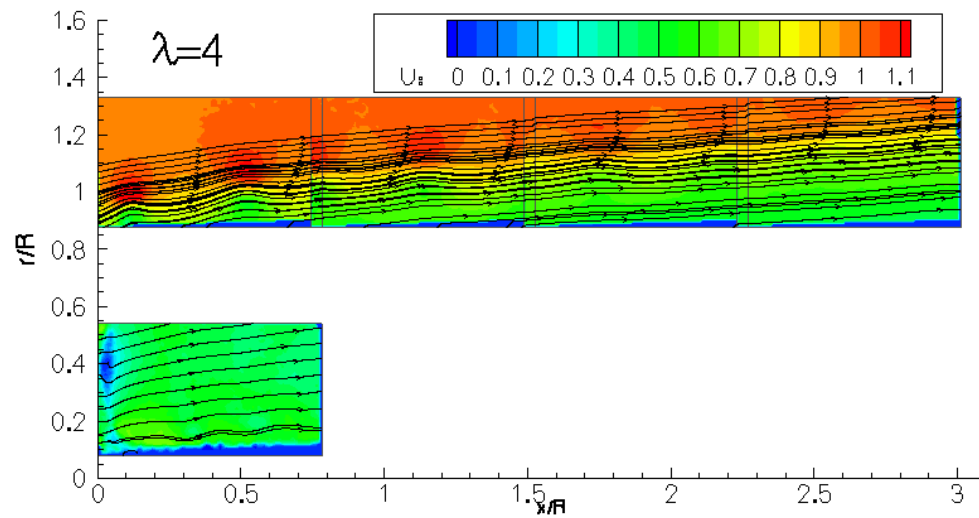
7



# PIV, Phase ave., U-vel, TSR 6

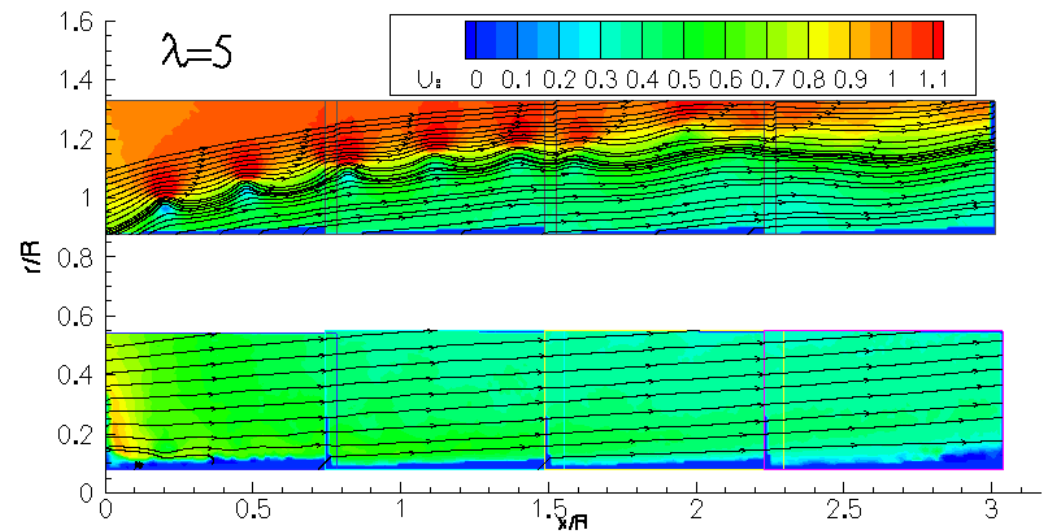
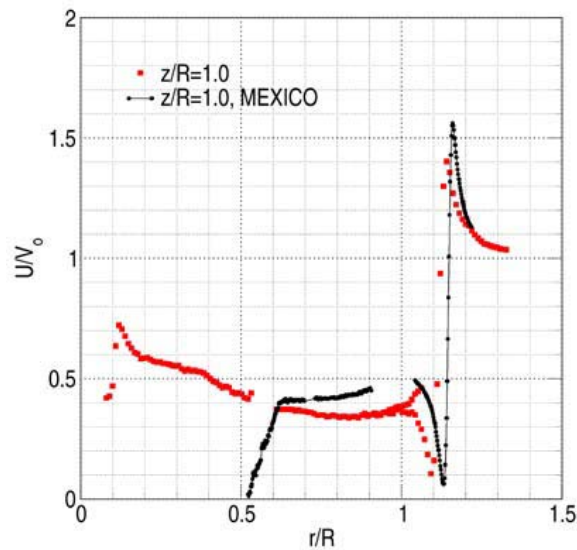
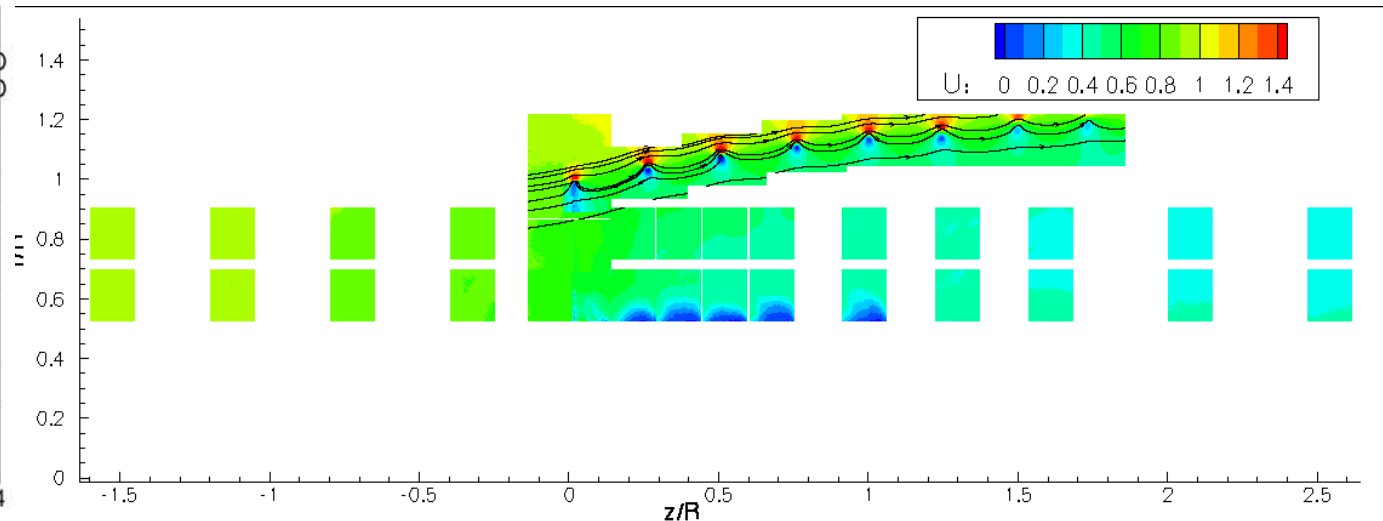
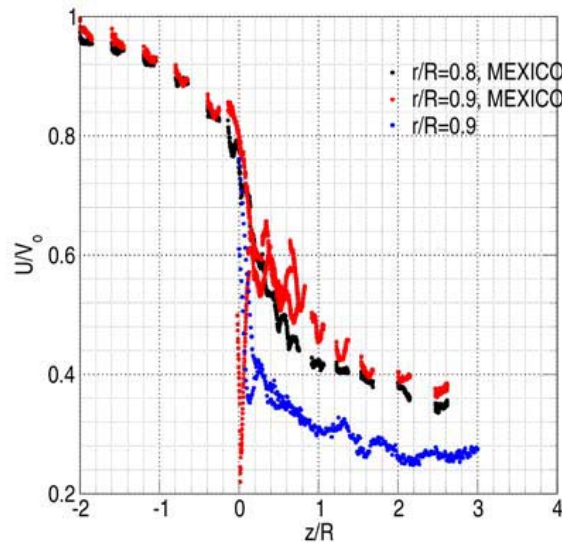


# PIV, Phase Average(100) $U_{ax}$ TSR 4-7



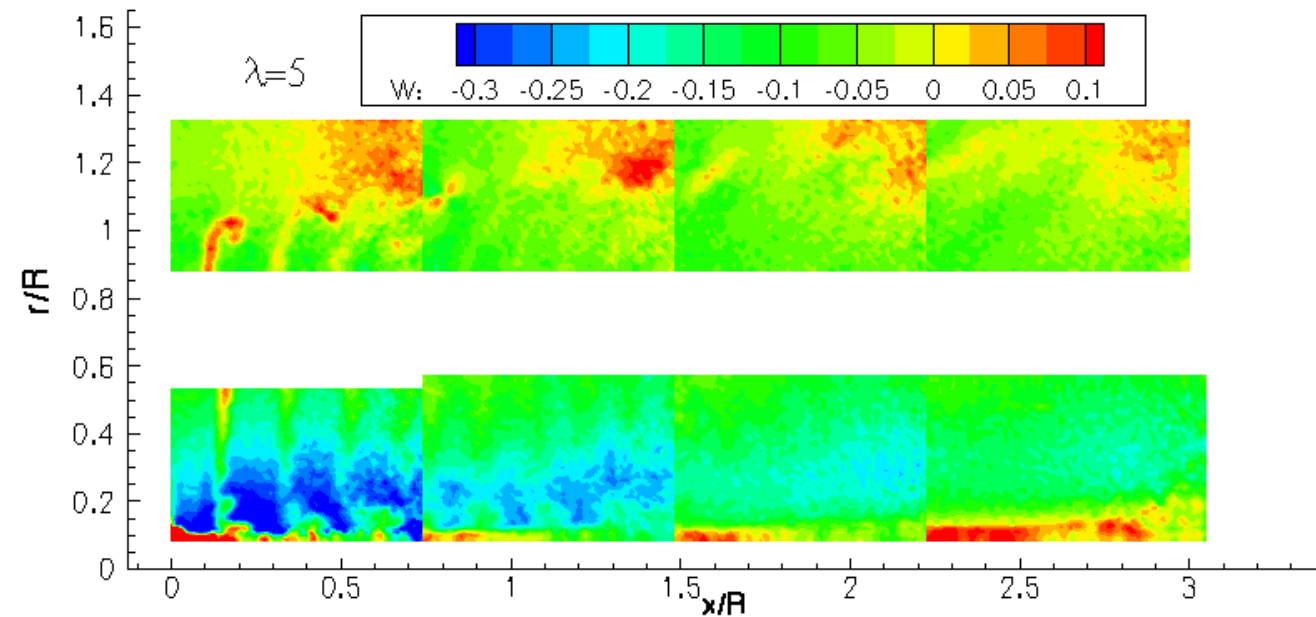
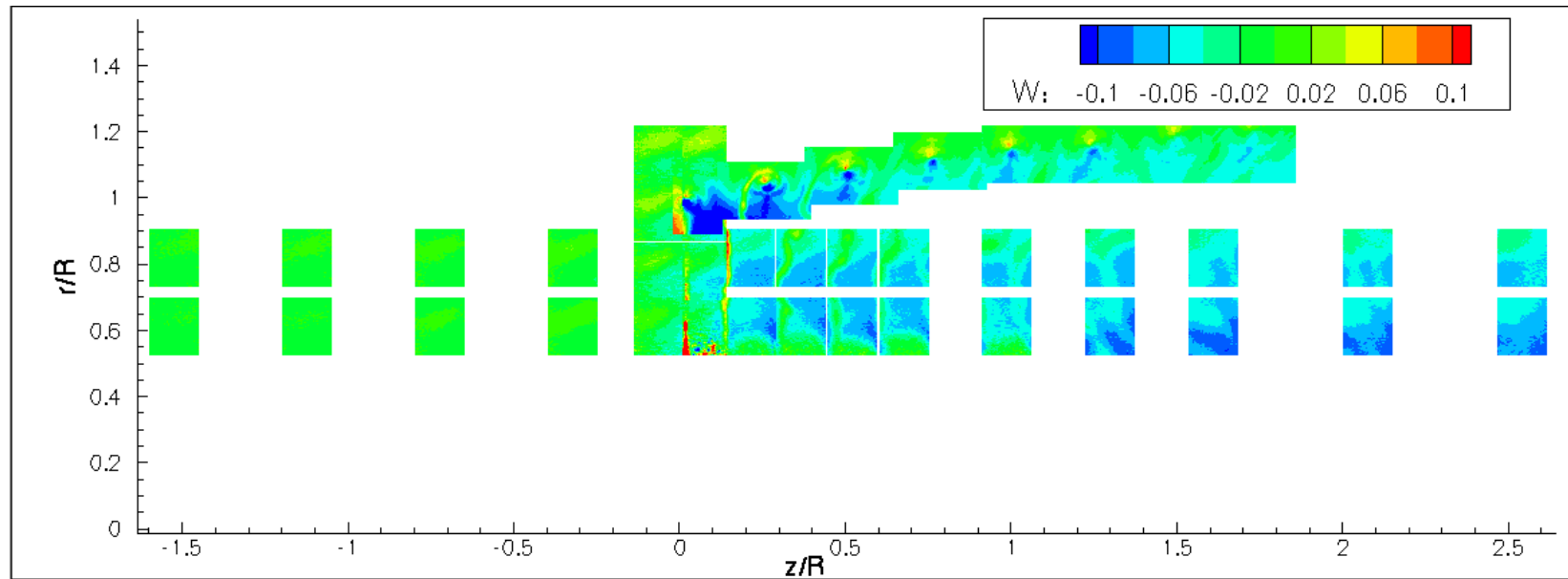


# MEXICO PIV, Phase Ave., $U_{ax}$

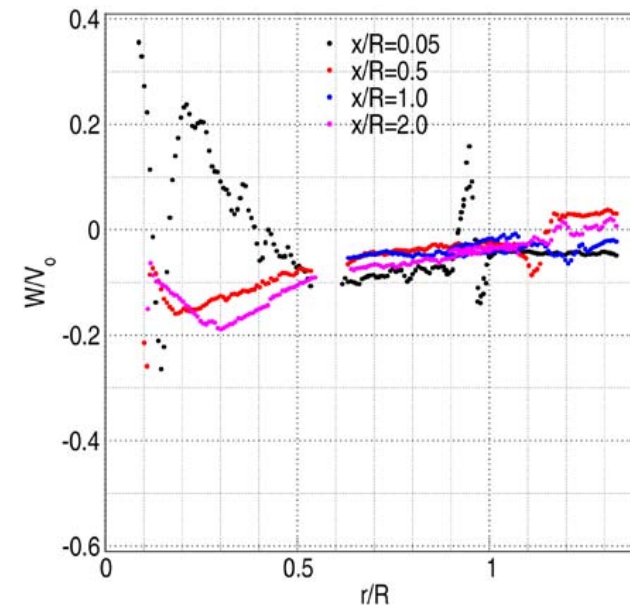
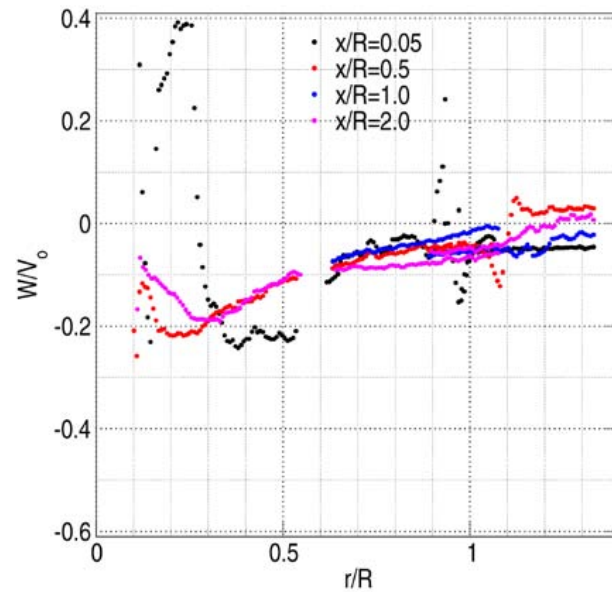
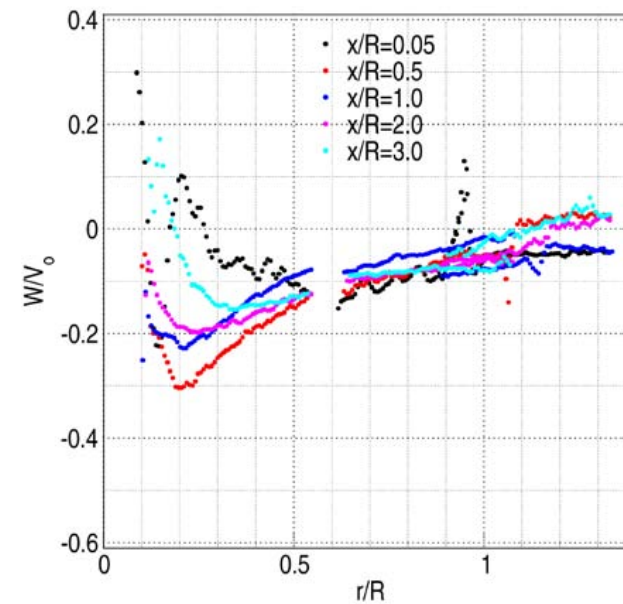
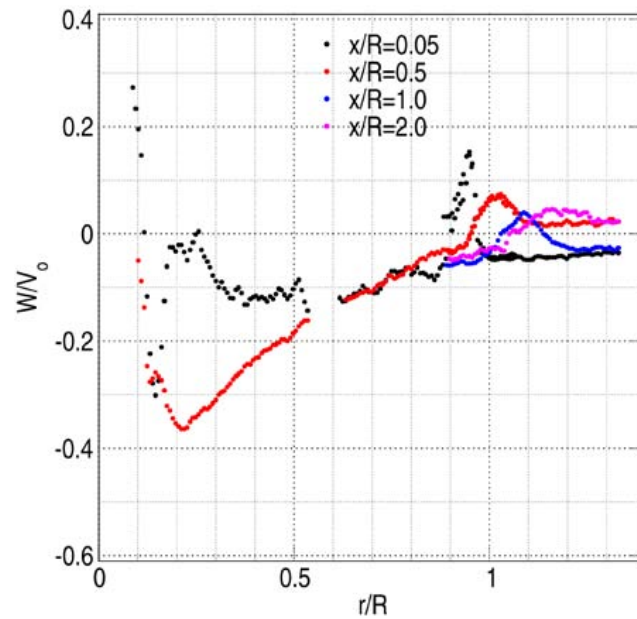




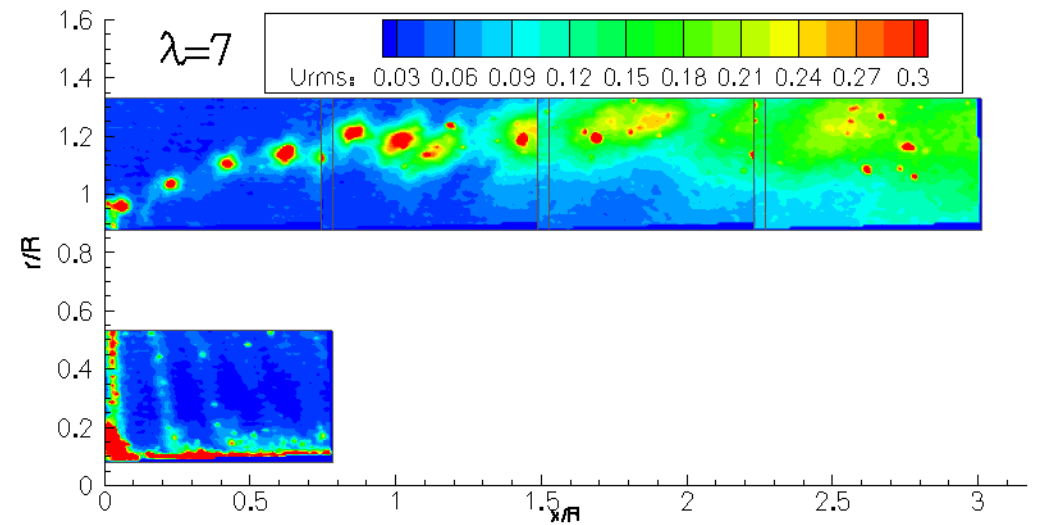
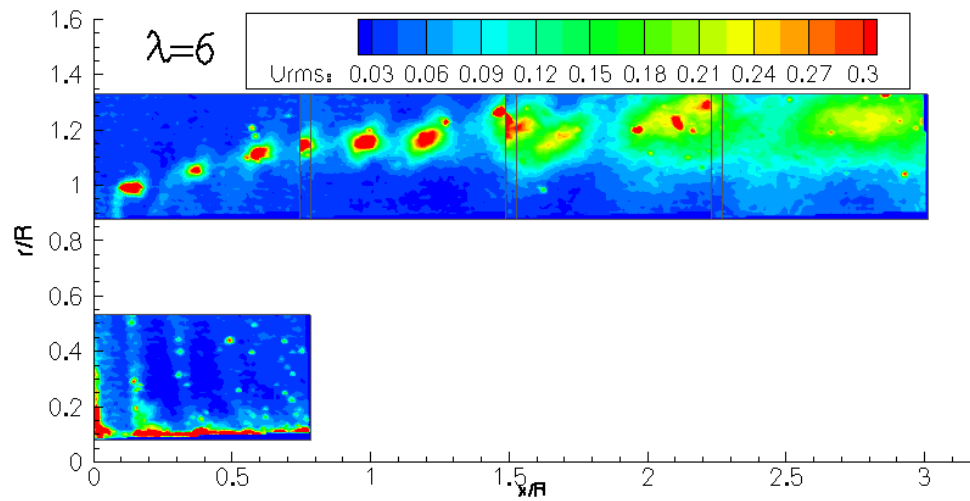
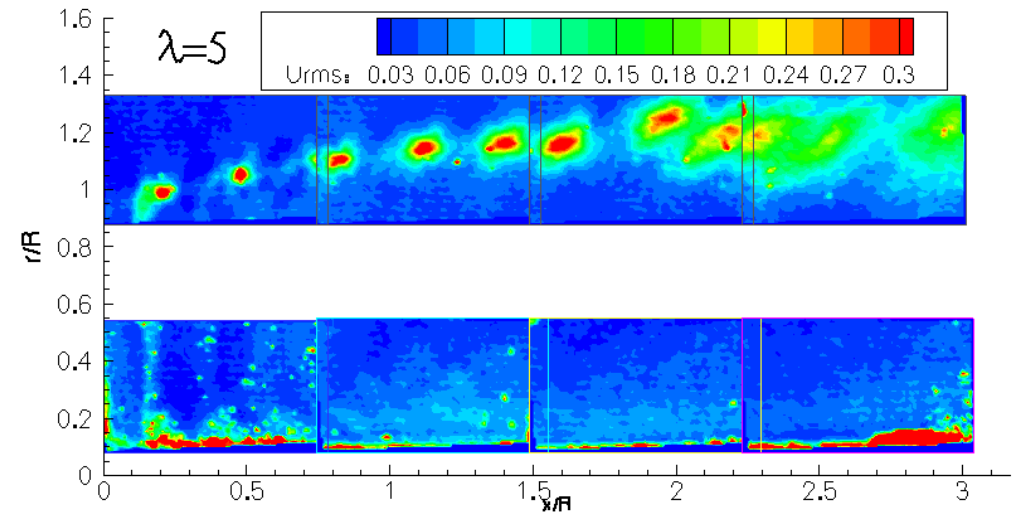
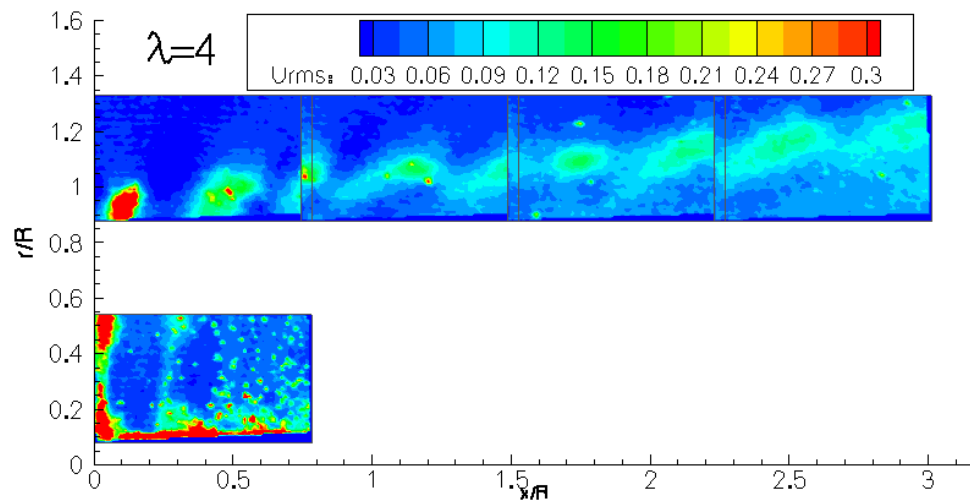
# MEXICO PIV, Phase Ave., W



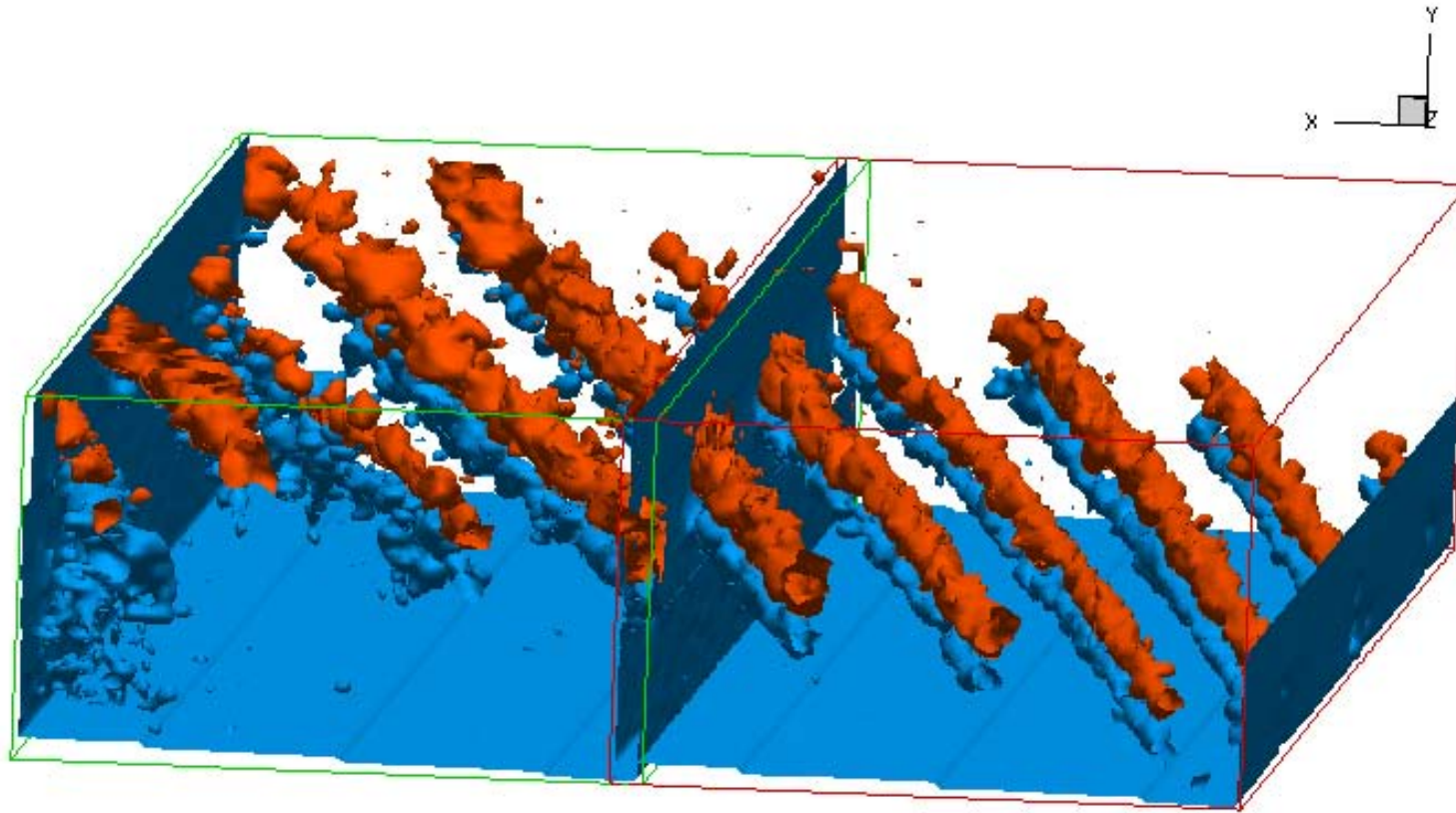
# PIV, Tangential Vel, W-mean TSR 4-7



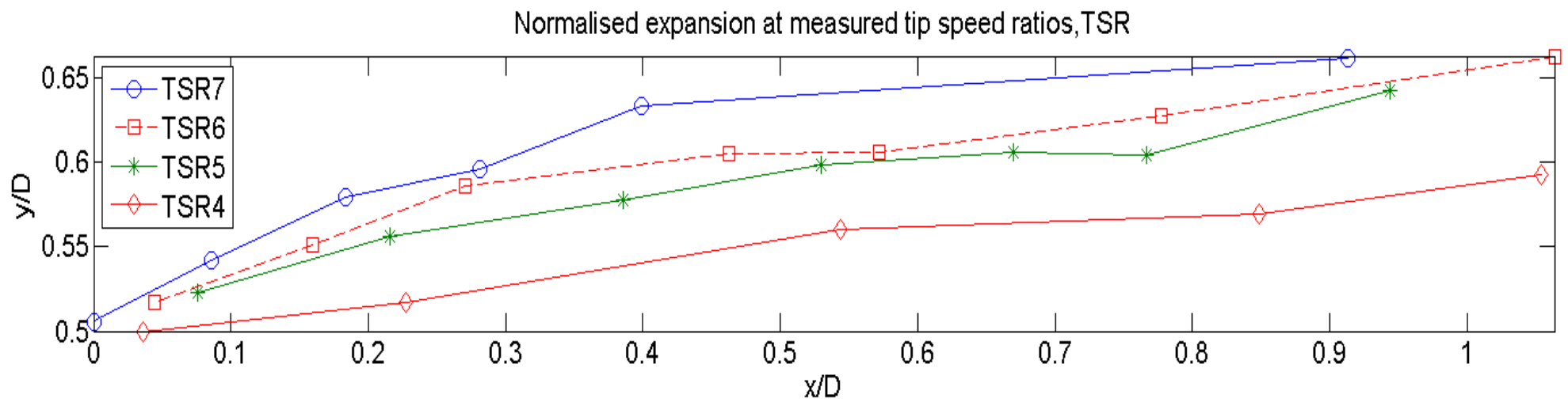
# PIV, Phase ave., U-rms, TSR 4-7



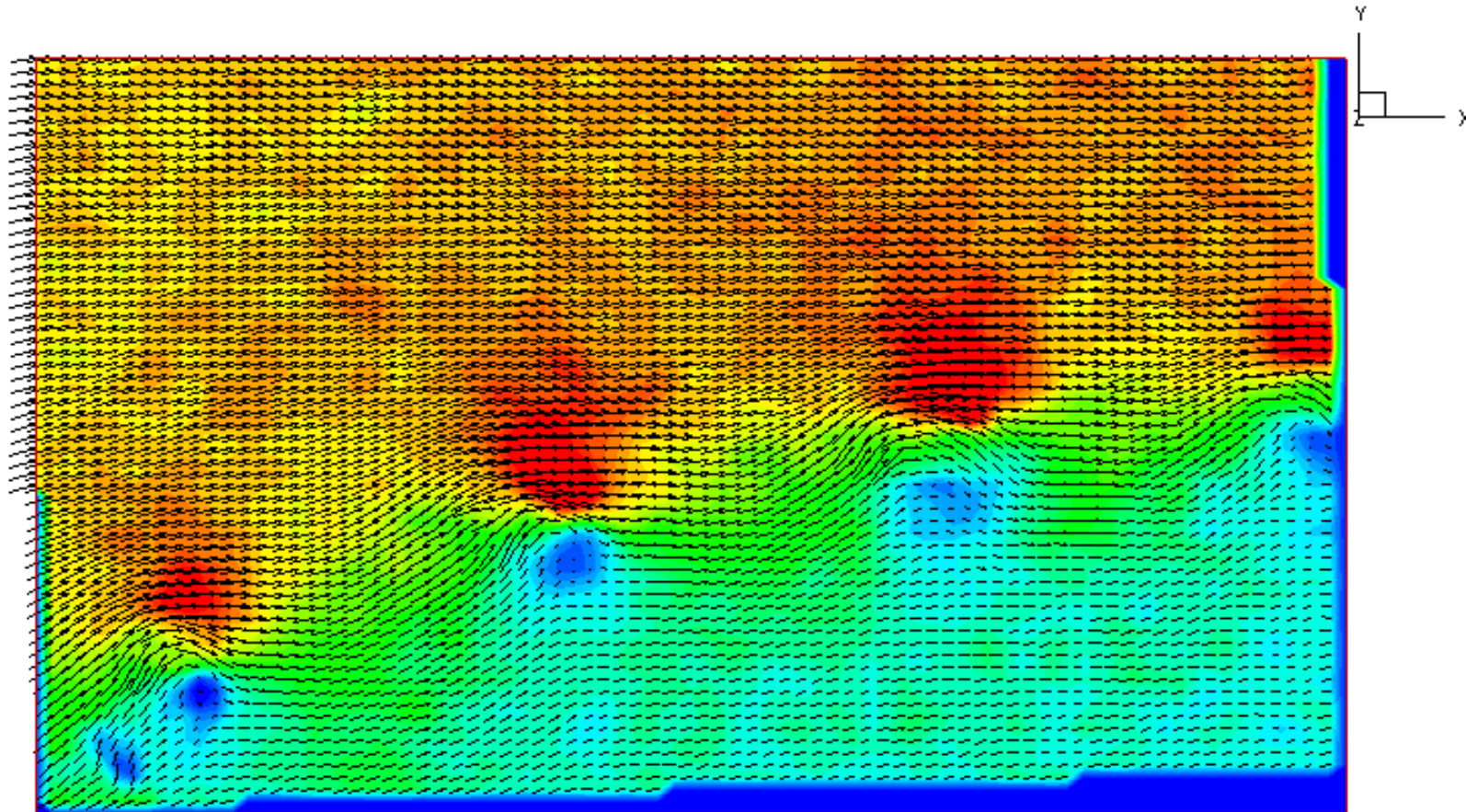
PIV, U-vel, TSR 6 unfolded, 5deg/s



# Expansion of the wake

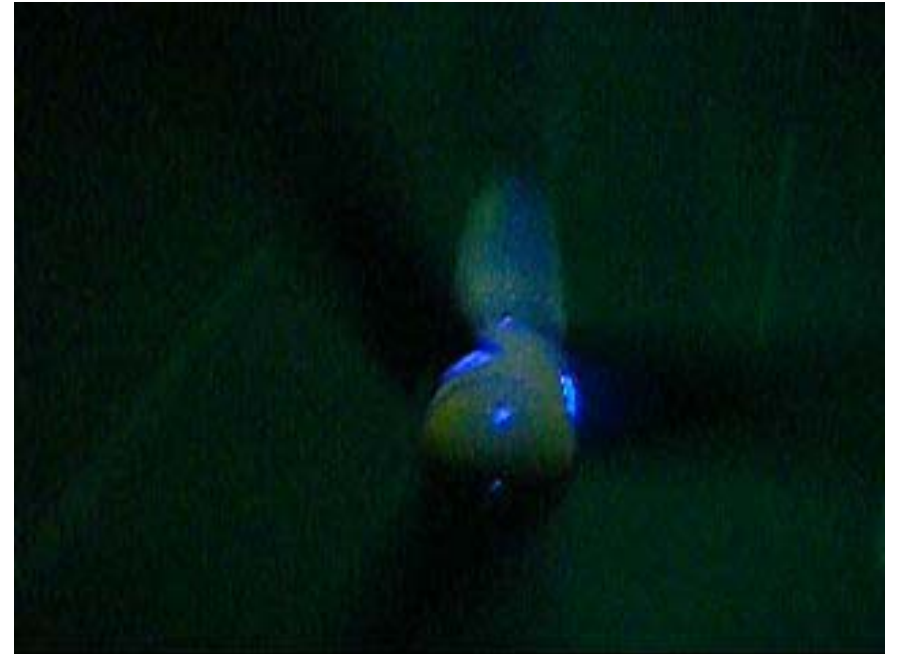
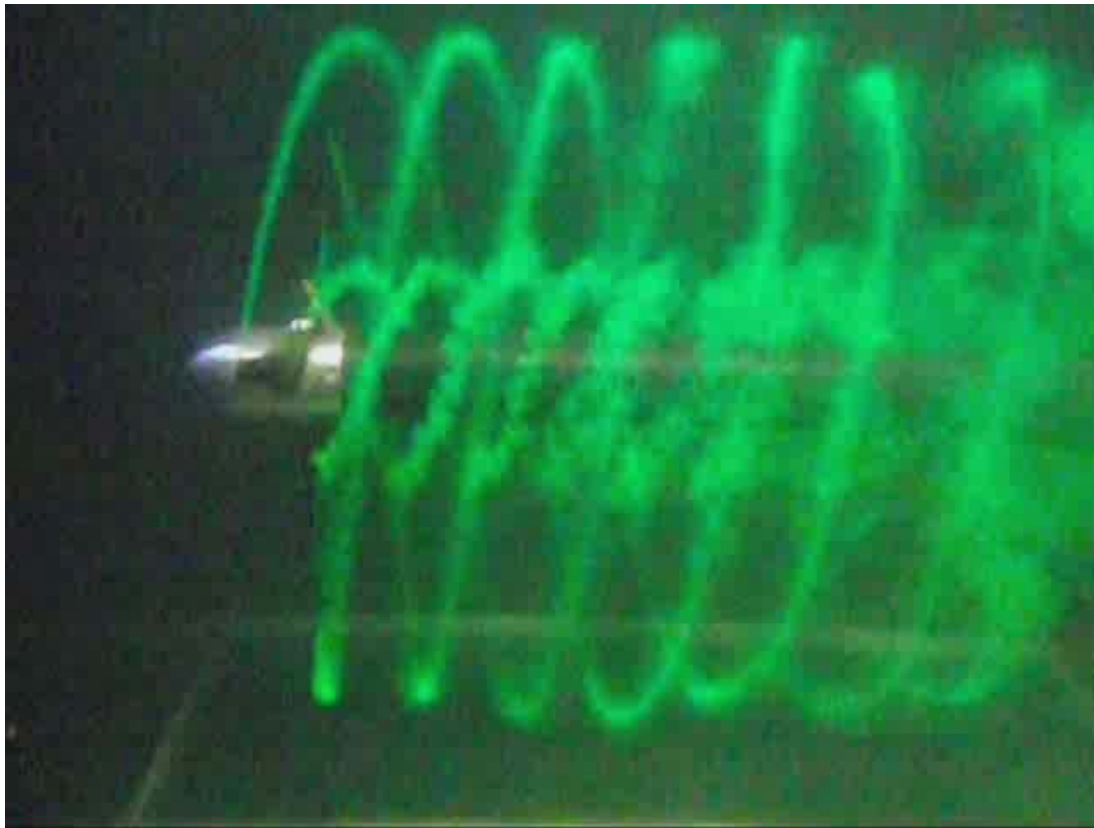


PIV, U-vel, TSR 6 unfolded, 5deg/s

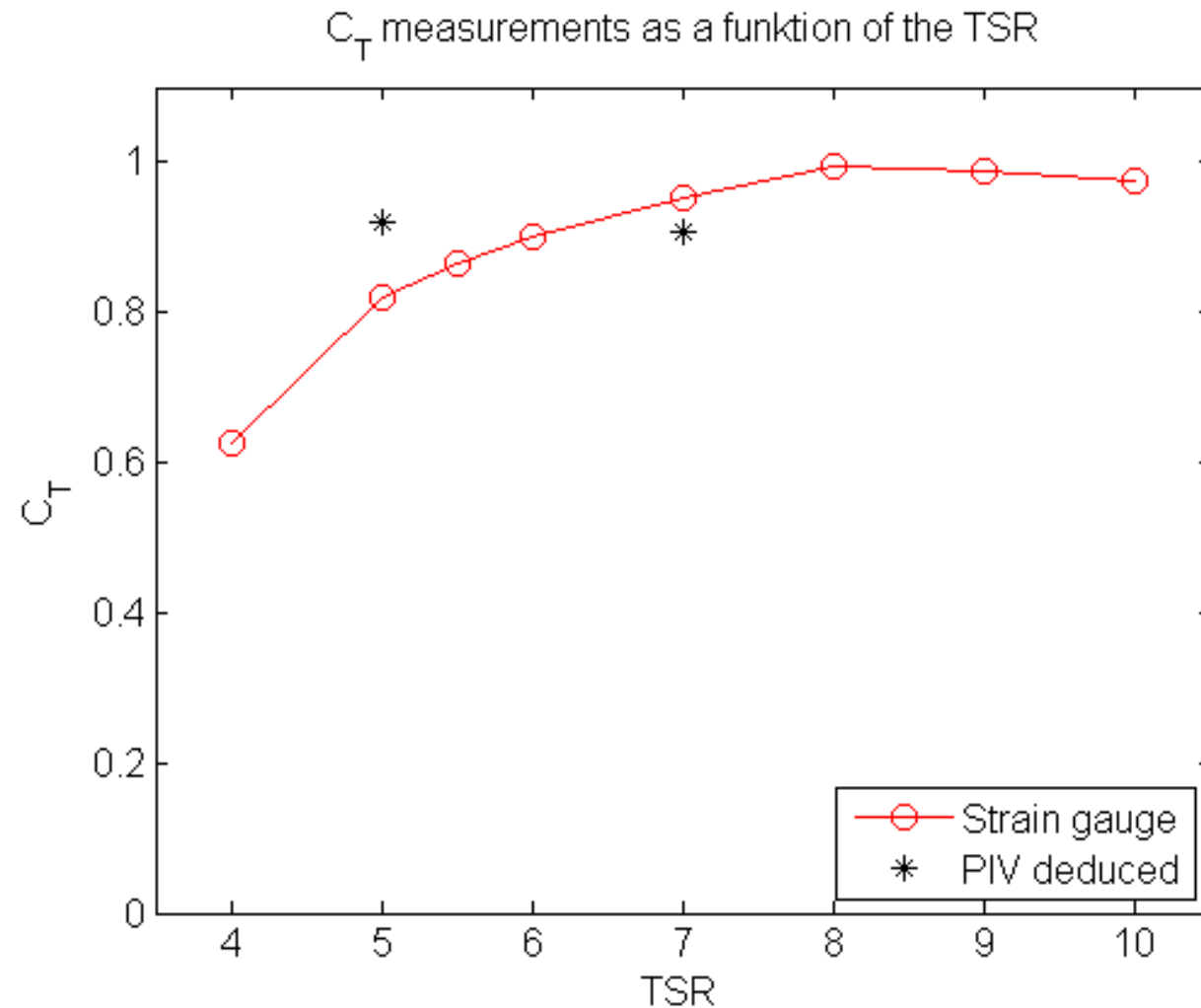




# Rotation of the wake



# Thrust measurements

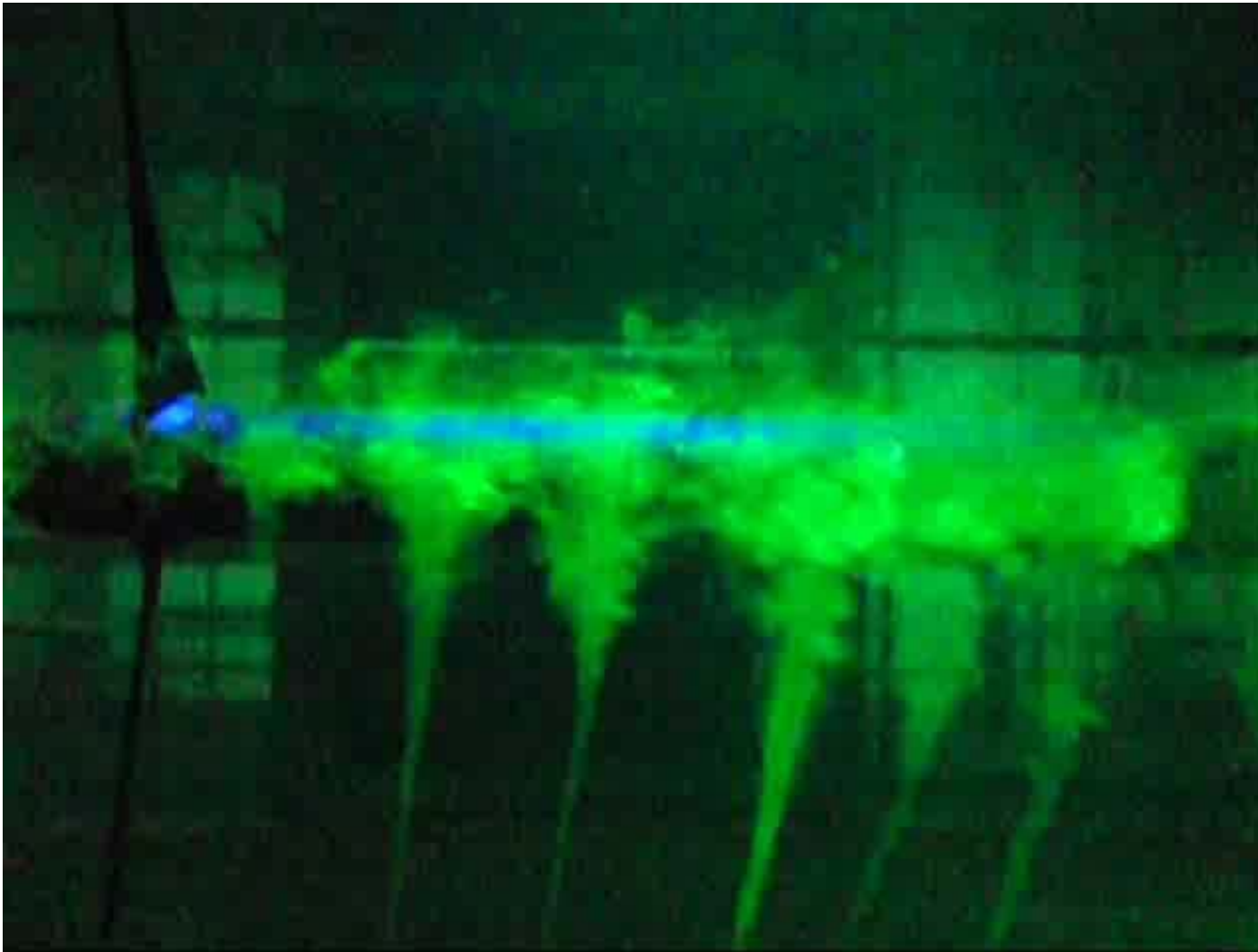
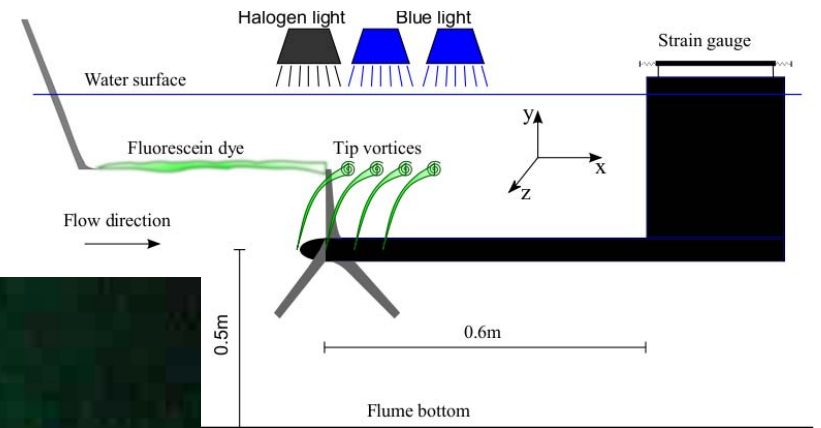


$$T = \dot{m}(V_0 - u_1)$$

$$C_T = \frac{T}{\frac{1}{2}\rho V_0^2 A}$$



# Visualisation with upstream injection



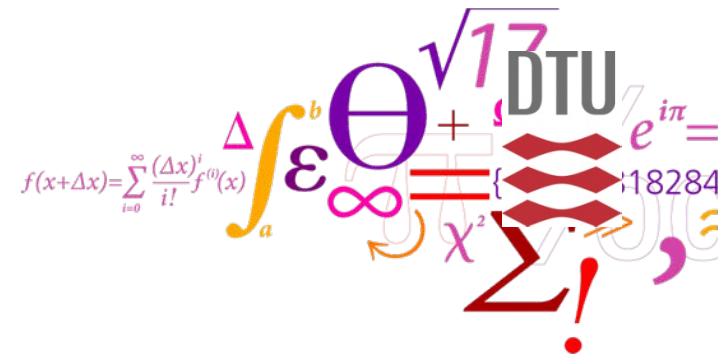
# Summary

- Experimental facilities were found useable
- Visualization captures dynamics of helical structures
- Full mapping of the mean flow in the wake at TSR 4-7
- Wake expansion at different TSR's
- 3D mapping of the wake near the rotor plane
- Strain gauge measurements needs improvment
- Improvement of PIV data
  - More measurements planed 2011
  - Out of plane vel.
  - Upstream measurements
  - Phase triggering

## **6 Simulations of backward swept blade**

# Potential of fatigue and extreme load reductions on swept blades using HAWC2

David Verelst  
RISØ DTU



# UPWIND Turbine: 5MW NREL

Reference turbine by J. Jonkman et al (NREL 2009)

Rating	5 MW
Configuration	Upwind, 3 blades
Control	Variable speed, collective pitch
Drivetrain	High speed, Multiple-stage gearbox
Rotor, Hub diameter	126m, 3m
Cut-in, Rated, Cut-out wind speed	3 m/s, 11.4 m/s, 25 m/s
Cut-in, Rated rotor speed	6.9, 12.1 RPM
Rated tip speed	80 m/s
Overhang, Shaft tilt, Precone	5m, 0 deg, 0 deg

# Previous swept blade studies

- This presentation is based on a public Risø report:  
Load Consequences when Sweeping Blades – A Case Study of a 5 MW Pitch Controlled Wind Turbine, D.R.S. Verelst, T.J. Larsen, 2010
- Sandia – Night & Karver STAR blade
  - Objective: increase energy consumption on Zond 750 turbine for low wind speed sites (average wind speed around 5.8 m/s)
  - Zond 750 is a variable speed pitch controlled machine
  - Larger swept blade but load level maintained (blade root bending moments)
  - Increased energy capture in below rated conditions.  
Full scale tests shows energy increase of 10-12%
  - Thomas Ashwill et al., *Development of the Swept Twist Adaptive Rotor (STAR) Blade*, AIAA-2010-1582).

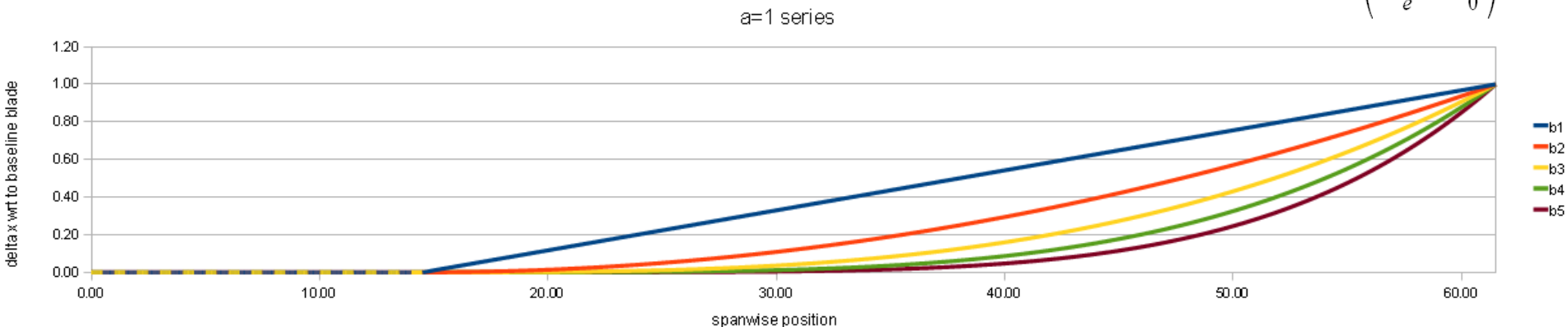
# Why sweep?

- Sweep adds a geometric coupling between bending and twist deformations of the blade
- Increase blade size while maintaining blade root bending moment load levels. As a result, increased energy capture due to larger rotor
- For backward sweep, pitch to feather decreases angle of attack variations over one rotor revolution (cfr. turbulence, shear): passive cyclic pitch
- Preliminary results indicate decreased yawing moments (work in progress for EWECC 2011)

# Methodology

- 5 sweep curve exponents combined with 24 tip offsets = 120 + 1 (ref.) blade variants
- 2 different controller implementations (Risø and NREL)
- Steady wind speeds (4..26 m/s, 1m/s steps)
- Turbulent wind speeds (4..26 m/s, 2m/s steps, 10 min series) same seed number, TI=0.18
- Equivalent loads for standard wind speed distribution and 20 years

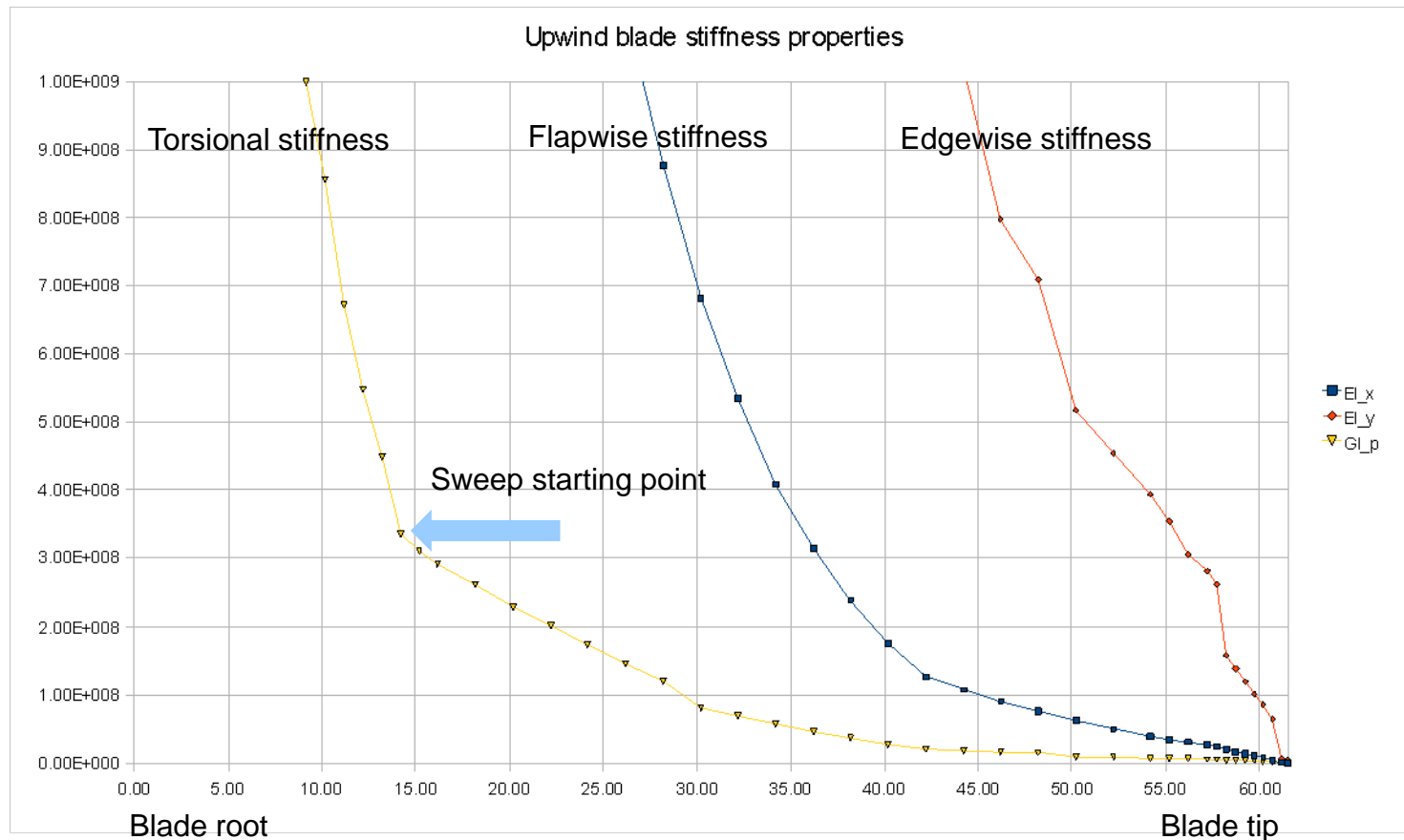
$$x = a \left( \frac{z - z_0}{z_e - z_0} \right)^b$$





# Blade structural characteristics

Start sweep curve at 14.35m (blade radial pos)



# Equivalent loads – blade flap

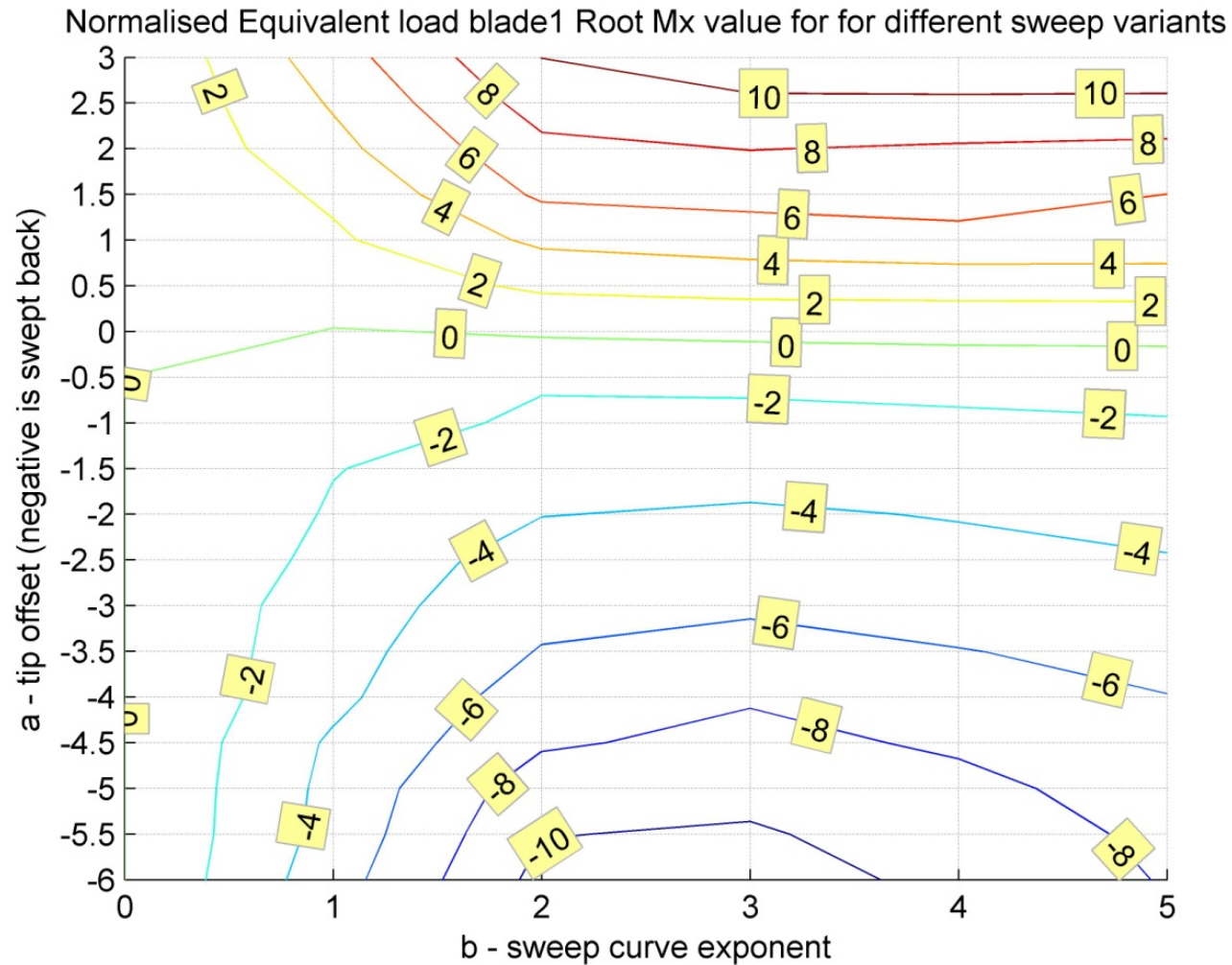
Forward sweep



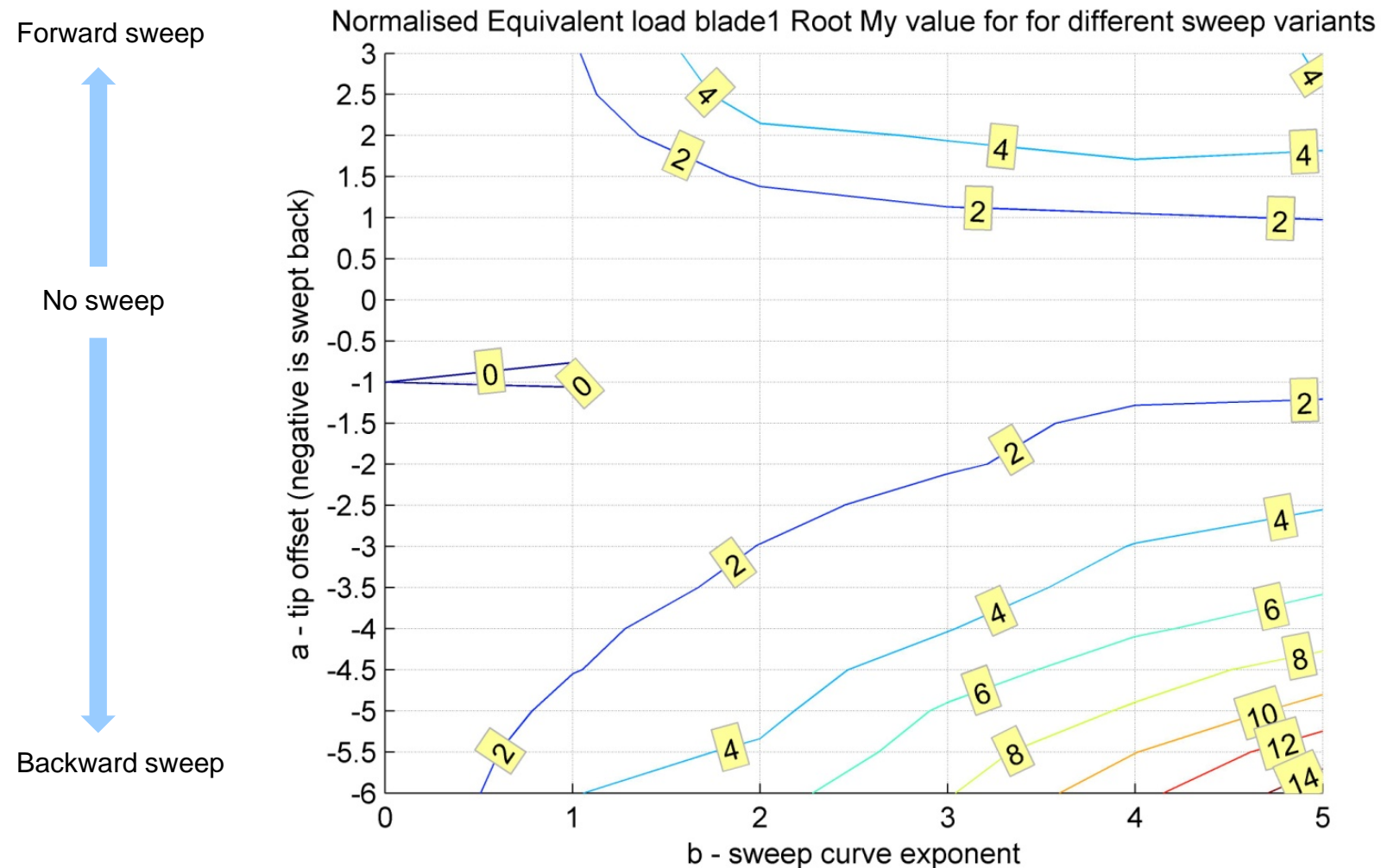
No sweep



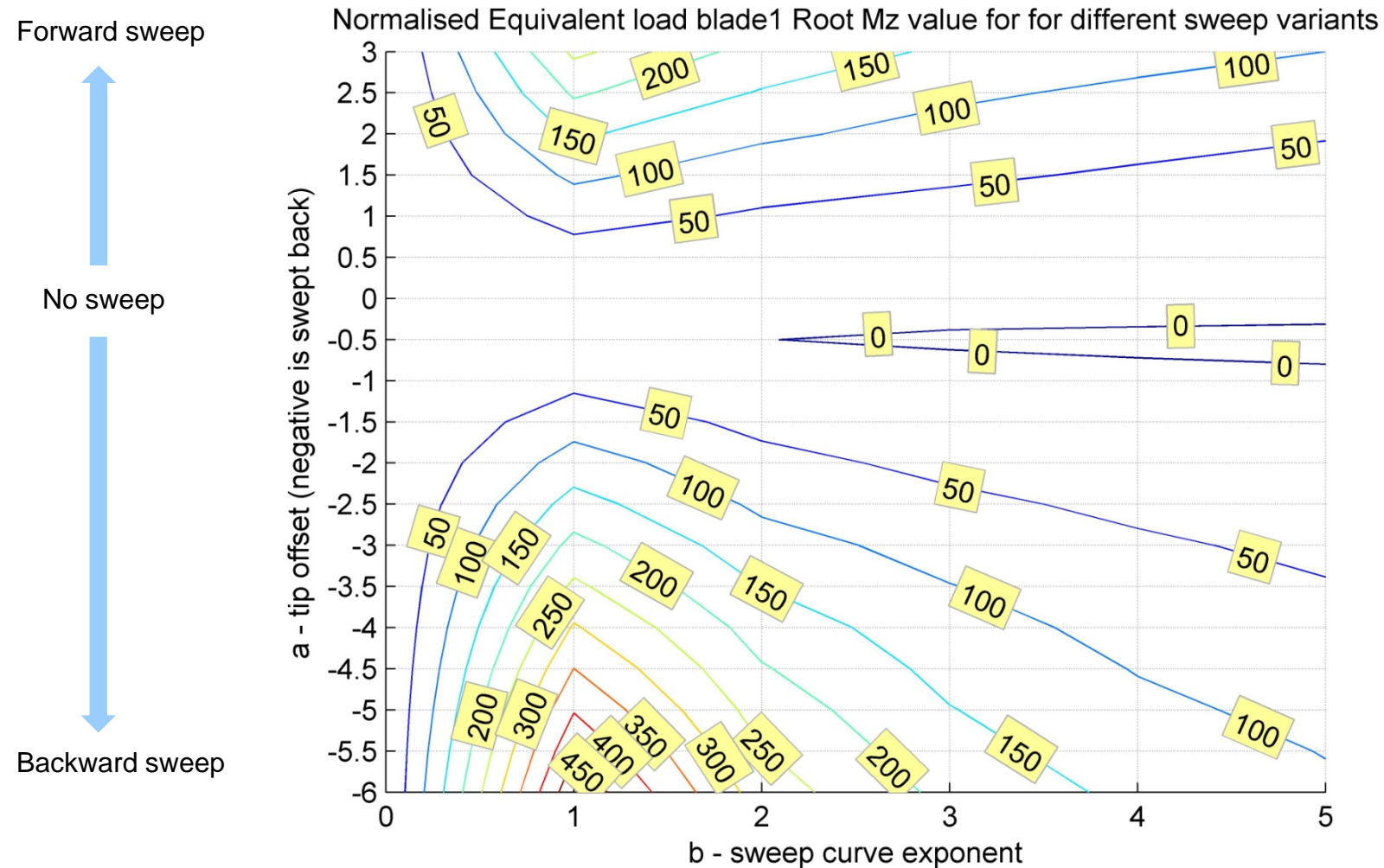
Backward sweep



# Equivalent loads – blade edge



# Equivalent loads – blade torsion

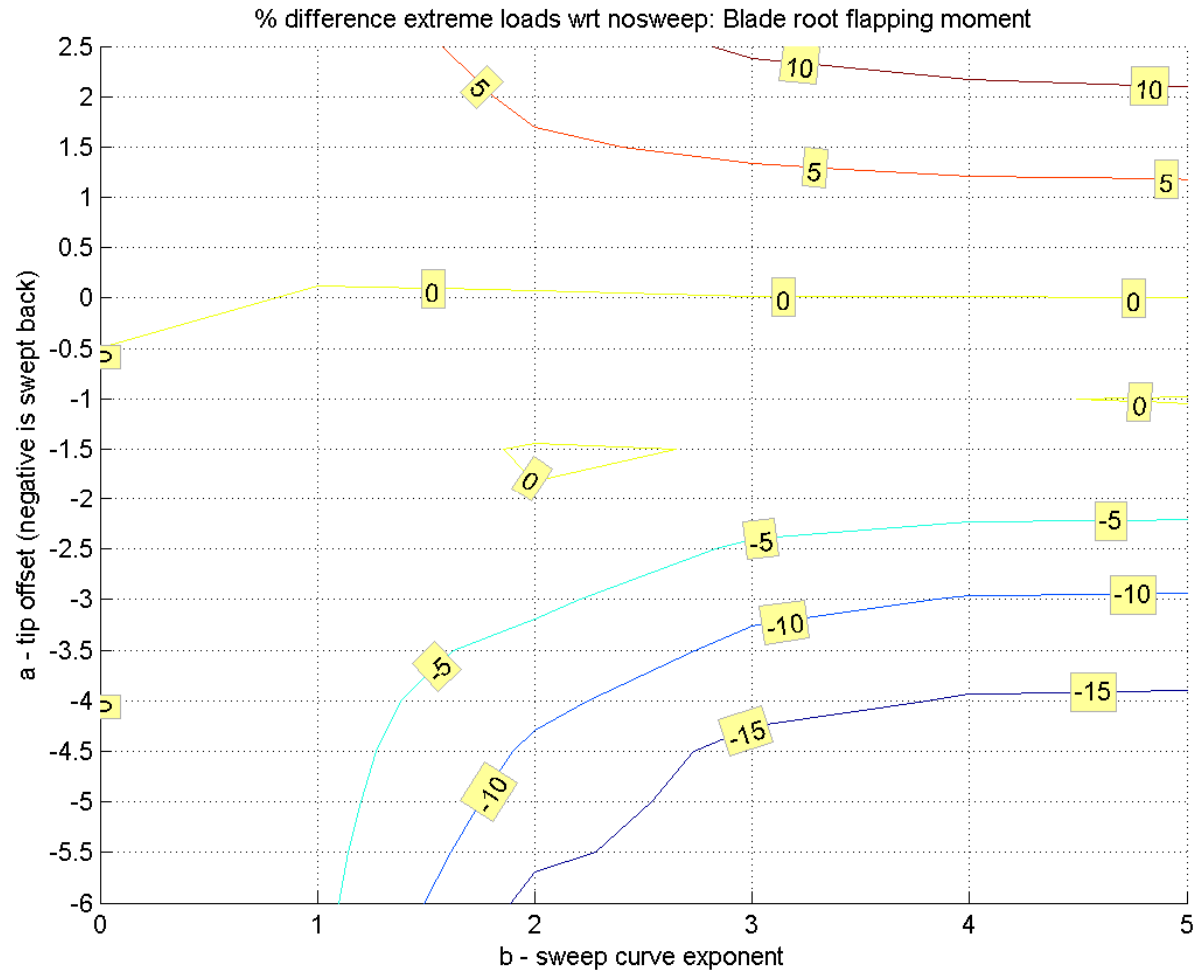


# Extreme loads – blade flap

Forward sweep

No sweep

Backward sweep

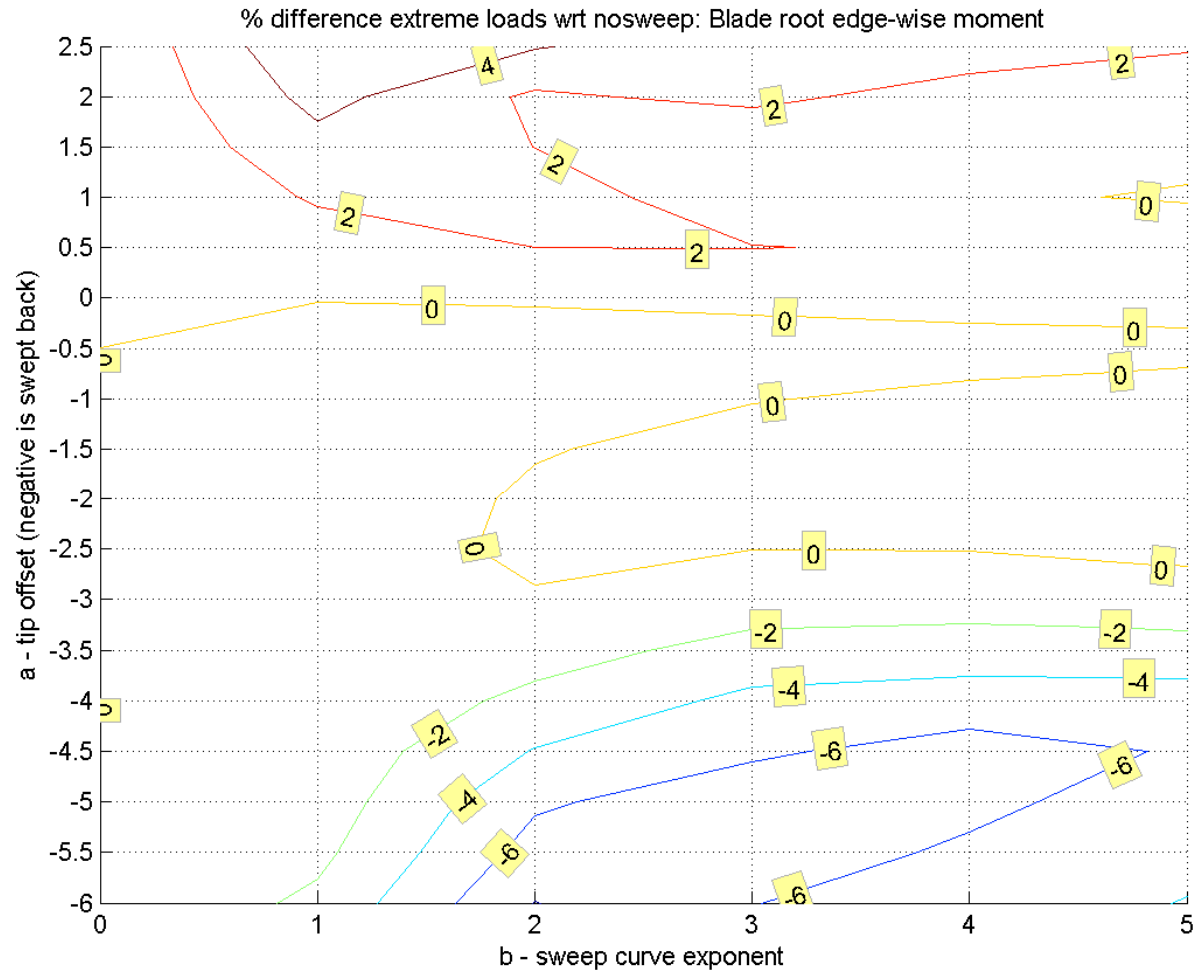


# Extreme loads – blade edge

Forward sweep

No sweep

Backward sweep

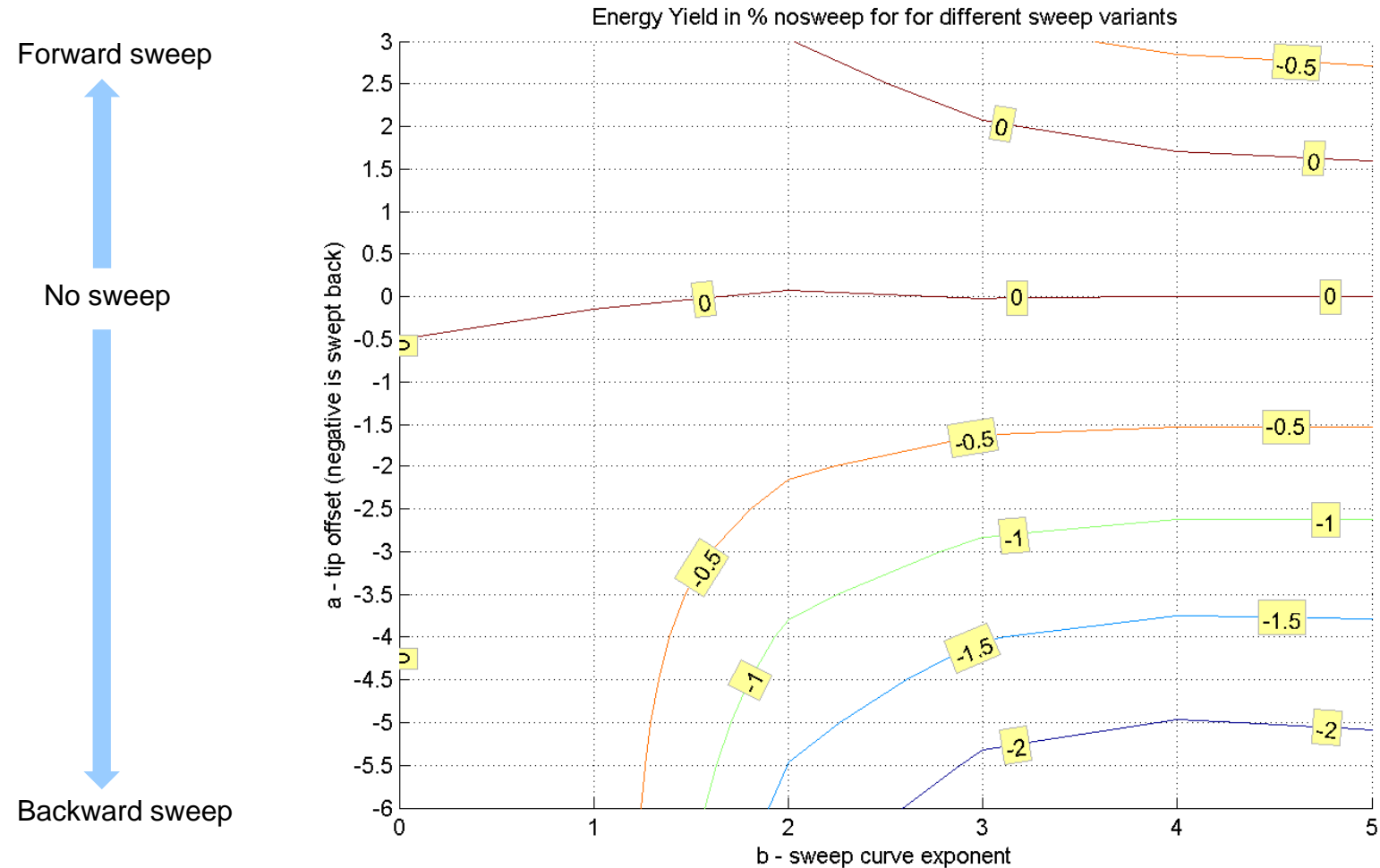


# Overview of Approximate Load Consequences

Load consequences backward sweep wrt no-sweep					Risø	
Controller	Risø		NREL		wrt NREL	
Loads	fat.	ext.	fat.	ext.	fat.	ext.
Blade root flap	-8 %	-15 %	-10 %	-15 %	0 %	+2 %
Blade root edge	+7 %	+6 %	+3 %	-4 %	+3 %	+12 %
Blade root torsion	+50 %	+50 %	+50 %	+50 %	+1 %	+2 %
Tower base FA	-3 %	-8 %	-3 %	-4 %	na	-3 %
Tower base SS	+2 %	-12 %	+4 %	-6 %	na	-10 %
Tow. base torsion	-10 %	-15 %	-8 %	-15 %	na	-2 %
Shaft-end tilt	-10 %	-2 %	10 %	-10 %	na	+20 %
Shaft-end yaw	-15 %	-20 %	-14 %	-20 %	na	-3 %
Shaft-end torsion	+ 1.5 %	0.5 %	+ 1.0 %	-2.5 %	na	+1.5 %

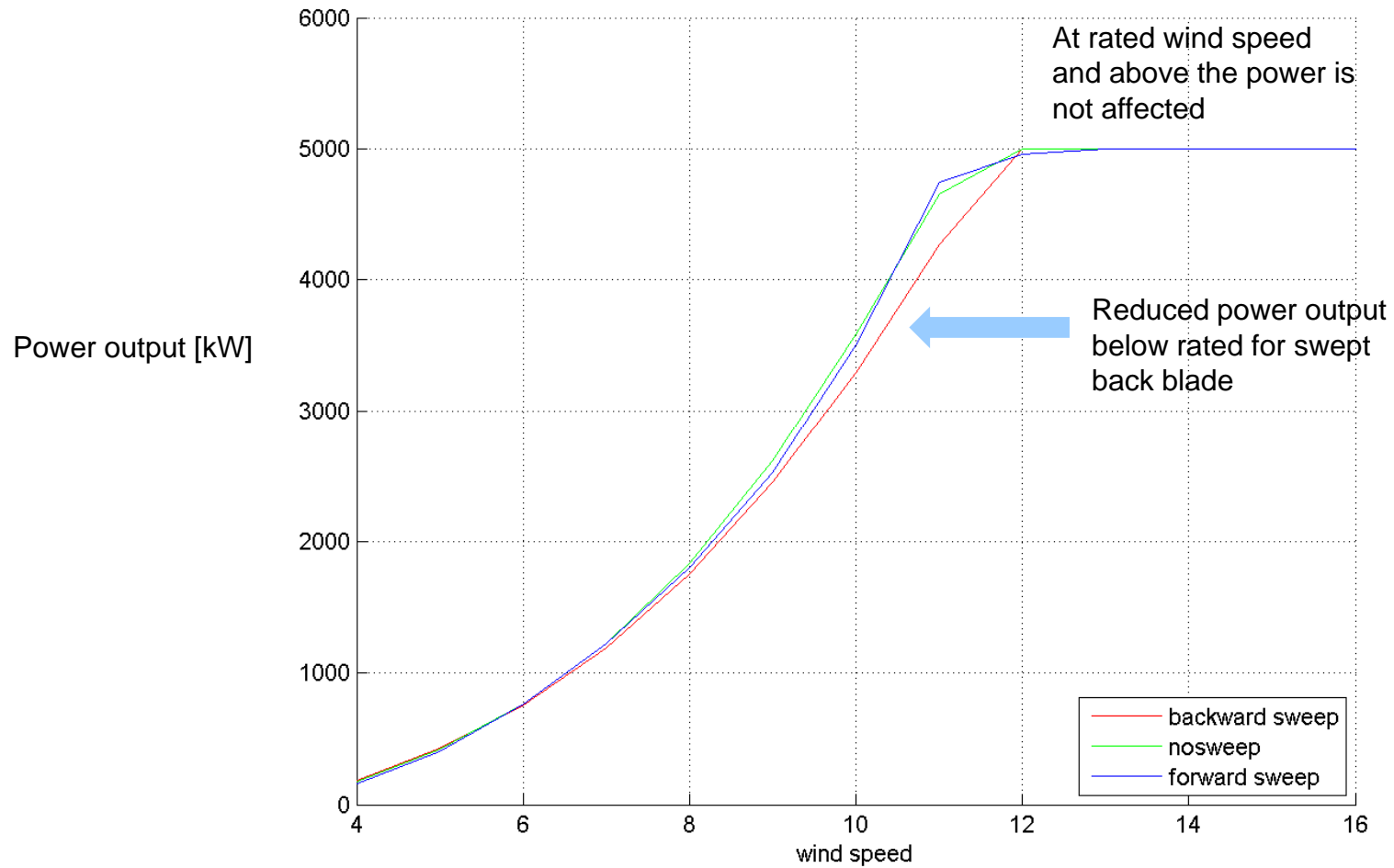
*Table 3. Overview of approximate load consequences for a pitched controlled, extreme swept wind turbine*

# Energy Yield – steady wind

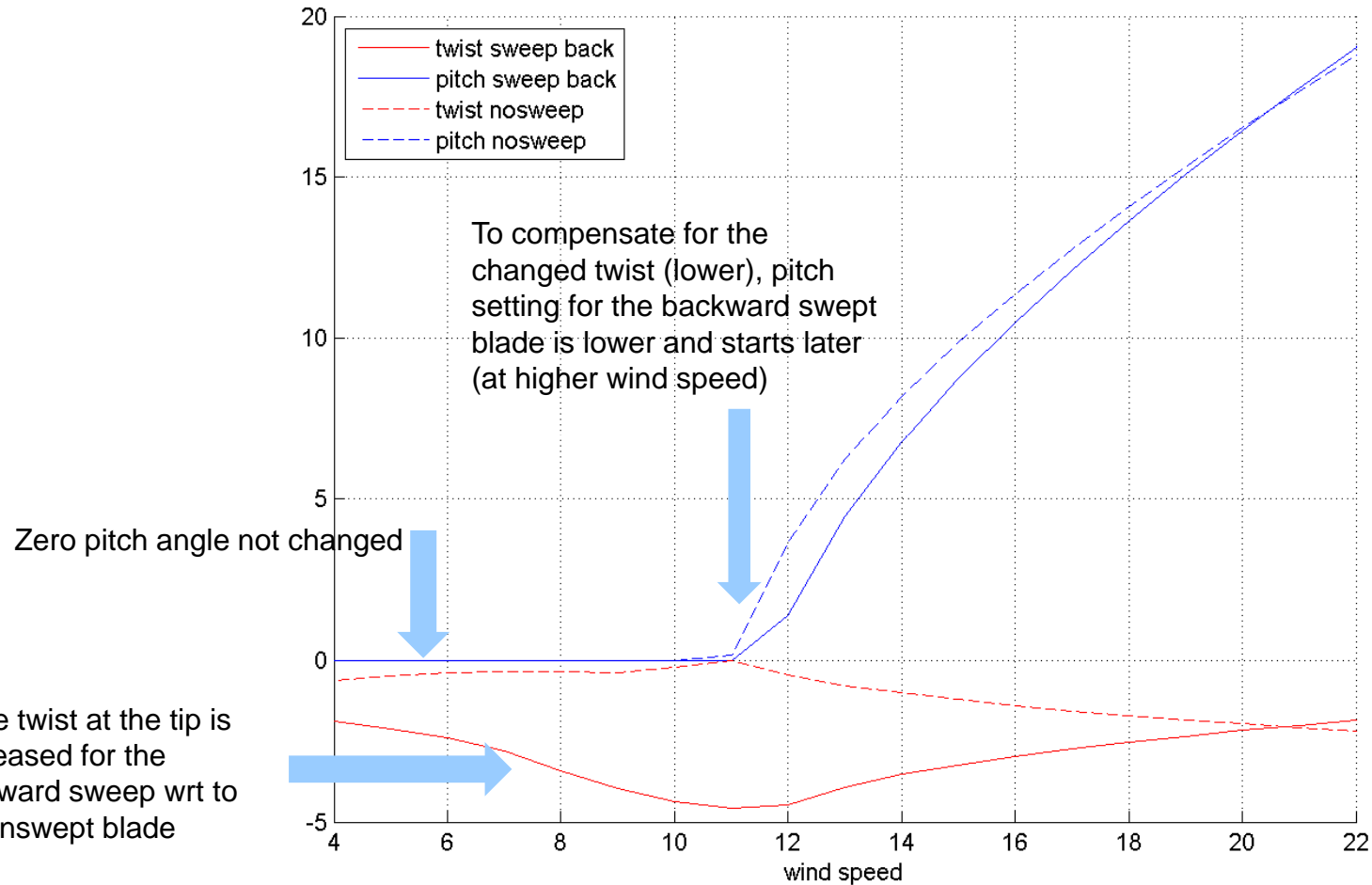




# Power Curve



# Tip Twist and Pitch Angle



# Conclusions

- Forward sweep (pitch to stall):
  - Edge- and flap-wise blade loading increases
  - Pitch control induced instabilities
- Backward sweep (pitch to feather):
  - Flap-wise blade loading decreased, edge-wise increased
- Blade root torsional moment increased significantly
- Decreased tower and shaft loadings
- Sensitive for sweep shape (exponent) and controller
- Passive load shedding mechanism is expected to be relevant for even larger wind turbines

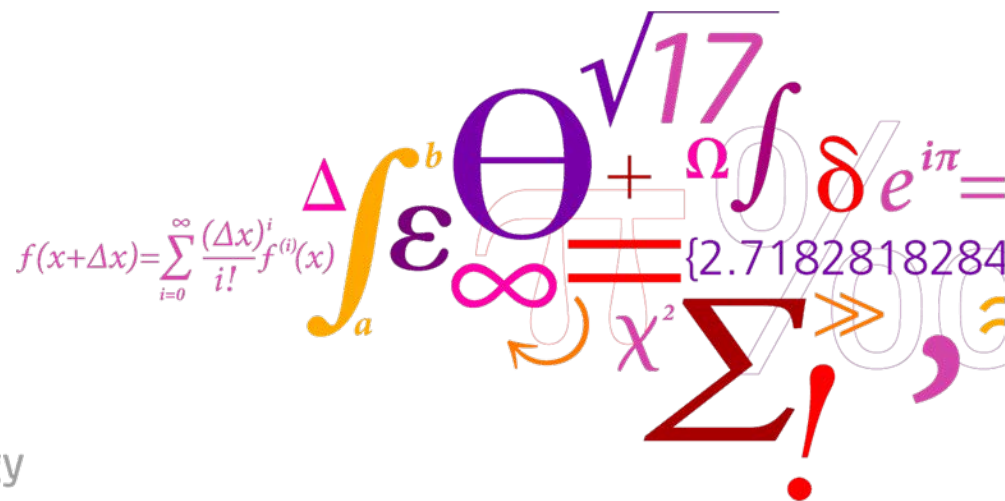
## **7 Eigenvalue analysis of backward swept blades**

# Aeroelastic modal analysis of backward swept blades using HAWCStab2

Morten Hartvig Hansen

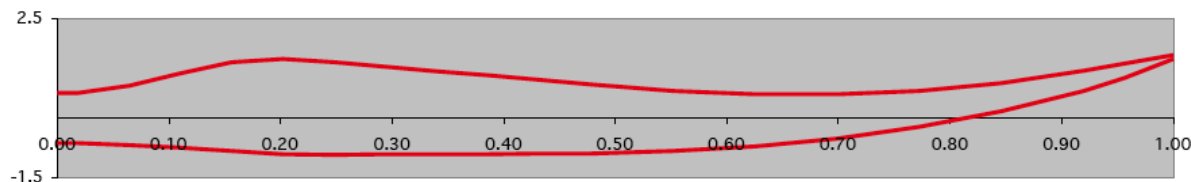
Old findings: - Lower flapwise loads for backward sweep

New findings: - Lower flapwise damping but higher flapwise stiffness  
- Flutter limit decreases



# Field test at Sandia Nat. Lab.

- Ashwil *et al.*, "Development of the swept twist adaptive rotor (STAR) blade", In Proc. of the 48th AIAA Aerospace Sciences Meeting, 2010:
  - 26.1 m STAR prototype blade can increase the annual energy capture by 10-12% compared to a baseline 23.5 m blade without increasing the blade root bending moments



# What is HAWCStab2?

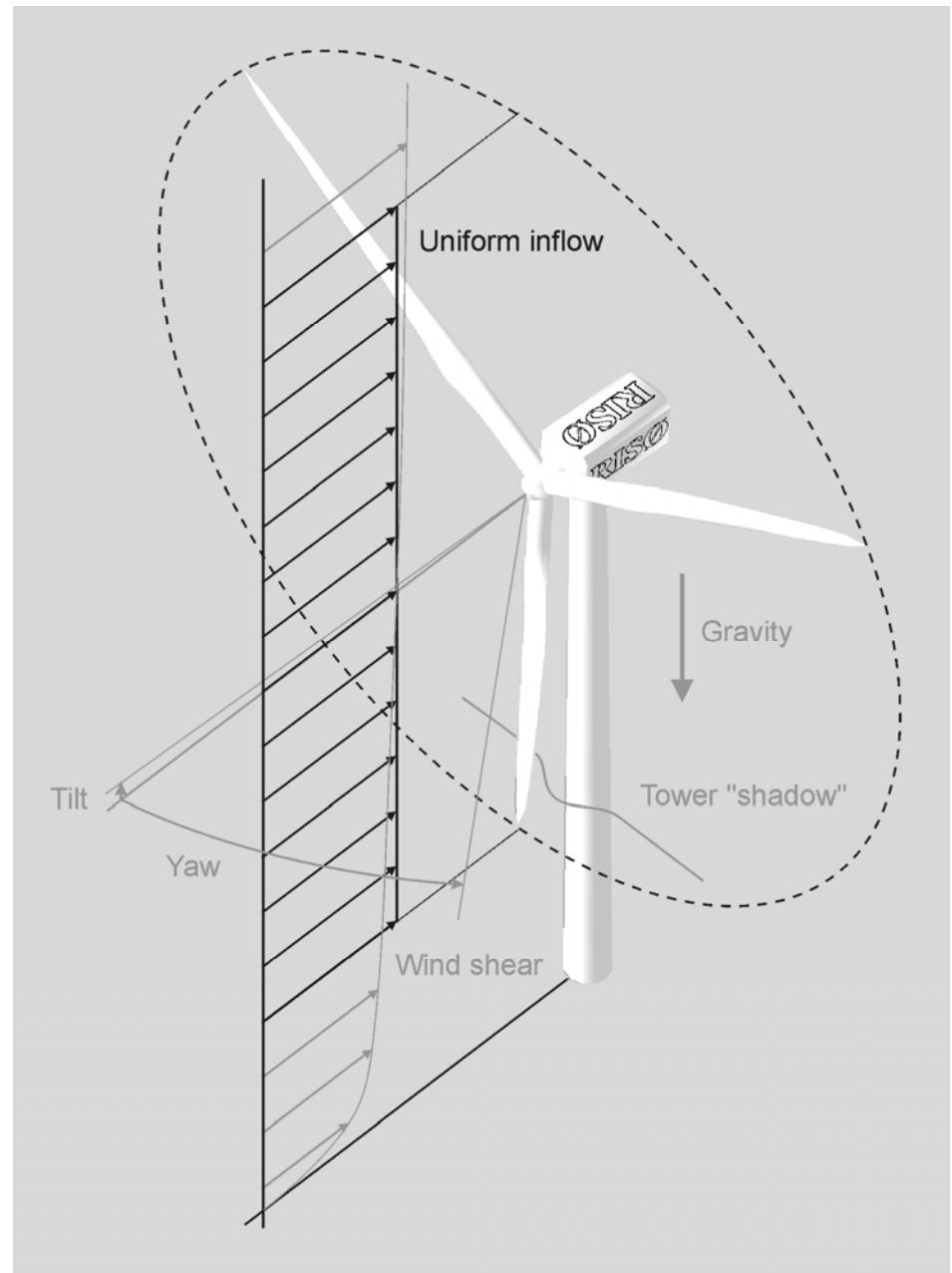
Linear aeroelastic model for eigenvalue and frequency domain analysis of wind turbines and blades

Nonlinear kinematics based on co-rotational elements with possibility of bearings e.g. generator and pitch.

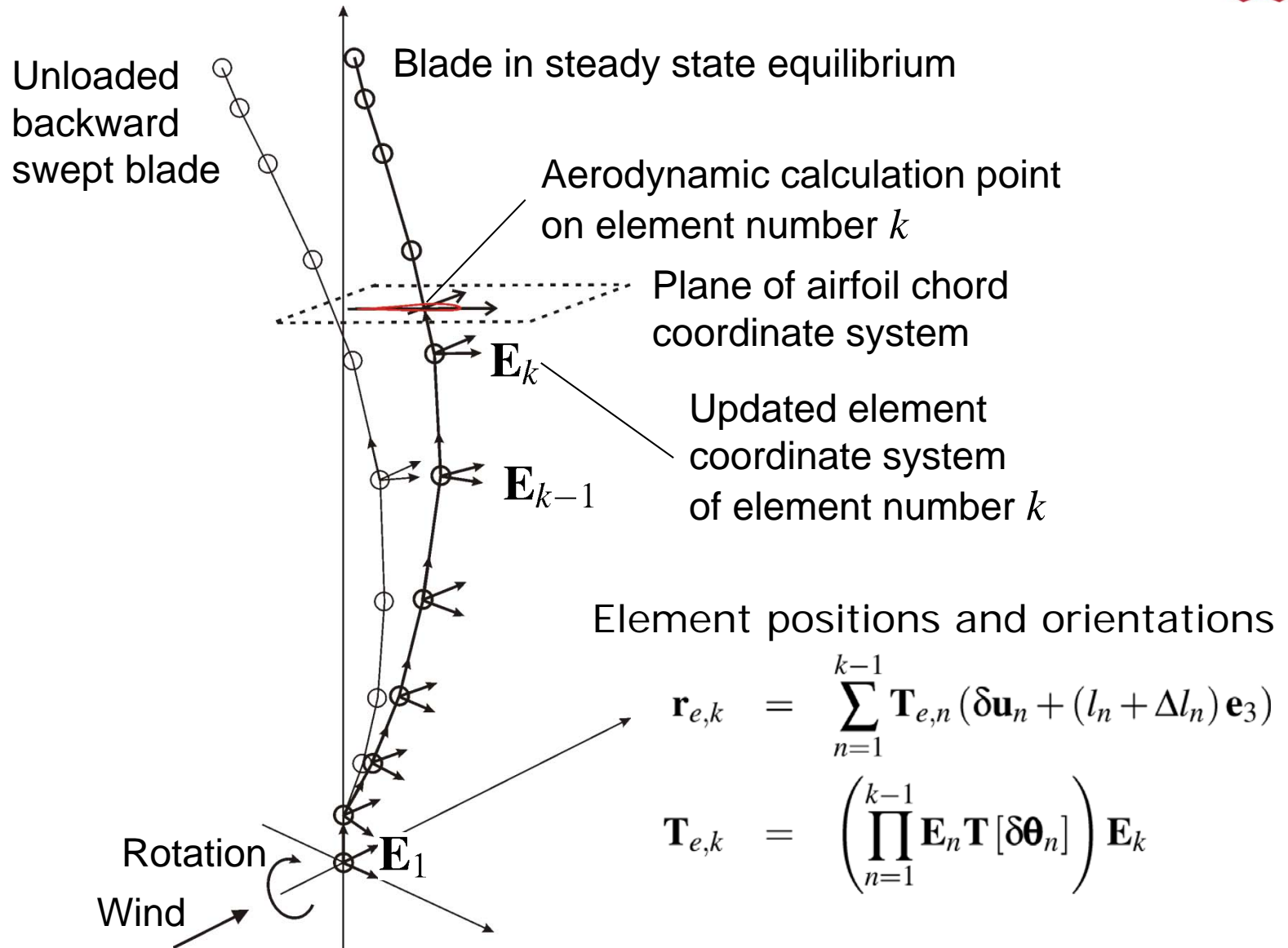
Uniform inflow to give a stationary steady state.

Analytical linearization about the stationary steady state.

Unsteady aerodynamics based on Leishman-Beddoes. A two state (per calc. point) model of dynamic inflow will soon be included.

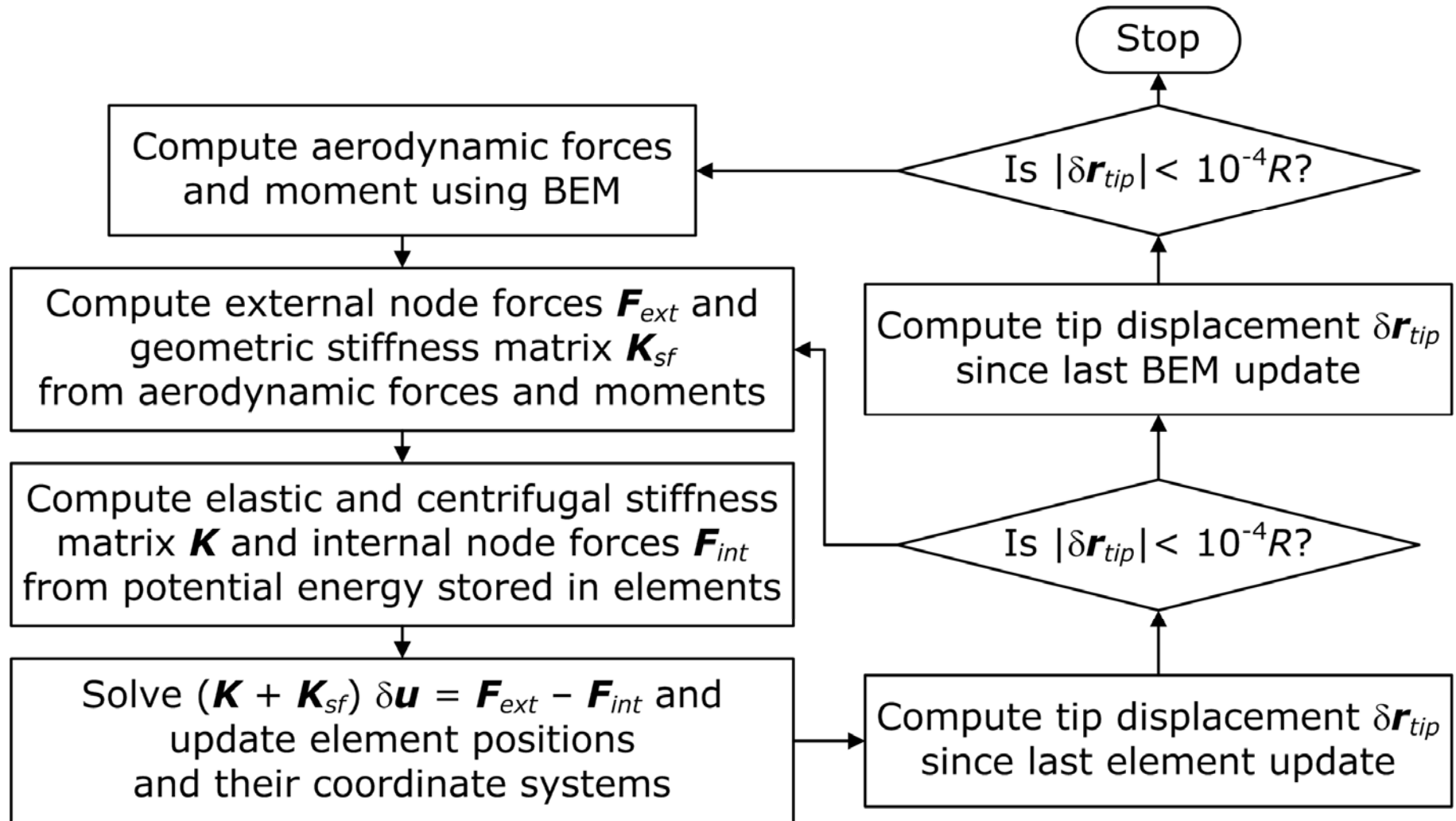


# Nonlinear kinematic formulation for blade





# Nonlinear steady state



# Linear equations for small vibrations about the nonlinear steady state

$$\begin{aligned}
 & \text{Structural mass} \quad \text{Structural damping} \quad \text{Gyroscopic forces} \quad \text{Aerodynamic damping} \quad \text{Elastic stiffness} \quad \text{Geometric stiffness of steady state force} \quad \text{Aerodynamic stiffness} \quad \text{Coupling to aerodynamic states} \\
 & \mathbf{M}\ddot{\mathbf{x}}_s + (\mathbf{C} + \mathbf{G} + \mathbf{C}_a)\dot{\mathbf{x}}_s + (\mathbf{K} + \mathbf{K}_{sf} + \mathbf{K}_a)\mathbf{x}_s + \mathbf{A}_f\mathbf{x}_a = \mathbf{F}_s \\
 & \quad \quad \quad \text{Time lags matrix} \quad \text{Coupling to structural states} \\
 & \quad \quad \quad \dot{\mathbf{x}}_a + \mathbf{A}_d\mathbf{x}_a + \mathbf{C}_{sa}\dot{\mathbf{x}}_s + \mathbf{K}_{sa}\mathbf{x}_s = \mathbf{F}_a
 \end{aligned}$$

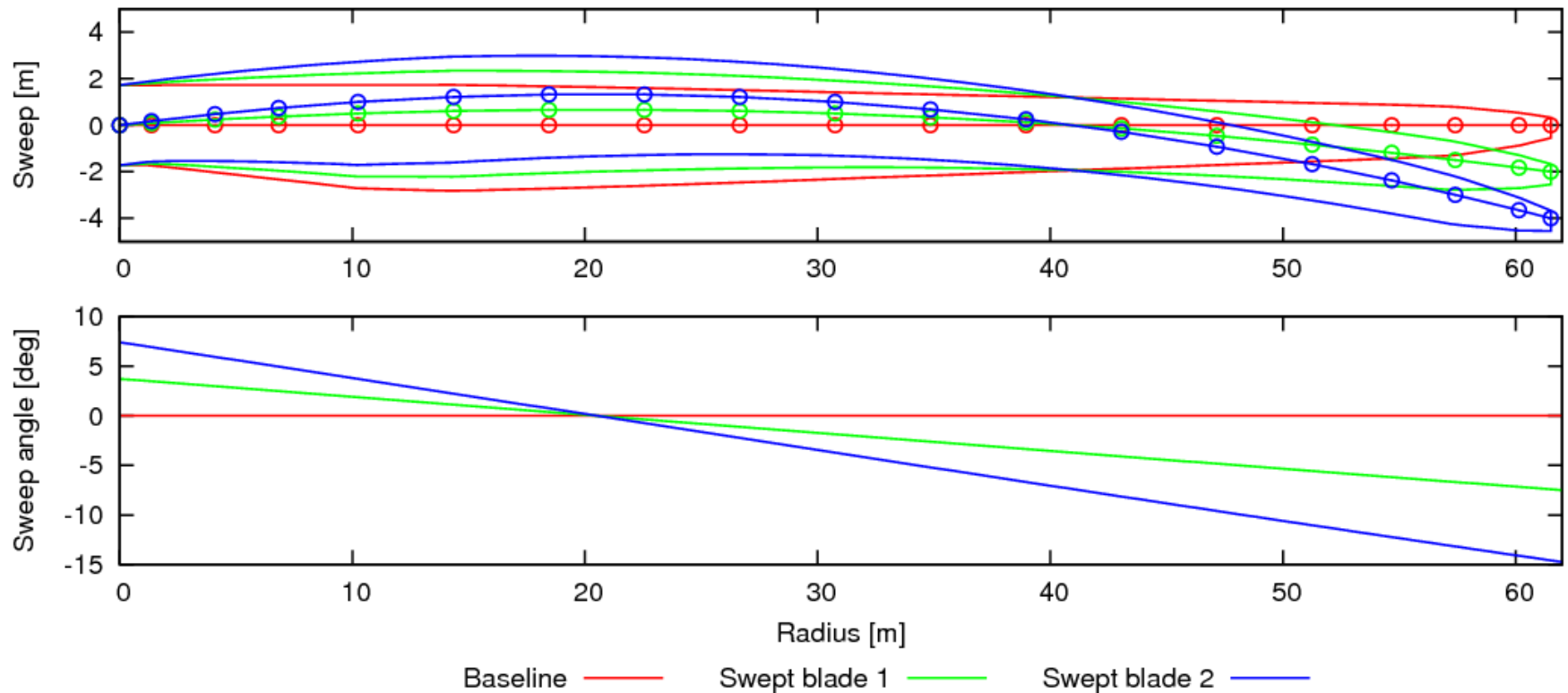
$\mathbf{x}_s$  = elastic (and bearing) degrees of freedom

$\mathbf{x}_a$  = aerodynamic state variables

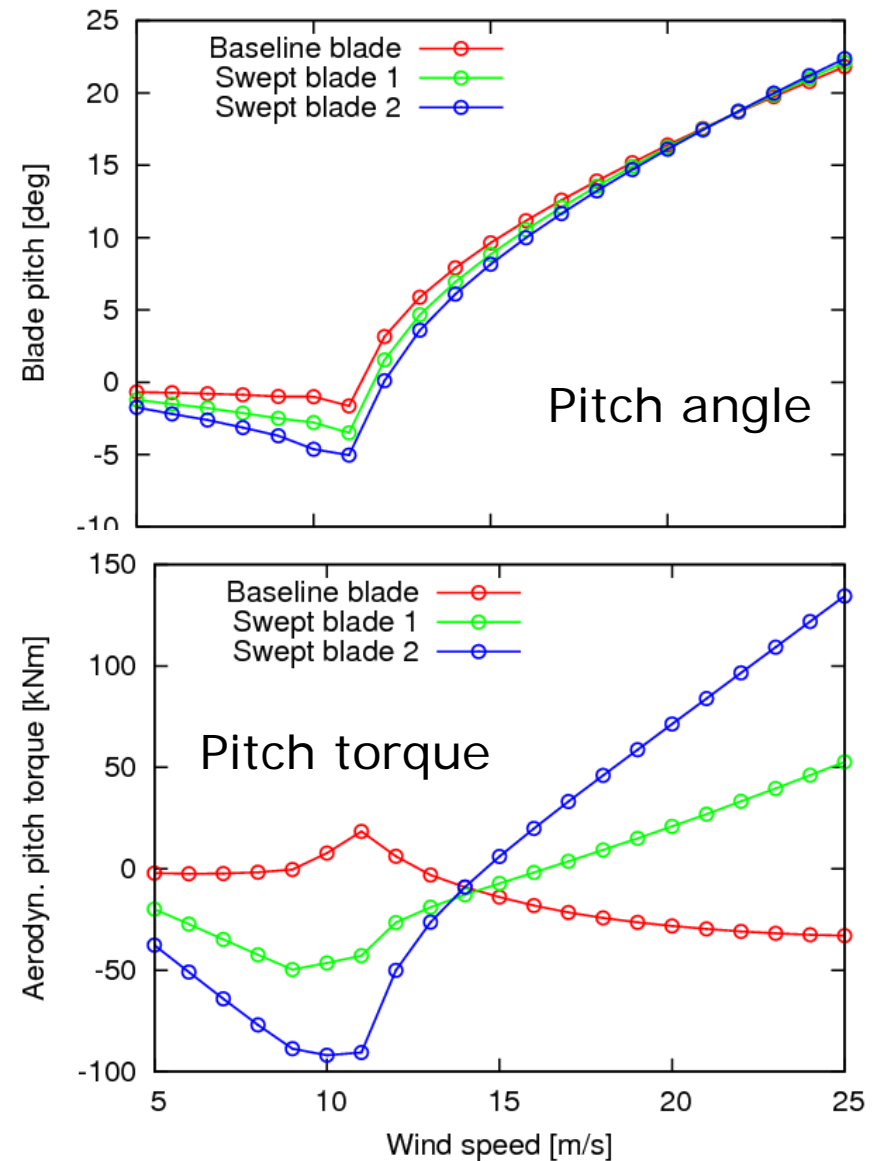
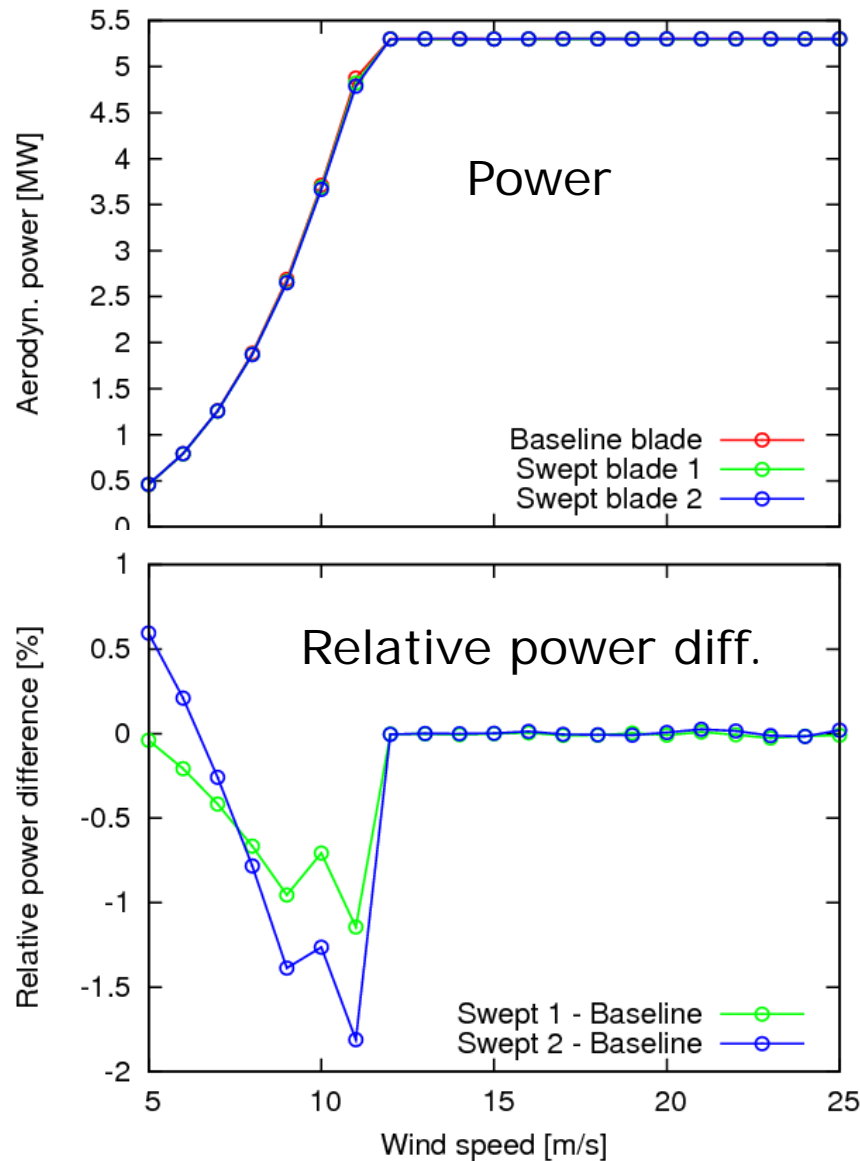
$\mathbf{F}_s, \mathbf{F}_a$  = forces due to actuators and wind disturbance

# Backward swept blades

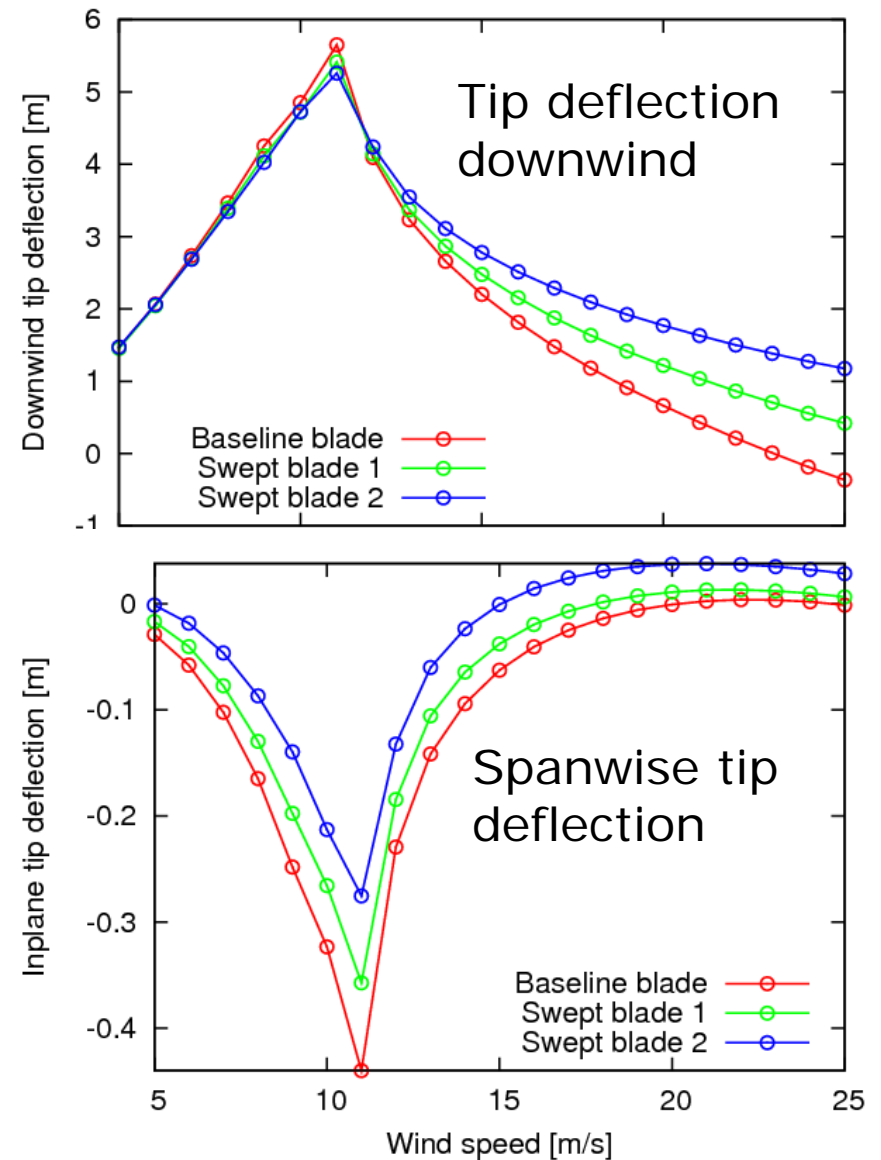
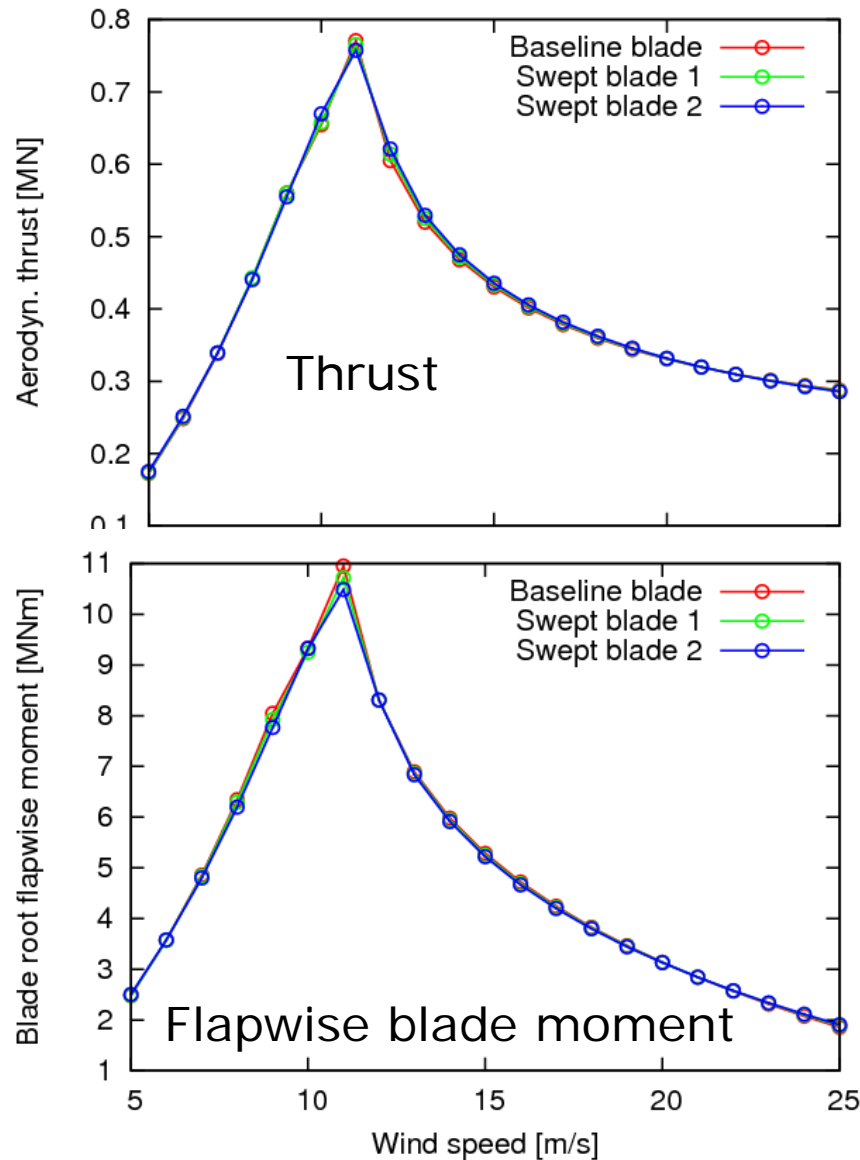
## Baseline – NREL 61.5m with CG at EA



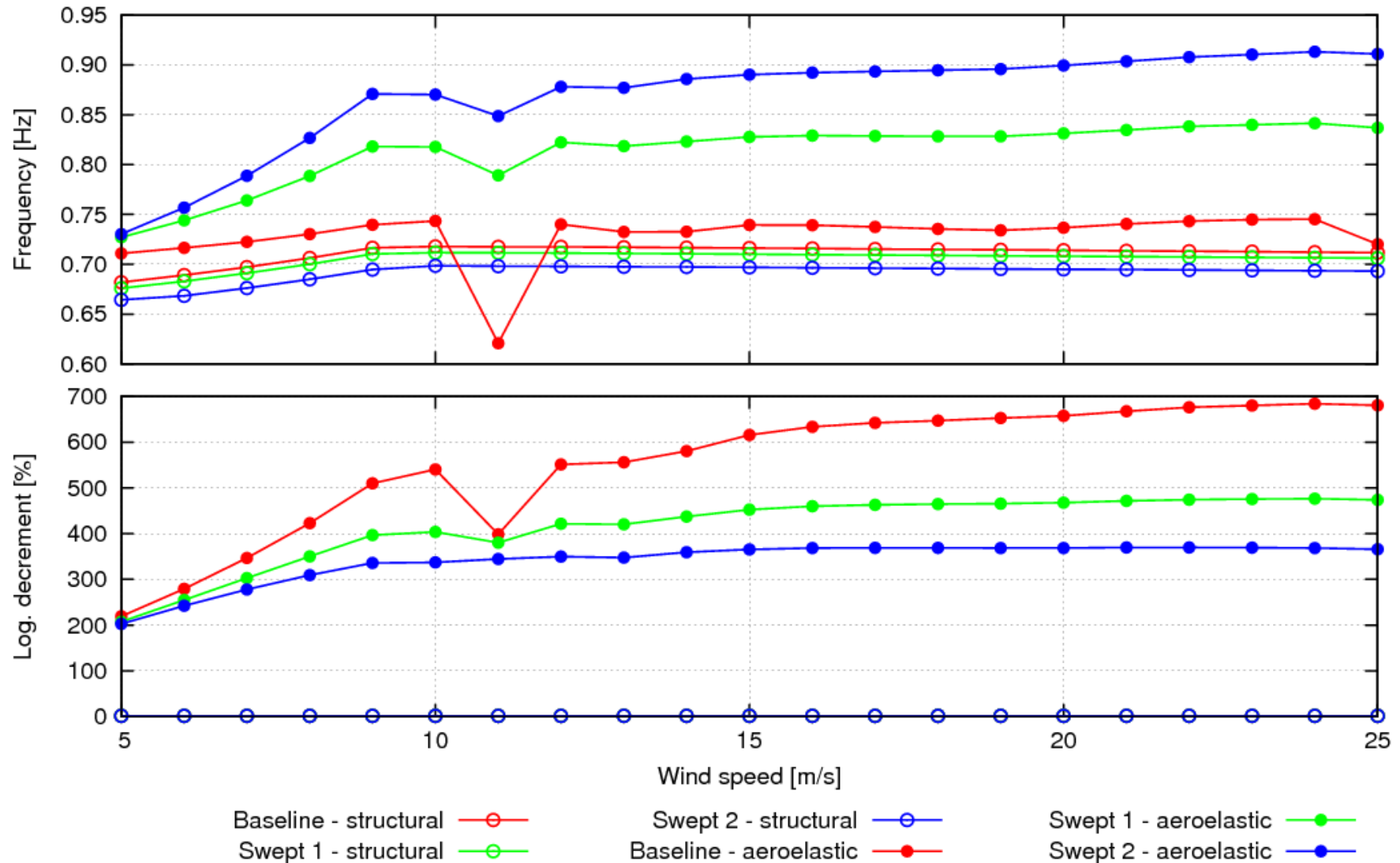
# Steady state power and pitch angle & torque



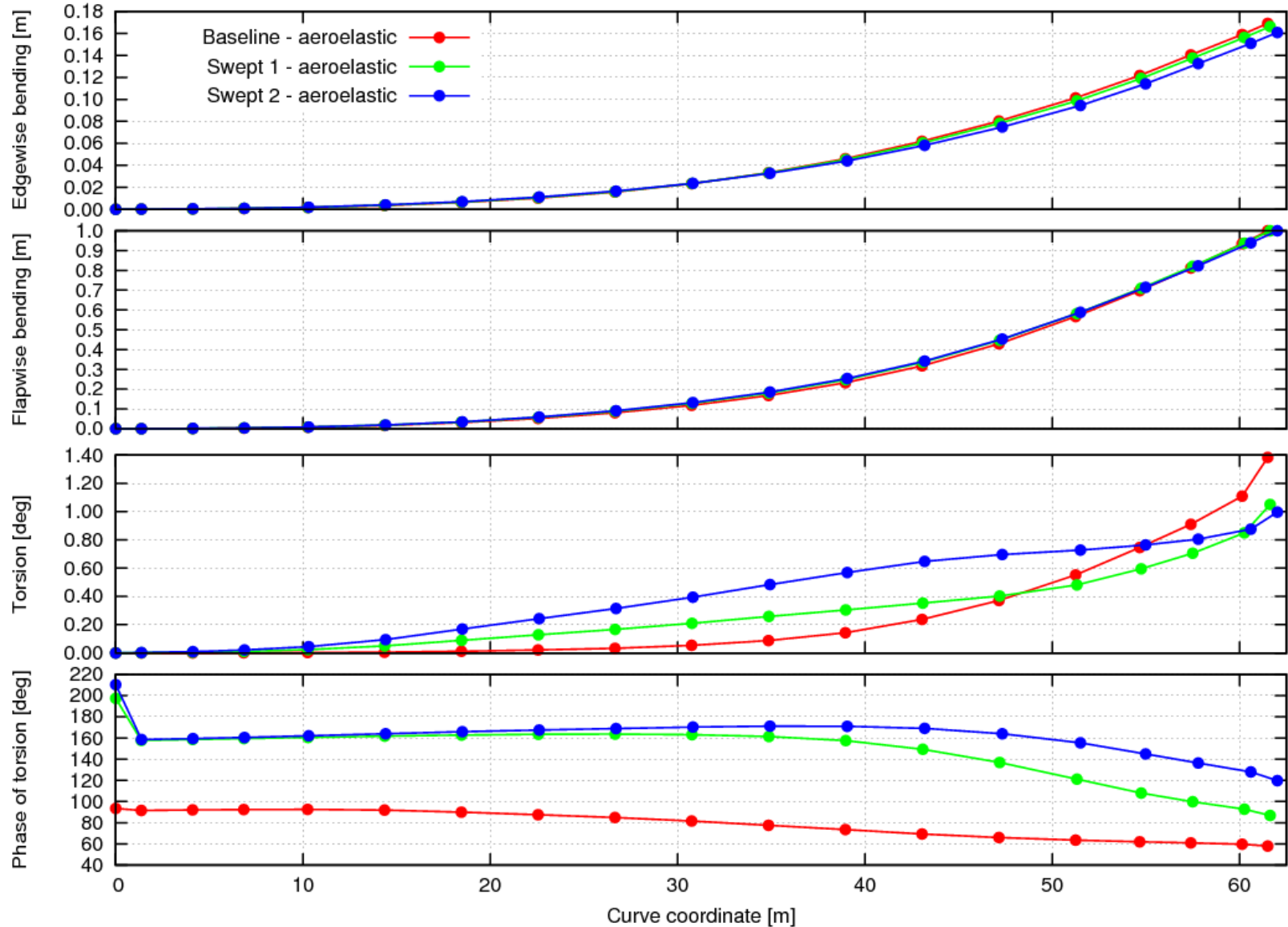
# Steady state thrust and tip deflection



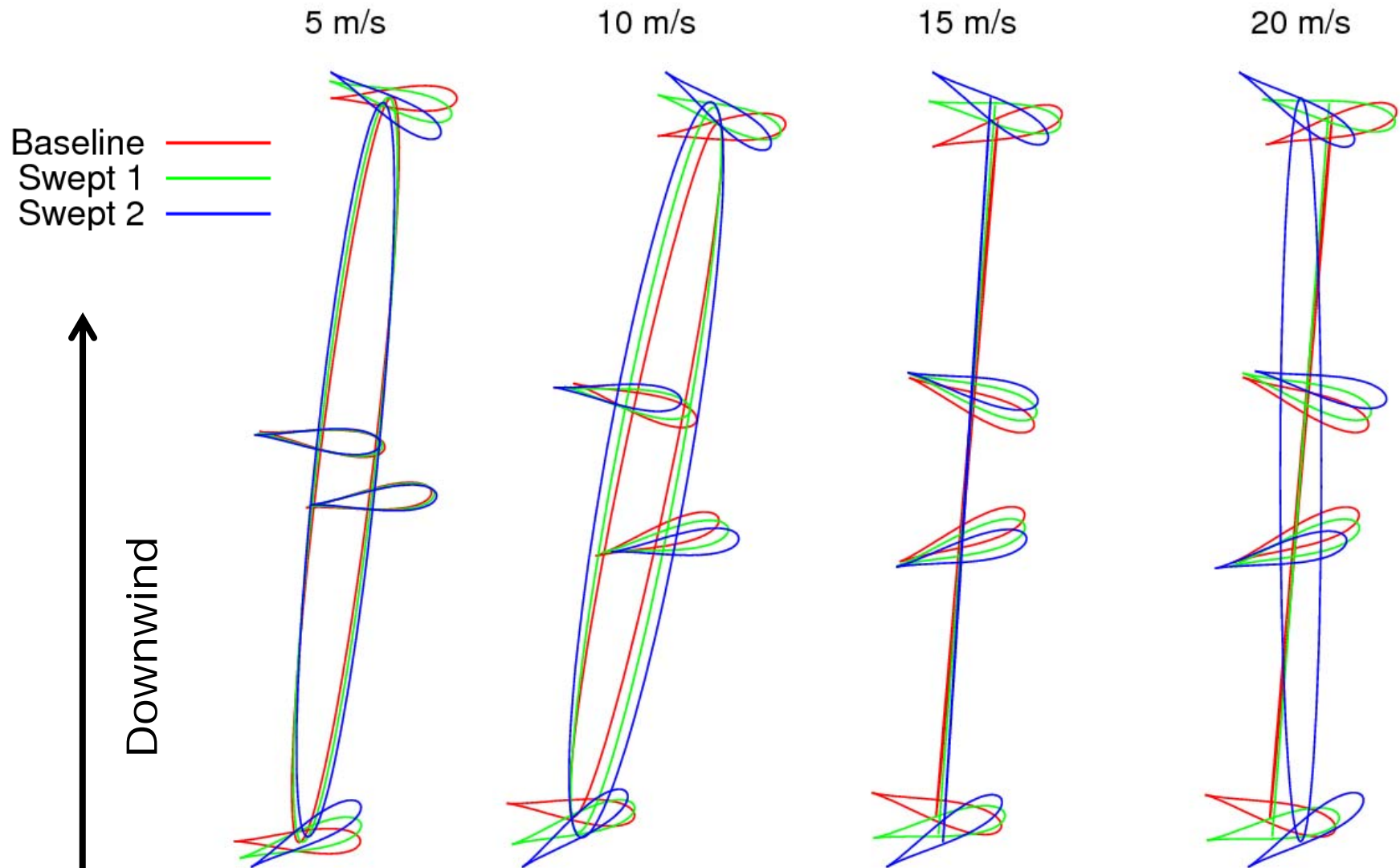
# Modal frequencies and damping – 1<sup>st</sup> flap



# Mode shapes at 12 m/s – 1<sup>st</sup> flap

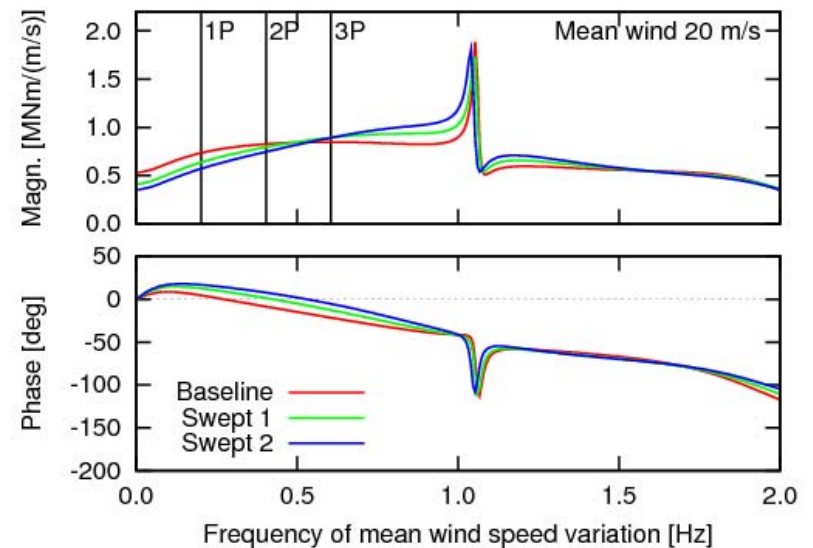
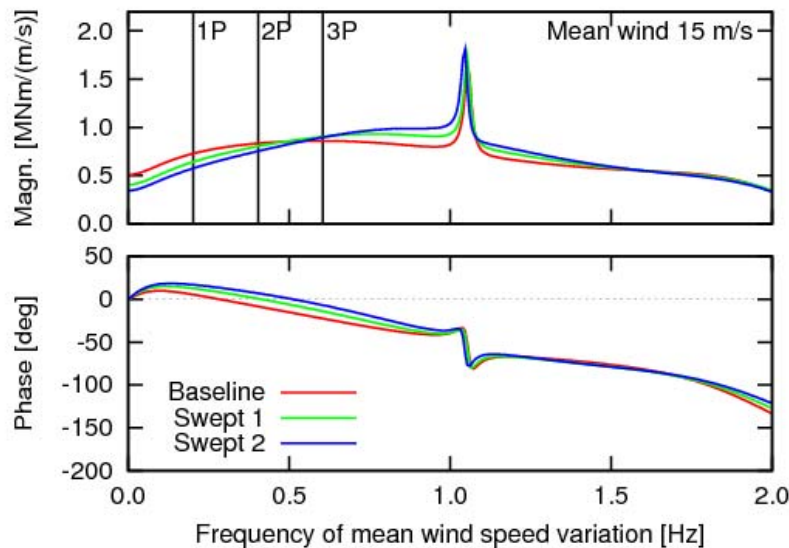
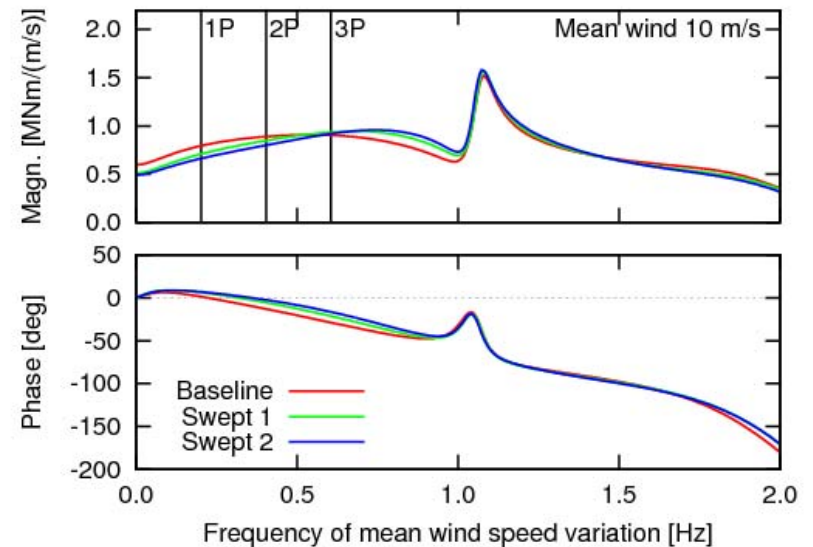
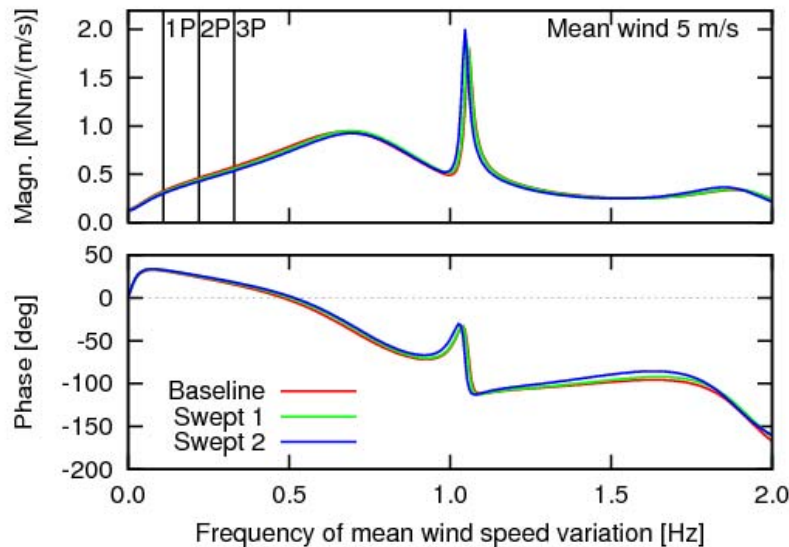


# Blade section motion at 75% radius – 1<sup>st</sup> flap

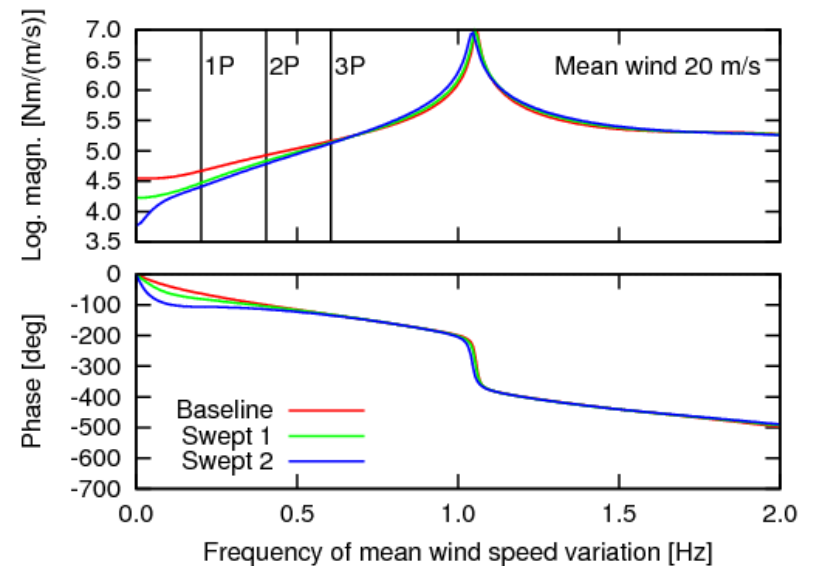
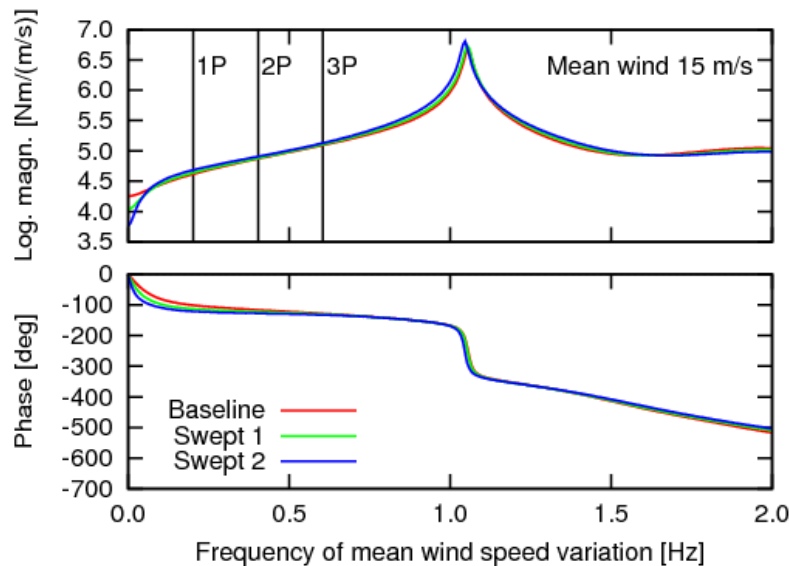
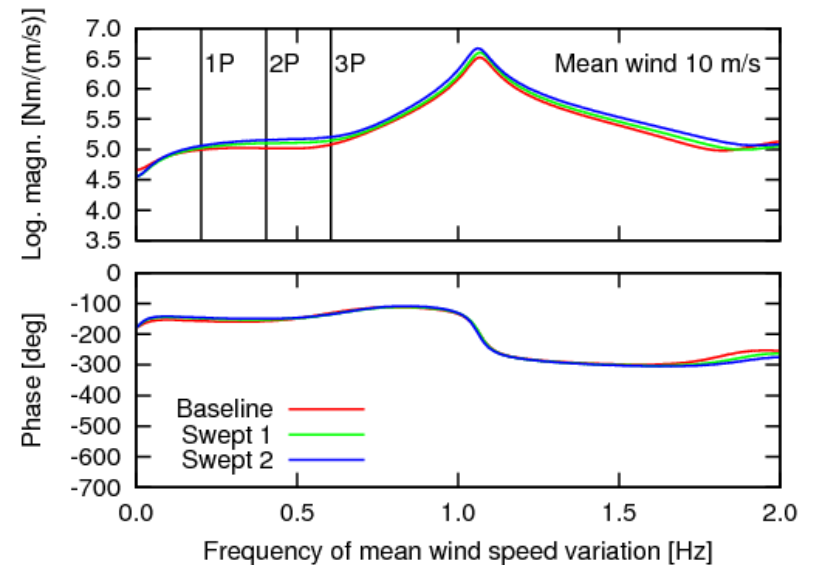
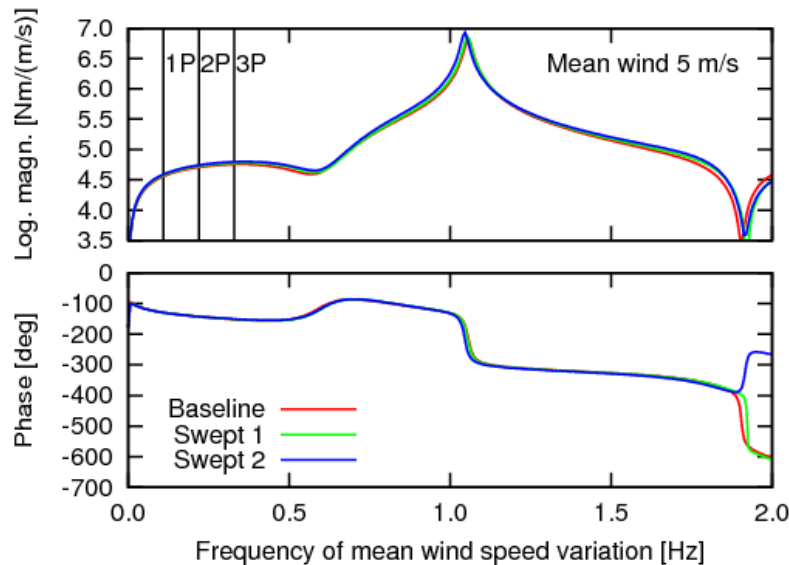




# Flapwise blade root moment



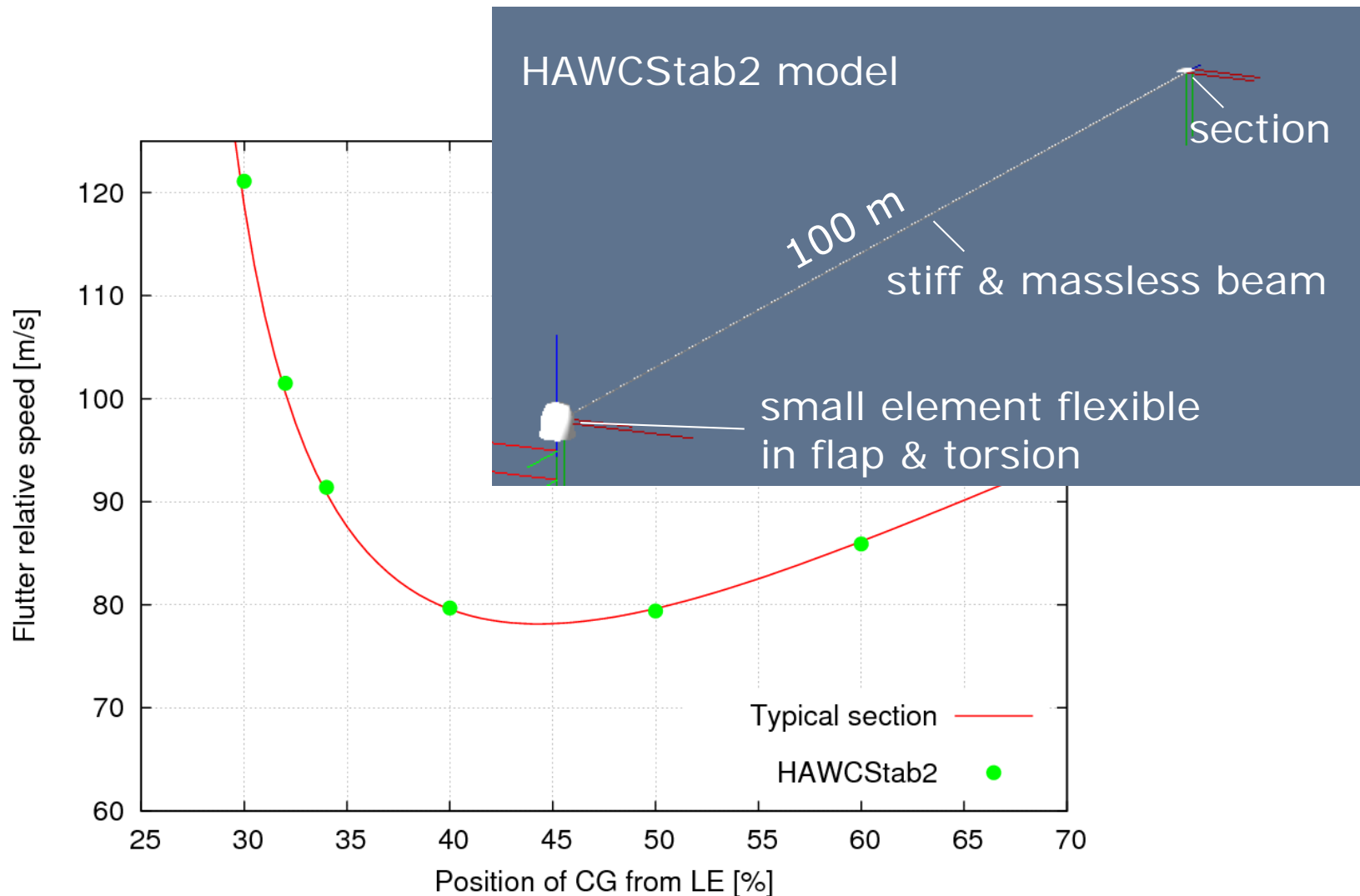
# Edgewise blade root moment



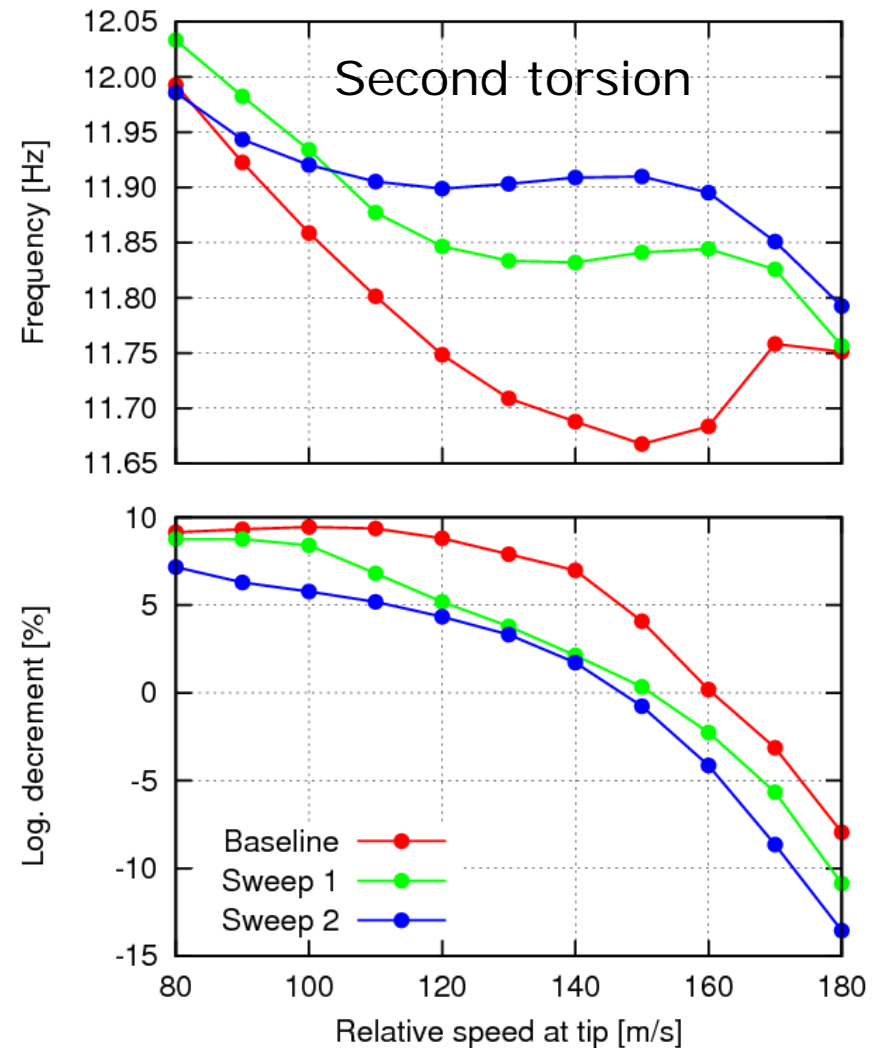
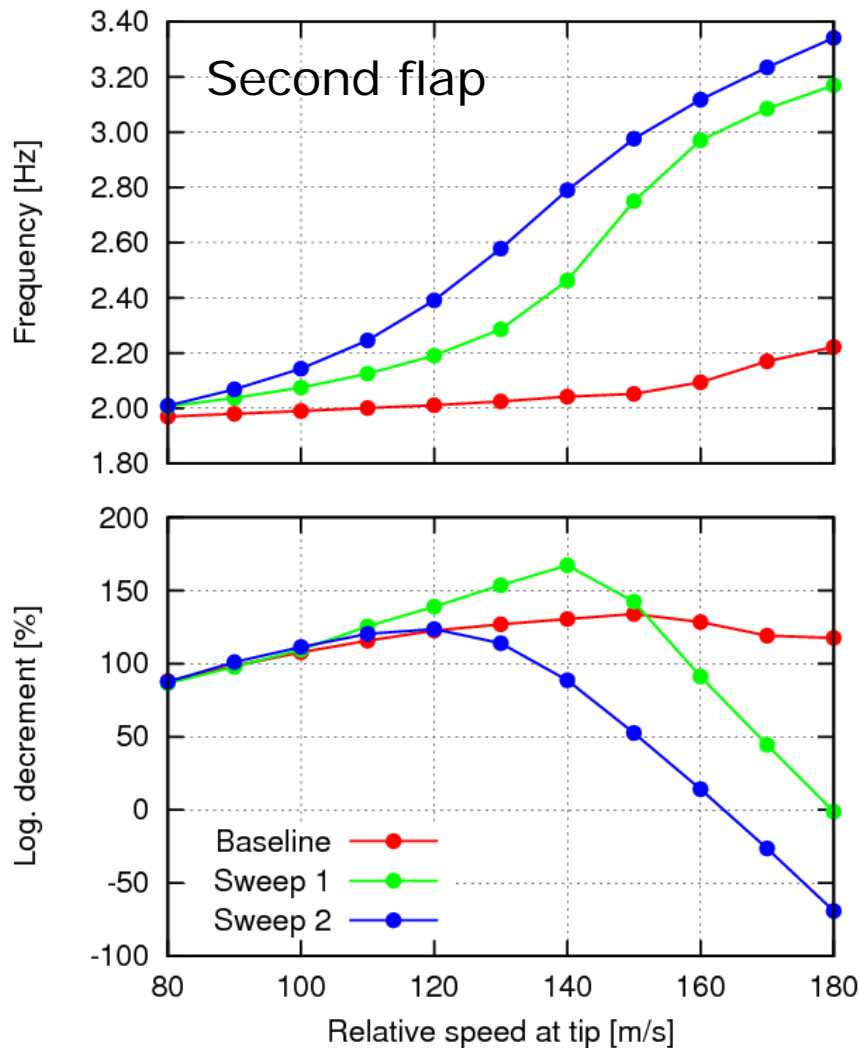
# Conclusions

- Backward swept blades twist towards feathering for flapwise bending in both structural and aeroelastic first flapwise bending modes
- This structural coupling of bending and torsion leads to higher aeroelastic modal frequency and lower aeroelastic damping of this mode
- The increased flapwise frequency of a backward swept blade is caused by added aerodynamic flapwise stiffness due to the twisting towards feathering when bending downwind
- This increased flapwise stiffness lowers the frequency response of backward swept blades at frequencies below the first flapwise frequency which can explain the reduced fatigue loads observed in previous studies
- The previously reported slight increase in edgewise blade root loads of backward swept blades can be explained by a slight reduction of aeroelastic damping of the first edgewise bending mode

# Flutter test case – Typical Section analogy



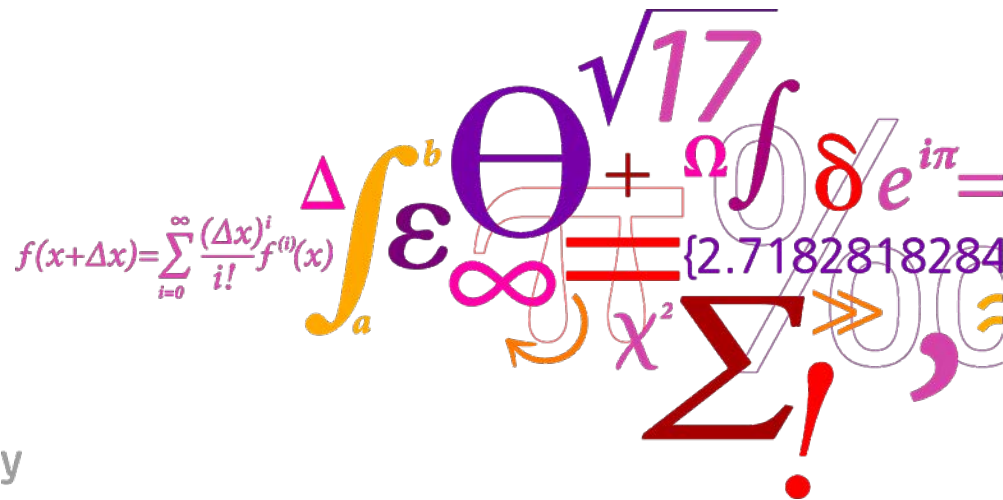
# Lowest damped modes for 0 deg pitch and increasing relative speed ( $\lambda = \sqrt{99}$ )



## **8 Aeroelastic rotor design minimizing the loads**

# Aeroelastic rotor design minimizing the loads

Mads Døssing, Christian Bak



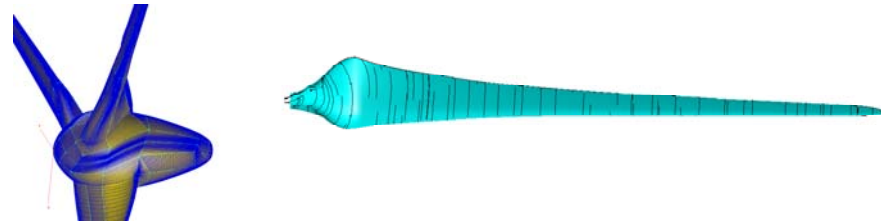
# Outline

- Background
- Simplified structural model
- Simplified fatigue model
- Influence of wide/slender blade on loads
- Optimization procedure
- Blade with DU airfoils (NREL 5MW)
- Blade with Risø-B1 airfoils (NREL 5MW)
- Conclusions



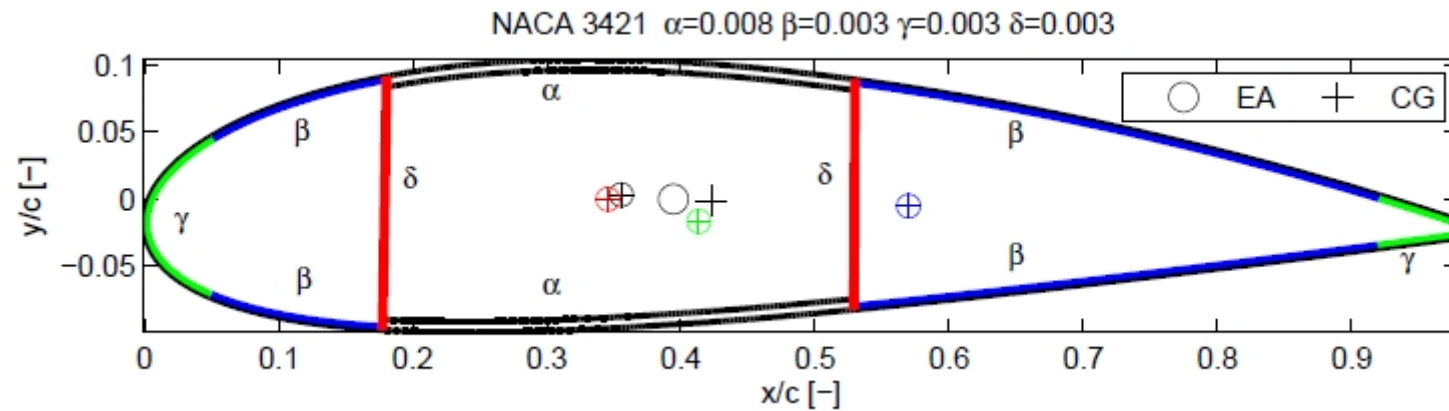
# Background

- Design of rotors purely based on aerodynamics have been carried out several times e.g. by Johansen et al.



- Design of rotors and the influence on loads have been investigated e.g. by Fuglsang in Research in Aeroelasticity, EFP2002. However, constant structural layout was assumed.
- Also, design of rotors and the influence on loads have been investigated e.g. by Fuglsang et al in the EU project SITEOPT. However, structural correlation to rotor design was very simple.
- In this work more advanced models (however still simple) are developed to take into account mass and stiffness variations

# Simplified structural model



# Simplified structural model

Section area (closed section)	$A_0 = c^2 C_{A_0}$
Section mass	$m = c^2 \sum_i \alpha_i \rho_i C_{A_i}$
Longitudinal stiffness	$EA = c^2 \sum_i \alpha_i E_i C_{A_i}$
Moment of stiffness about the x axis	$ES_x = c^3 \sum_i \alpha_i E_i C_{S_{x_i}}$
Moment of stiffness about the y axis	$ES_y = c^3 \sum_i \alpha_i E_i C_{S_{y_i}}$
Moment of mass about the x axis	$\rho S_x = c^3 \sum_i \alpha_i \rho_i C_{S_{x_i}}$
Moment of mass about the y axis	$\rho S_y = c^3 \sum_i \alpha_i \rho_i C_{S_{y_i}}$
Moment of stiffness inertia about the x axis	$EI_x = c^4 \sum_i \alpha_i E_i C_{I_{x_i}}$
Moment of stiffness inertia about the y axis	$EI_y = c^4 \sum_i \alpha_i E_i C_{I_{y_i}}$
Moment of centrifugal stiffness	$ED_{xy} = c^4 \sum_i \alpha_i E_i C_{D_{xy_i}}$

$C_{A_0} = \int_i \text{sgn}(y^*) y^* dx^*$
$C_{A_i} = \int_i ds^*$
$C_{S_{x_i}} = \int_i y^* ds^*$
$C_{S_{y_i}} = \int_i x^* ds^*$
$C_{I_{x_i}} = \int_i y^{*2} ds^*$
$C_{I_{y_i}} = \int_i x^{*2} ds^*$
$C_{D_{xy_i}} = \int_i x^* y^* ds^*$

# Simplified fatigue model

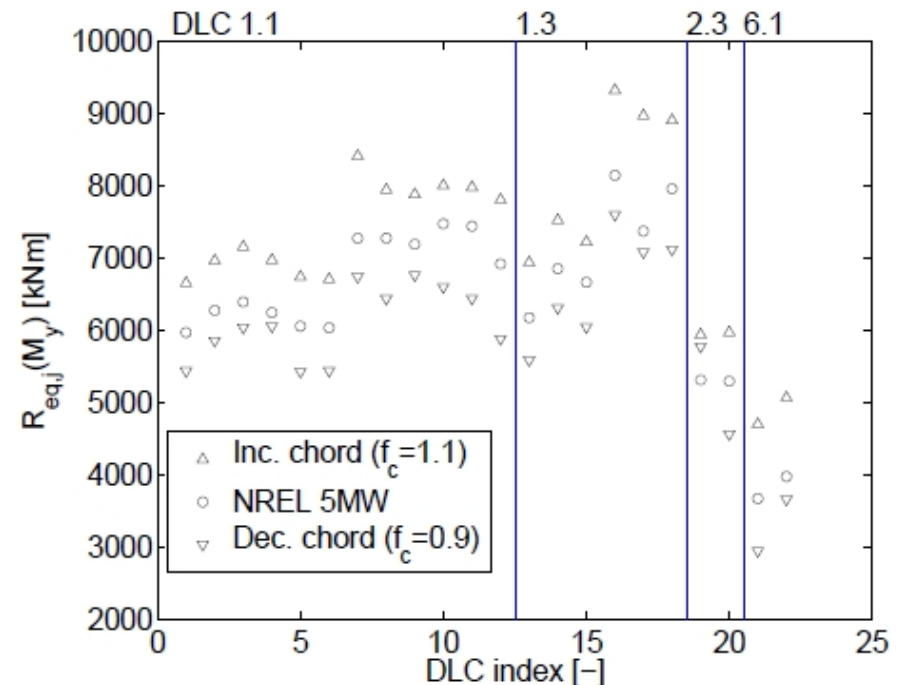
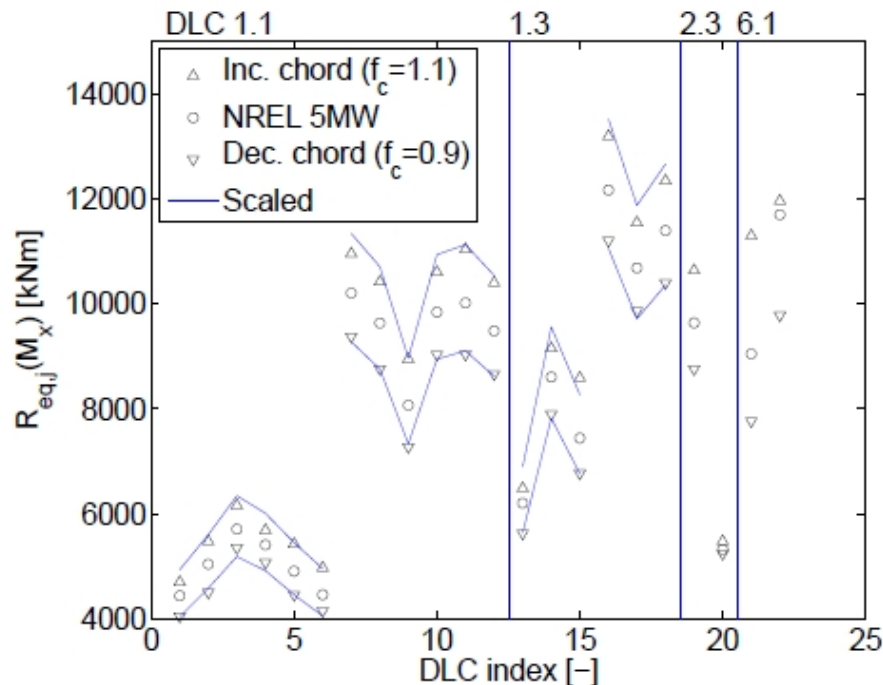
$$R_{eq} \propto (1 - a)^{1/m} \Omega^{1+1/m} \int_r^R (r' - r) r' C_l' c dr'$$



$$R_{eq} \propto c_1 = \Omega \int_r^R (r' - r) r' c dr'$$

# Influence of wide/slender blade on loads

	M [kg]	AEP [GWh]	$f_1$ [Hz]	$f_2$ [Hz]	$f_3$ [Hz]
Increased chord ( $f_c=1.1$ )	16900	19.72	0.647	1.10	1.91
NREL 5MW	15100	19.51	0.665	1.05	1.94
Decreased chord ( $f_c=0.9$ )	13340	19.23	0.683	9.84	1.99



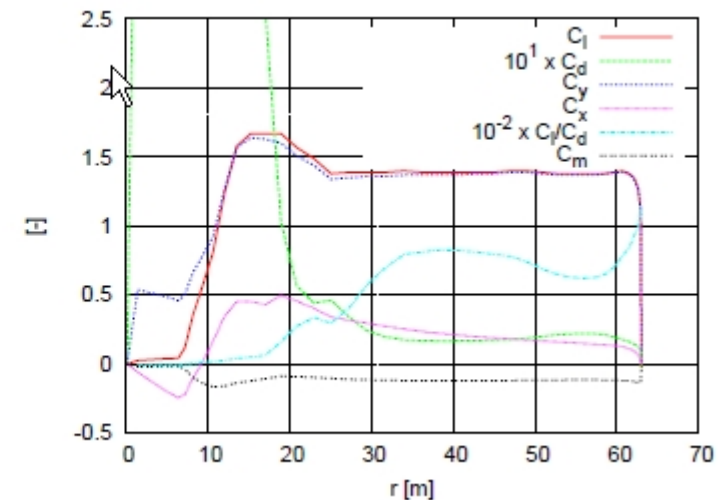
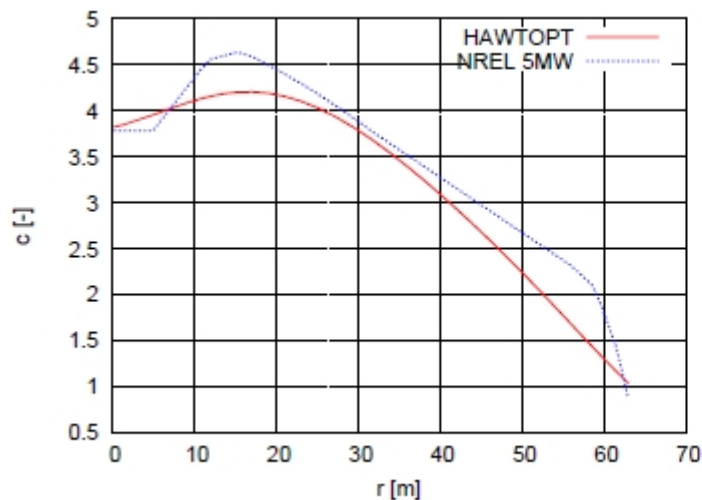
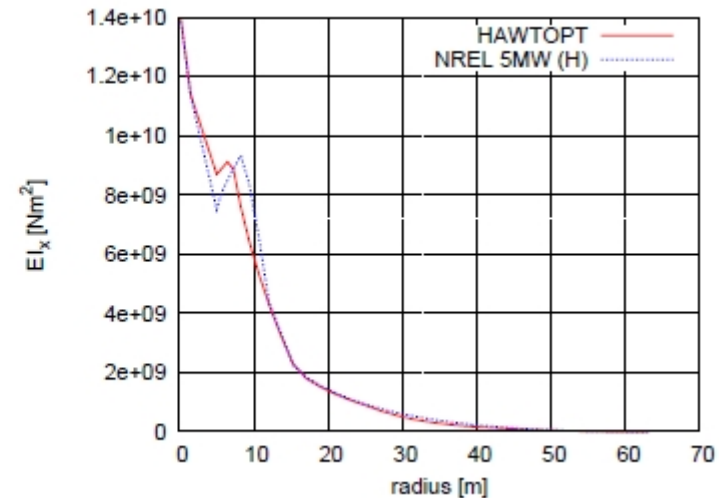
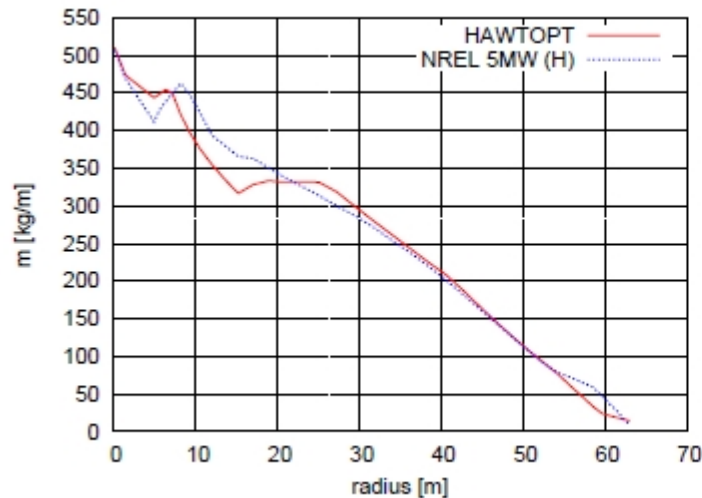
# Optimization procedure

- Optimization using steady state aerodynamic design and simplified fatigue model to reduced blade root flap fatigue load. Constraints on power and blade mass in design point (design point: 11m/s i.e. at rated wind speed for load reduction)

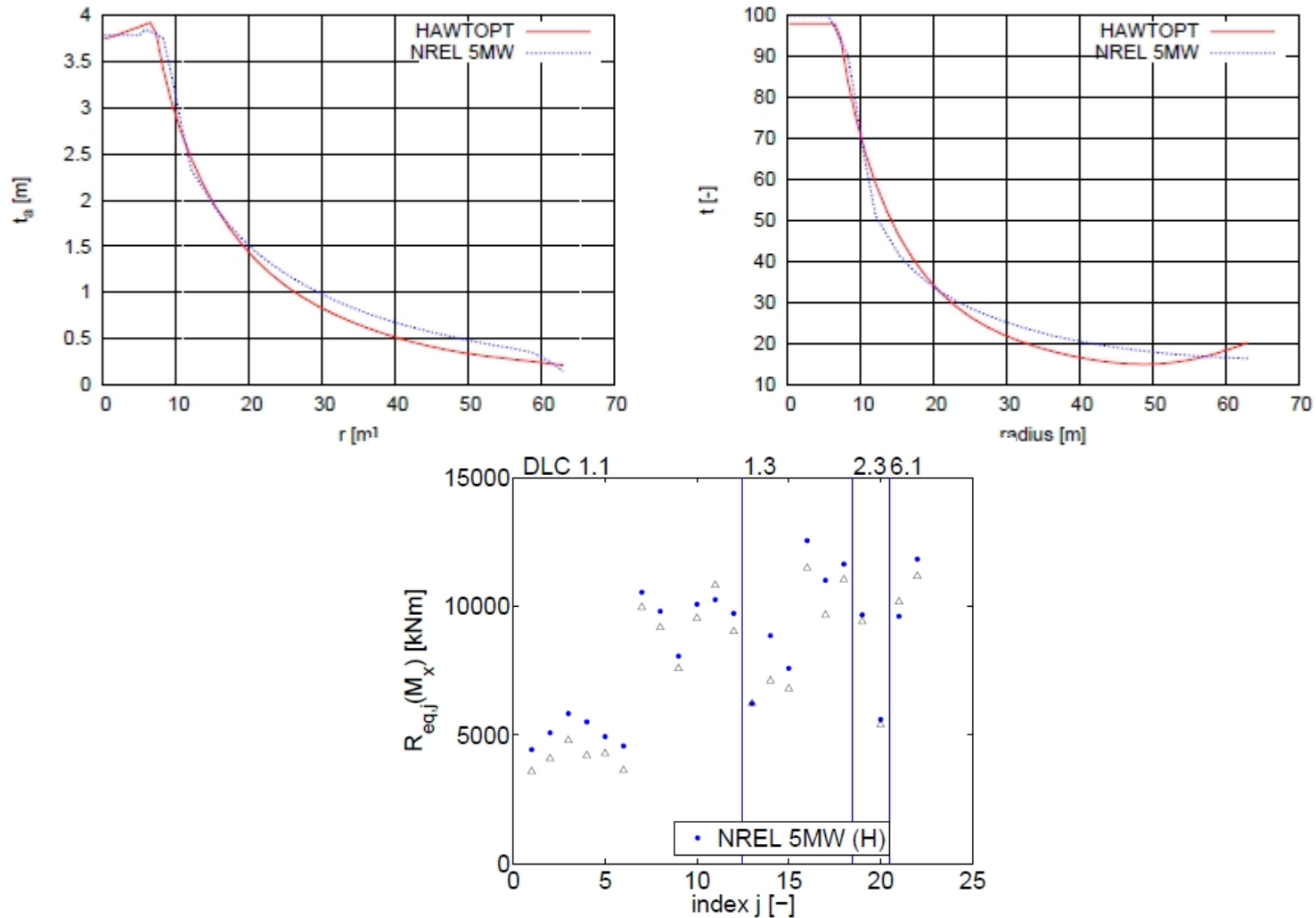


- Optimization using aeroelastic computations (HAWC2) with reduced number of design load cases to reduce blade root flap fatigue load. Constraints on power and blade mass in design point (design point: 10m/s )
- The load cases should as far as possible be controller independent
- No power optimization

# Blade with DU airfoils (NREL 5MW)

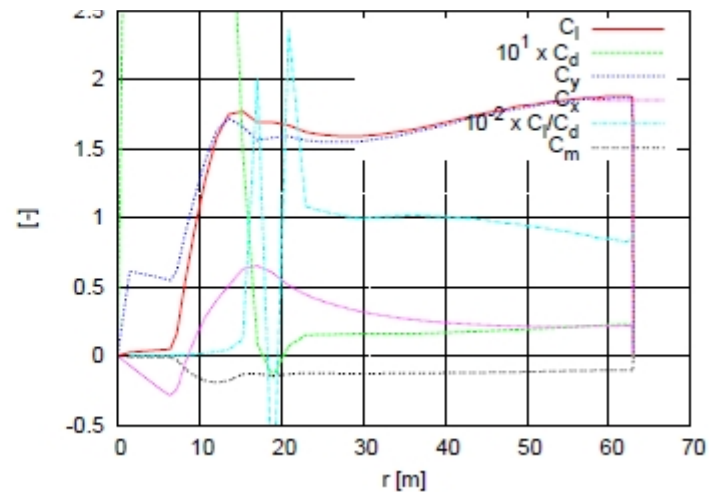
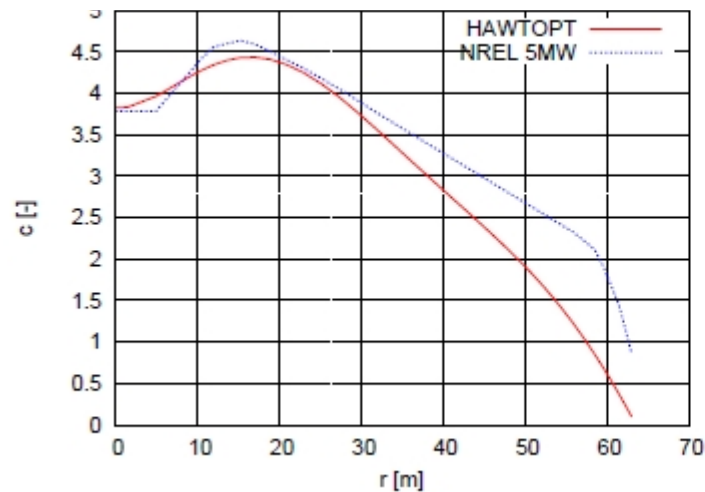
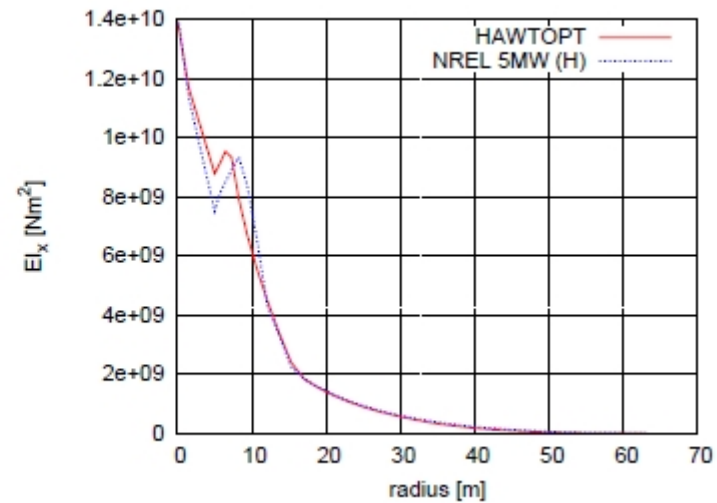
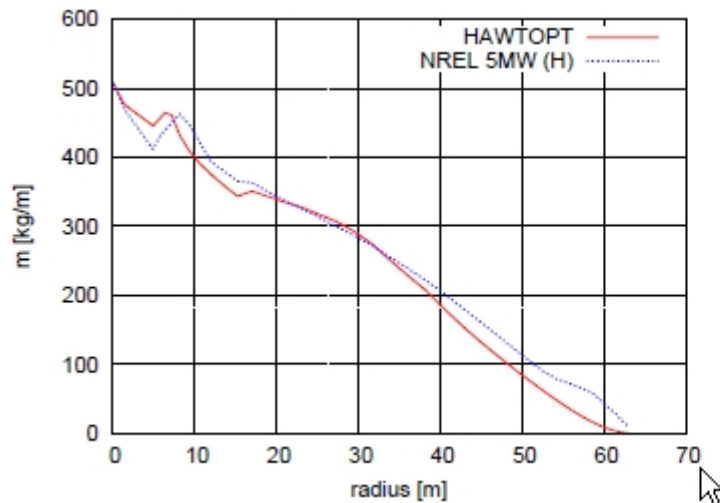


# Blade with DU airfoils (NREL 5MW)

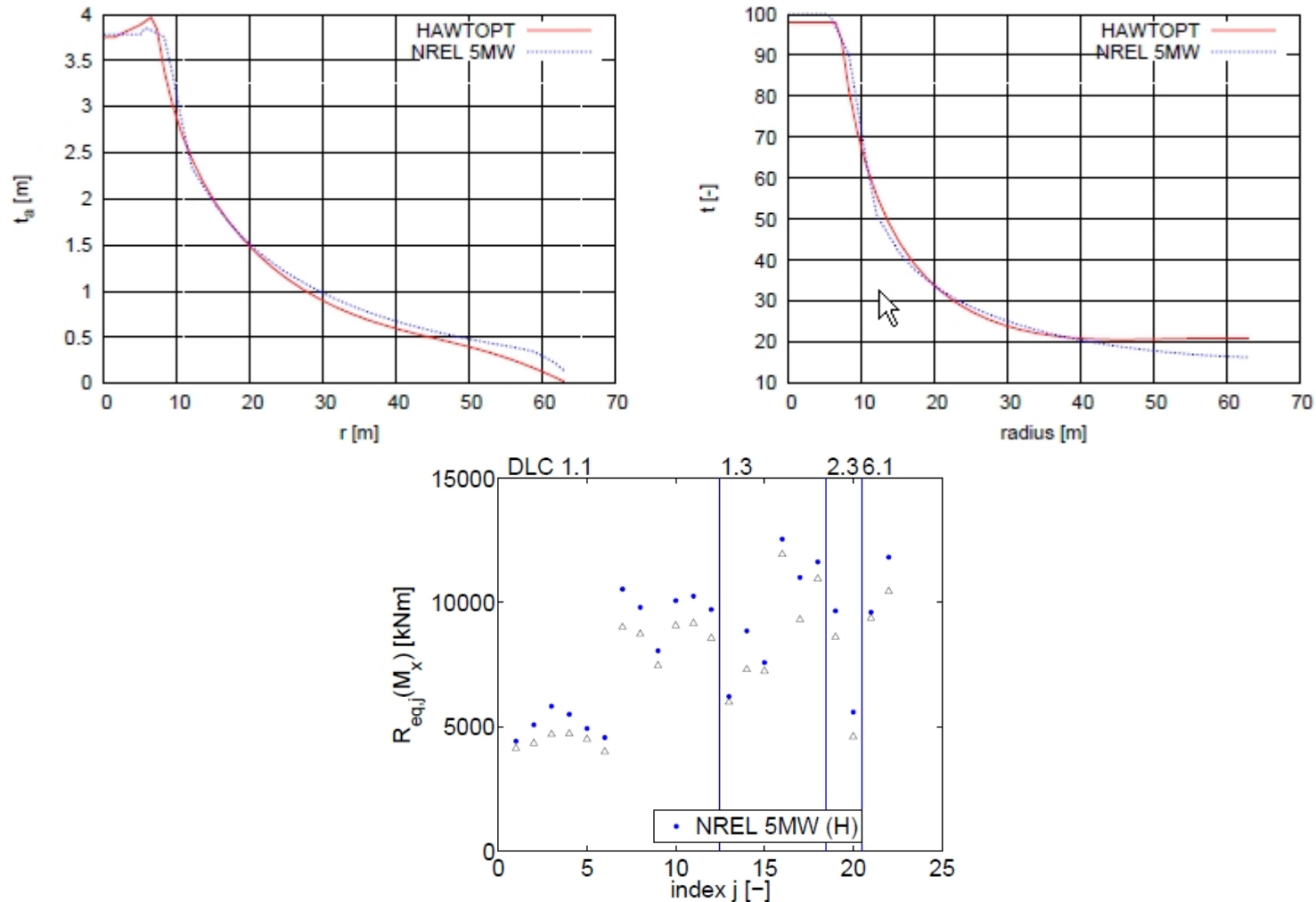




# Blade with Risø-B1 airfoils (NREL 5MW)



# Blade with Risø-B1 airfoils (NREL 5MW)



# Comparing blades

		$M$ [kg]	$f_1$ [Hz]	$f_2$ [Hz]	$f_3$ [Hz]
6.1	NREL 5MW	16880	0.672	1.05	1.95
6.2	NREL 5MW (H)	16330	0.665	1.06	1.94
6.4	Point Opti. (DUxx)	15945	0.658	1.03	1.89
6.5	Point Opti. (B1-xx)	15500	0.798	1.19	2.25

		AEP [GWh]	Airfoils	$\lambda$	$C_l$
6.1	NREL 5MW	21.3425	DUxx	7.7	0.95
6.4	Point Opti. (DUxx)	21.0414	DUxx	6.4	$\approx 1.4$
6.5	Point Opti. (B1-xx)	20.9682	B1-xx	6.4	$\approx 1.6-1.8$

		$R_{eq,1(100s)}(M_x)$	$R_{eq}(M_x)$	$R_{eq}(M_y)$
6.1	NREL 5MW	-	-	-
6.2	NREL 5MW (H)	4202.0	5983.0	5270.9
6.4	Point Opti. (DUxx)	3142.0	5787.5	5376.2
6.5	Point Opti. (B1-xx)	3466.0	5258.1	4966.1

# Conclusions

- A simplified structural model has been formulated
  - Comparison to existing blades show good agreement
- A simplified fatigue model has been formulated
  - Comparison to aeroelastic calculations show good agreement
  - Slender blades show lower loads
- Design with DU airfoils showed
  - 3.3% reduction in fatigue loads
  - 2.4% reduction in mass
  - 1.4% reduction in AEP
- Design with Risø B1 airfoils showed
  - 12.1% reduction in fatigue loads
  - 5.1% reduction in mass
  - 1.8% reduction in AEP

## **9 A small study of flat back airfoils**

## A Small Study of Flatback Airfoils

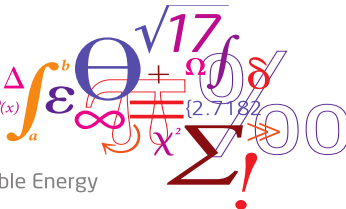
Niels N. Sørensen

Wind Energy Division · Risø DTU

RISØ-DTU, 27-01-2011



$$f(x+\Delta x) = \sum_{i=0}^{\infty} \frac{(\Delta x)^i}{i!} f^{(i)}(x)$$



Risø DTU

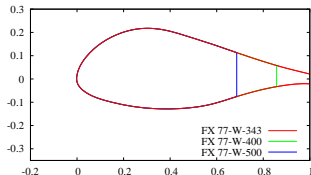
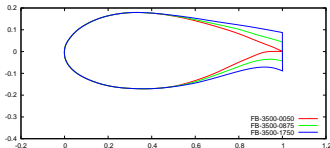
National Laboratory for Sustainable Energy

## Outline

- 1 Introduction
- 2 Flow solver settings
- 3 Grid Generation
- 4 Evaluation of Performance, 2D
- 5 3D Investigation
- 6 Parametric Study, 2D
- 7 Conclusion and Further Work

## Background

- ◆ Why are 'flatback' airfoils interesting for rotor root design
  - ◆ They may be desirable from a structural point of view
  - ◆ They are claimed to be more roughness insensitive
  - ◆ They can provide relatively high lift ( $Cl > 2$ )
  - ◆ The drag penalty of the thick trailing edge may not be important at the inboard sections
  - ◆ They are sometimes claimed to be more efficient than traditional truncated airfoils





- ◆ What problems must be foreseen when designing 'flatback' airfoils, designed for the root section where the thickness is larger than 30%
  - ◆ Typical design codes as the Xfoil code will eventually fail to give answers due to the trailing edge thickness
  - ◆ The validity of CFD codes for these airfoils must be checked
  - ◆ Wind tunnel testing of thick airfoils at high Re and AOA may be difficult
  - ◆ What should the design philosophy be
- ◆ How will the flatback airfoils work during operational conditions
  - ◆ How will the 3D effects often referred to as 'Stall Delay' influence the performance
  - ◆ How are there dynamical behaviour in stall

## Present Study

The present study will not answer all these questions, but is the first step towards the design and testing of a flatback airfoil.

- ◆ We will evaluate the capability of our in-house CFD solver (EllipSys) to predict flatback and truncated airfoils
- ◆ We will briefly investigate possible wall junction problems for thick airfoils in tunnels
- ◆ We will do a small parametric study of possible ways to generate truncated airfoils

## EllipSys2D/3D

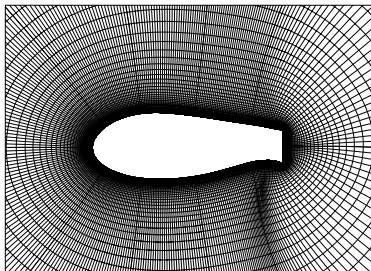
- ◆ Two dimensional simulations and a few three dimensional simulations are performed
- ◆ Both steady and transient runs  $\Delta t = \tilde{\Delta t} \frac{c}{U_\infty} = 1 \times 10^{-2}$
- ◆ For the 2D simulations we use both fully turbulent and transitional computations based on the  $k - \omega$  SST model
- ◆ For the 3D simulations we use a so called Delayed Detached Eddy Simulation technique based on the SST model, along with the transition modeling
- ◆ Transition modeling is based on the  $\gamma - Re_\theta$  model
- ◆ The diffusive terms are model using central differences
- ◆ In 2D the third order accurate QUICK scheme is used for the convective terms
- ◆ In 3D a hybrid fourth order central/QUICK scheme is used to resolve the DES areas

## Grid Generation

### Grid Generation 2D

All grids are generated with the hyperbolic grid generation code HypGrid2D

- ◆ The grid has 320 cells in chordwise direction, and 128 cells in the wall normal direction
- ◆ The height of the first cell is  $1 \times 10^{-6} \times \text{Chord}$
- ◆ The outer boundary are placed 45 Chords away from the airfoil

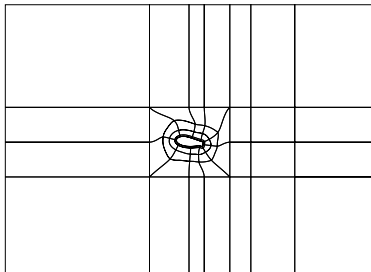


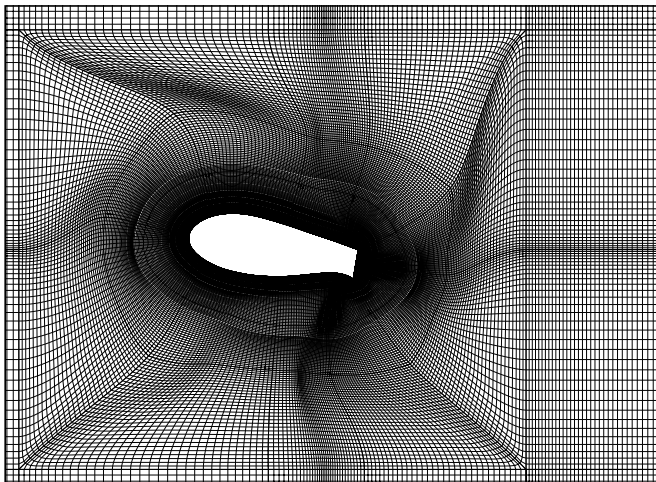
## Grid Generation

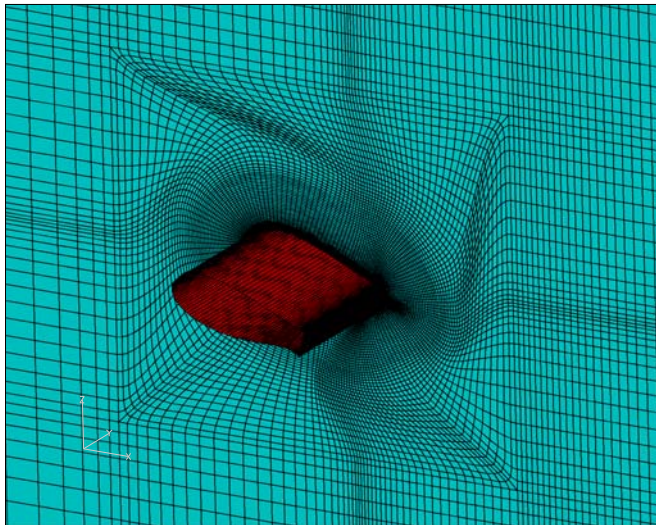
### Grid Generation 3D

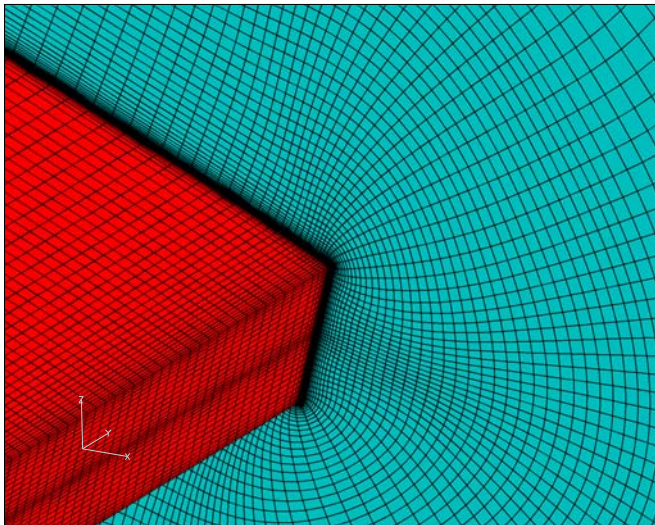
All grids are generated with the hyperbolic grid generation code HypGrid2D

- ◆ The inner O-grid has 320 cells in chordwise direction, and 128 cells in the wall normal direction
- ◆ The inner O-grid is embedded in a stretched square grid
- ◆ The height of the first cell is  $1 \times 10^{-6} \times \text{Chord}$
- ◆ The upstream and downstream boundaries are placed 9 chords away, while the bottom and lid are approximately 5 chords away
- ◆ In the spanwise direction, the domain is 1 Chord long and 128 cells are used











## FX-77-W-343

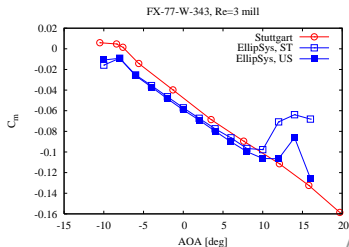
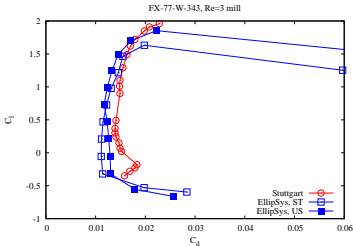
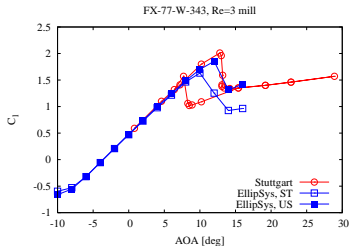
Conditions:  $Re = 3 \times 10^6$ , free transition

Data from University of Stuttgart



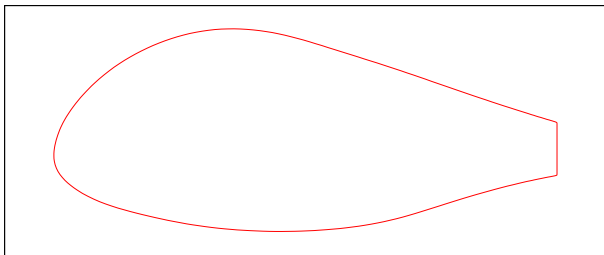
## FX-77-W-343

Conditions:  $Re = 3 \times 10^6$ , free transition  
Data from University of Stuttgart



## **FX-77-W-400**

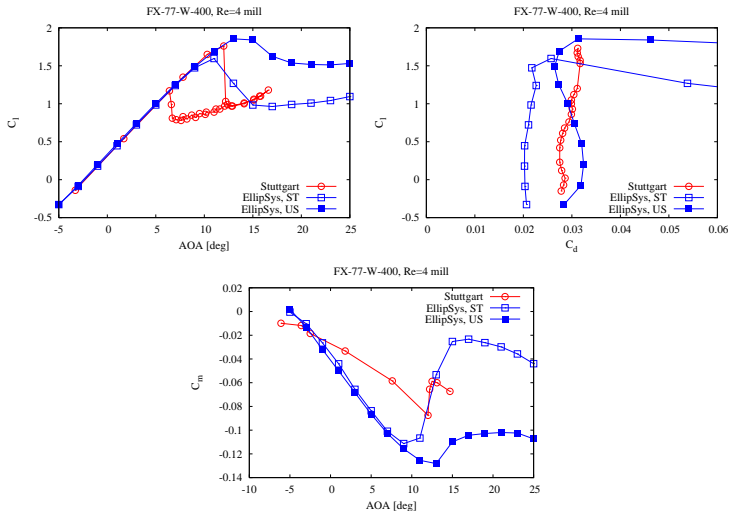
Conditions:  $Re = 4 \times 10^6$ , free transition



# Evaluation of Performance, 2D

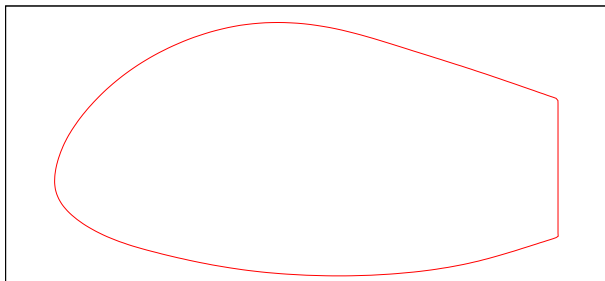
## FX-77-W-400

Conditions:  $Re = 4 \times 10^6$ , free transition



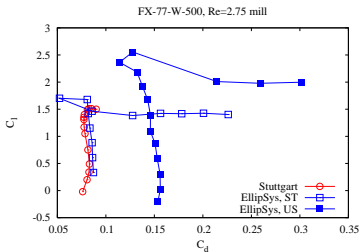
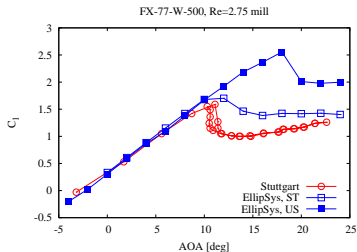
## FX-77-W-500

Conditions:  $Re = 2.75 \times 10^6$ , free transition



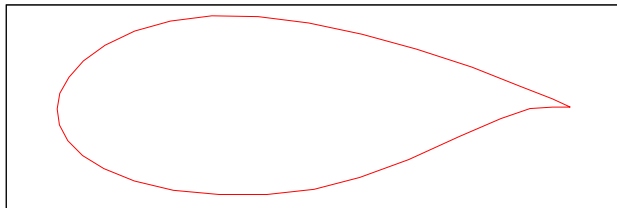
## FX-77-W-500

Conditions:  $Re = 2.75 \times 10^6$ , free transition



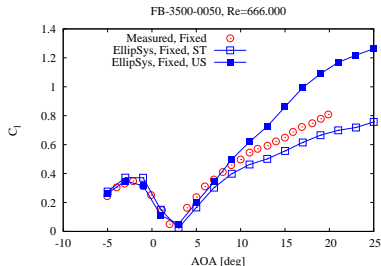
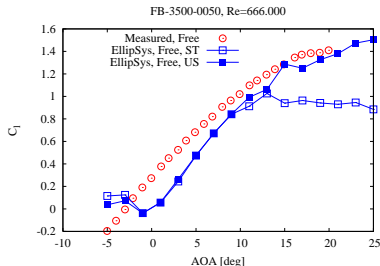
## FB-3500-0050

Conditions:  $Re = 666.000$ , free transition left and fixed right  
Data from University of California (UC Davis)



## FB-3500-0050

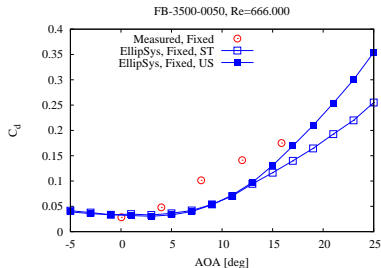
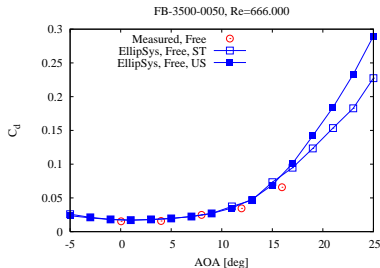
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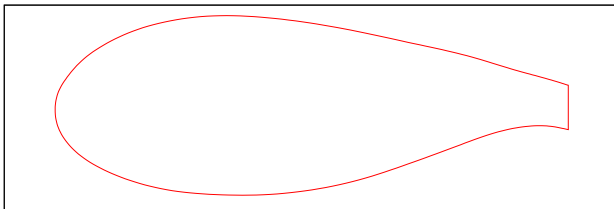
## FB-3500-0050

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Data from University of California (UC Davis)



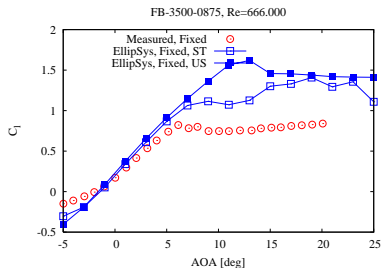
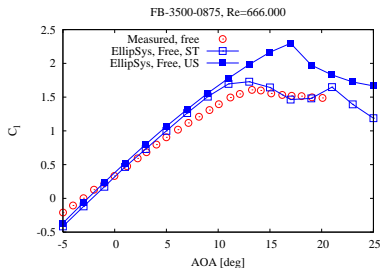
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Conditions:  $Re = 666.000$ , free transition left and fixed right



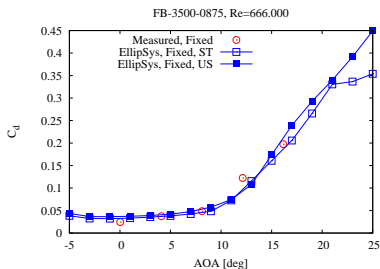
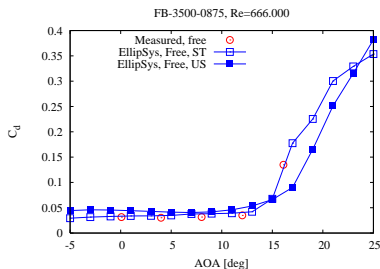
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Conditions:  $Re = 666.000$ , free transition left and fixed right



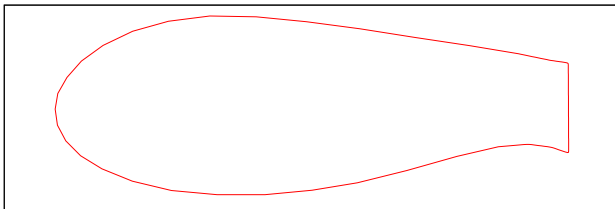
## FB-3500-0875

Conditions:  $Re = 666.000$ , free transition left and fixed right



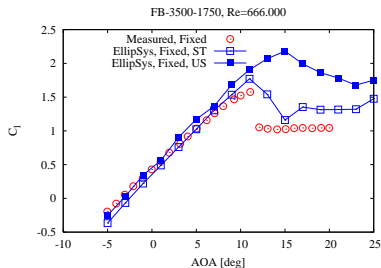
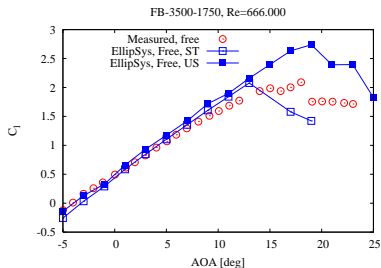
## FB-3500-1750

Conditions:  $Re = 666.000$ , free transition left and fixed right



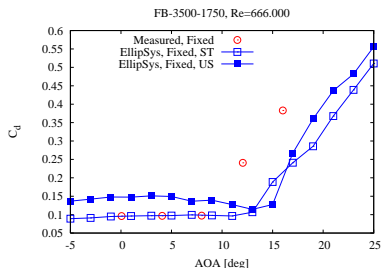
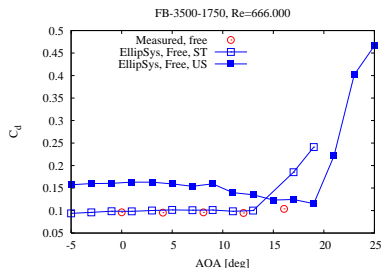
## FB-3500-1750

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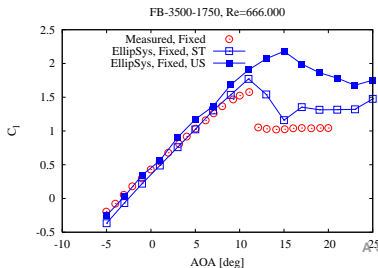
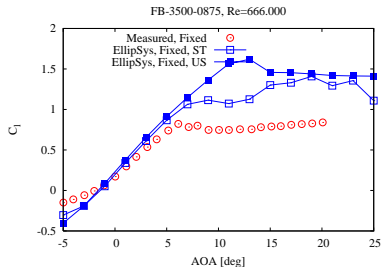
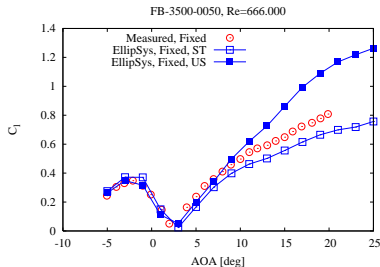
## FB-3500-1750

Conditions:  $Re = 666.000$ , free transition left and fixed right



## FB-3500

### Comparison of the three flat back airfoils

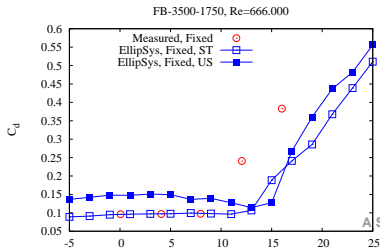
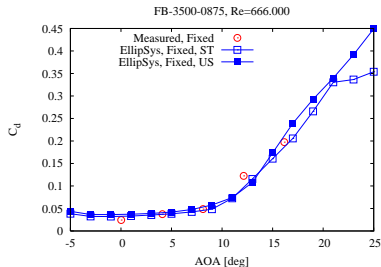
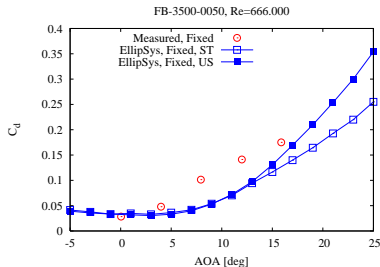




# Evaluation of Performance, 2D

## FB-3500

### Comparison of the three flat back airfoils

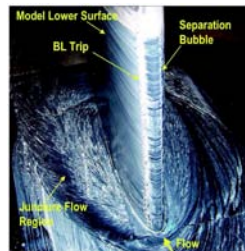
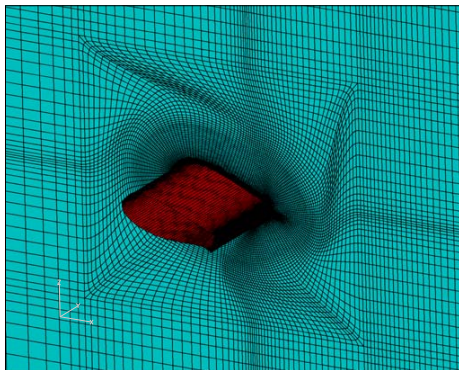


### Resume of performance evaluation

- ◆ The solver is capable of reproducing effect of changing from free to fixed transition
- ◆ Generally the drag is well captured for the flatback airfoils, (it is mainly pressure based)
- ◆ In all 2D cases the steady state results are closer to the measured lift (slightly surprising)
- ◆ The tendency of the drag is not as clear, in some cases the unsteady agrees better
- ◆ We can use CFD to compare the quality of different designs

# 3D Investigation

- ◆ How will the flatback airfoils behave in the tunnel
- ◆ Is the fact that 2D steady computations perform better due to some 2D artifact
- ◆ Can 3D provide improved insight?

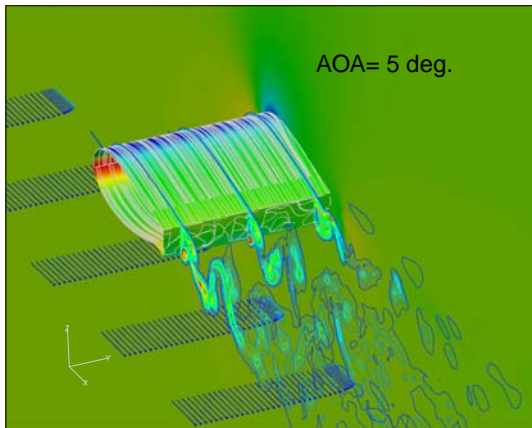


## 3D Investigation

### 3D Flow Patterns

Operational conditions

- ◆  $Re = 666.000$
- ◆ Free transition
- ◆ Span length is equal to 2 chords

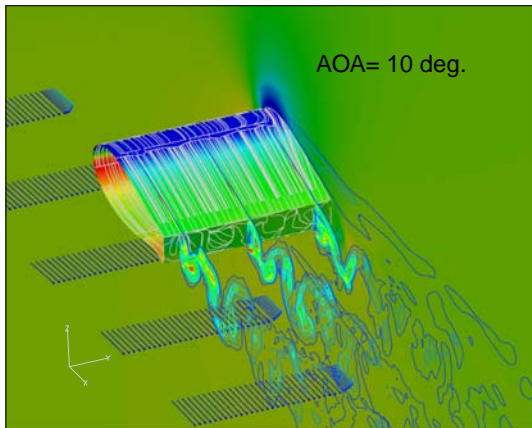


## 3D Investigation

### 3D Flow Patterns

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- ◆ Free transition
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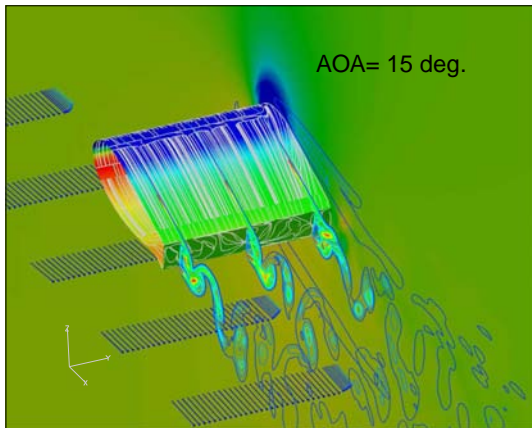


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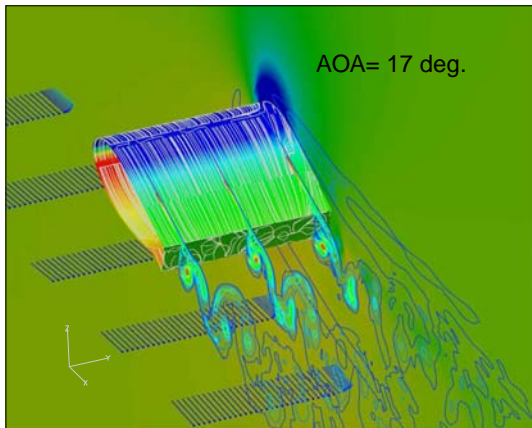


## 3D Investigation

### 3D Flow Patterns

Operational conditions

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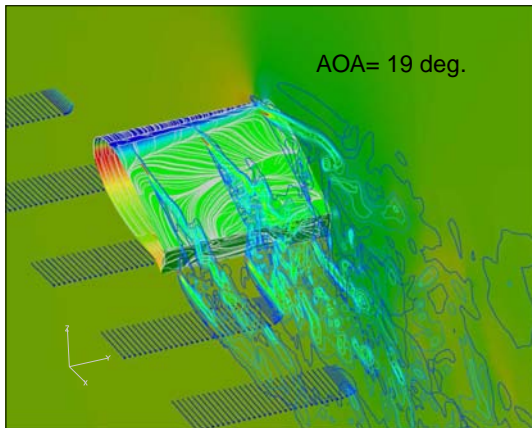


## 3D Investigation

### 3D Flow Patterns

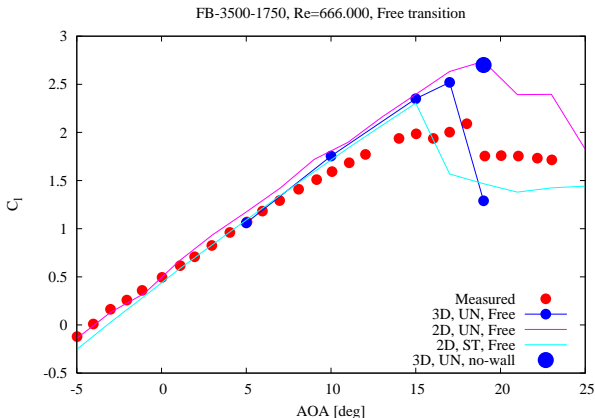
Operational conditions

- ◆  $Re = 666.000$
- ◆ Free transition
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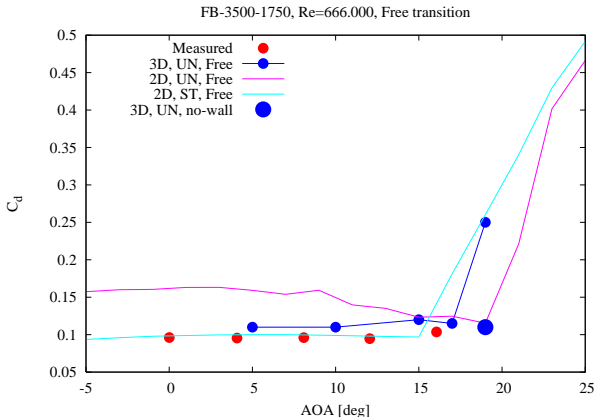


## Comparison between different techniques



- ◆ 3D unsteady comp. agrees better than 2D unsteady comp
- ◆ By coincidence 2D steady captures nearly the same value as 3D unsteady

## Comparison between different techniques



- ◆ 3D unsteady comp. agrees better than 2D unsteady comp
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### Resume of 3D computations

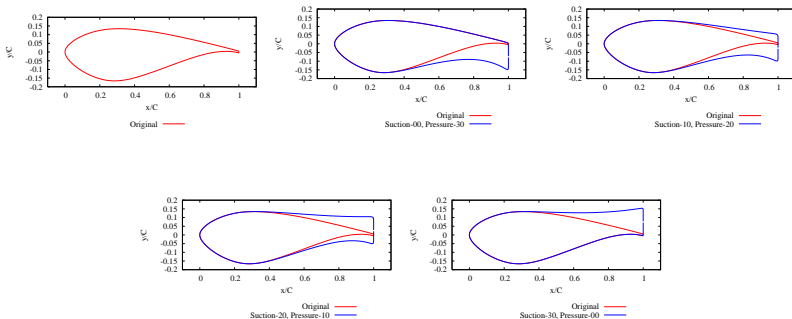
#### Results for the FB-3500-1750 Airfoil

- ◆ At low angles of attack ( $<17$  degrees) the inclusion of the wall junction only caused minor changes
- ◆ At high angle of attack ( $>17$  degrees) the wall junction induces severe 3D flow and low lift
- ◆ Tunnel effects may play an important role in experimental and computational evaluation of FB airfoils

## Flatbacking the DU-97-W-300

Operational conditions,  $Re = 3.2 \times 10^6$ , Free transition

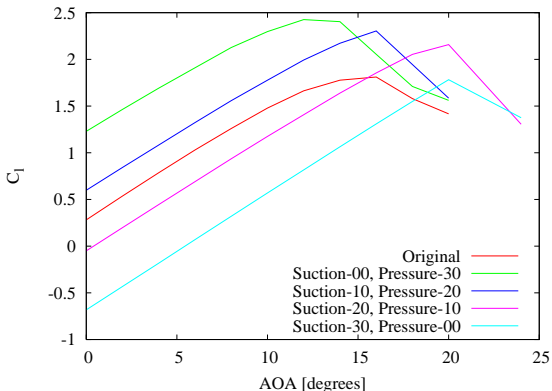
Opening the trailing edge, towards suction or pressure side



### Airfoil performance

Operational conditions,  $Re = 3.2 \times 10^6$ , Free transition

All generated flatback airfoils have higher max lift

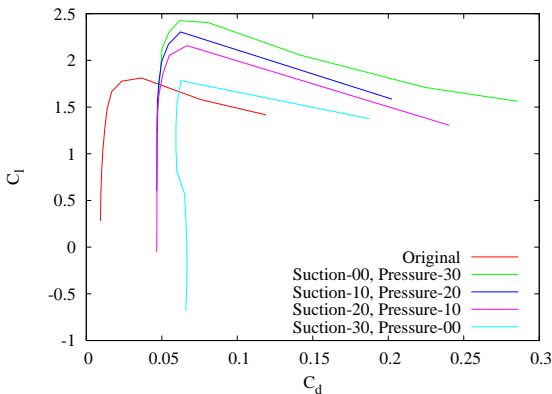


## Parametric Study, 2D

### Airfoil performance

Operational conditions,  $Re = 3.2 \times 10^6$ , Free transition

All generated flatback airfoils have higher drag



### Resume of parametric study

- ◆ The flatback version has a higher lift
- ◆ The most efficient one is the one opened solely to the pressure side
- ◆ The drag increases for all airfoils, and generally to the same level

## Conclusion and Further Work

### Conclusions:

- ◆ We believe that both the 2D/3D CFD solvers can be used to evaluate flatback airfoils
- ◆ Computations indicate that high lift can be obtained, and the exp. of FB-3500-1750 indicates that this may be true
- ◆ It is clear from the parametric study that to increase the lift the opening of the trailing edge must be done towards the pressure side

### Further work:

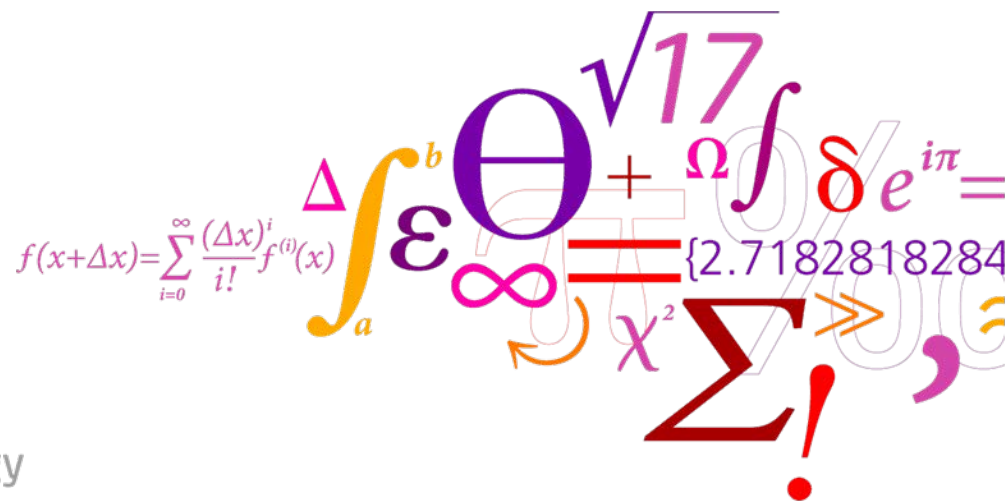
- ◆ We need to design an airfoil for tunnel test
- ◆ We need to evaluate the dynamic performance (3D dynamic stall comp.)
- ◆ We need to evaluate the performance of flatback in rotational environment
- ◆ Noise issues from the vortex shedding at the thick trailing edge



## **10 Status of airfoil design**

# Status of airfoil design and plans for wind tunnel tests of new thick airfoils

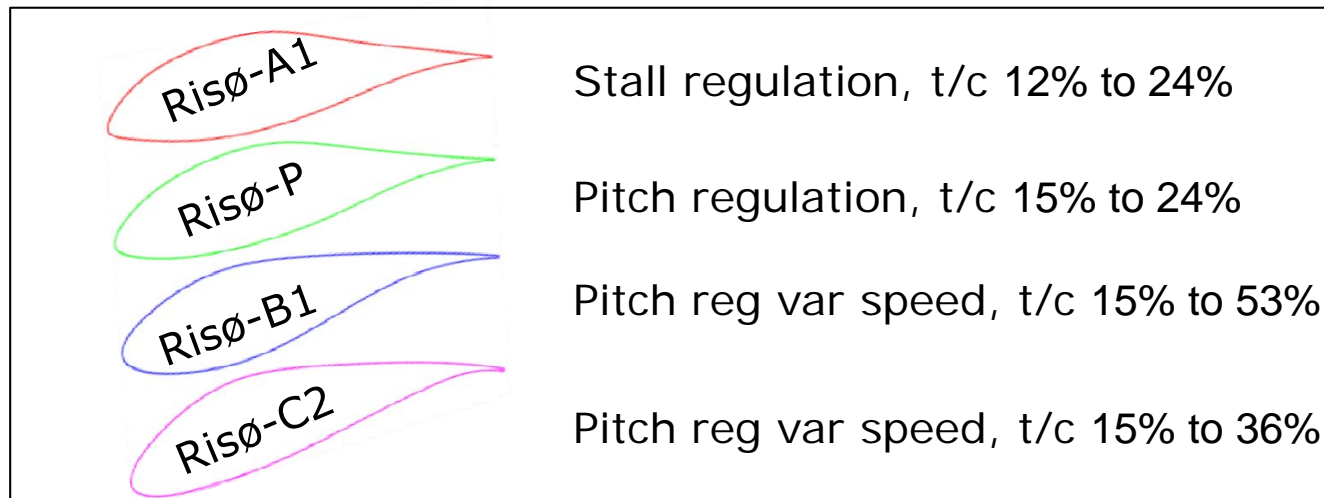
Christian Bak, Mac Gaunaa, Niels Sørensen, Franck Bertagnolio



# Background

## Airfoils designed and tested in the past

- **Risø-A1:** High  $cl$ - $cd$ -ratio, good stalling characteristics, **good roughness sensitivity**
- **Risø-P:** High  $cl$ - $cd$ -ratio, **very good stalling characteristics**, good roughness sensitivity
- **Risø-B1:** Medium  $cl$ - $cd$ -ratio, **high lift**, **very good roughness insensitivity**
- **Risø-C2:** High  $cl$ - $cd$  ratio, high lift, very good roughness insensitivity, **high moment of resistance**



# Status

## Recent designs

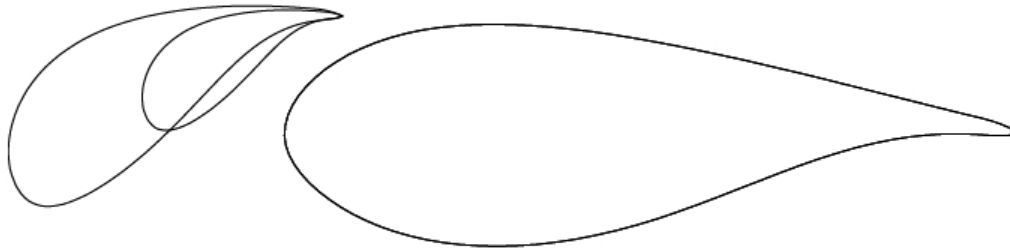
- New aspects taken into account:
  - Trailing edge noise (mainly thin and medium thick airfoils)
    - TNO model
    - Glegg model
  - Thick airfoils with high lift and low sensitivity to roughness
    - Flat back airfoils
    - Multielement airfoils

# Thick multielement airfoils

## Slat size investigation

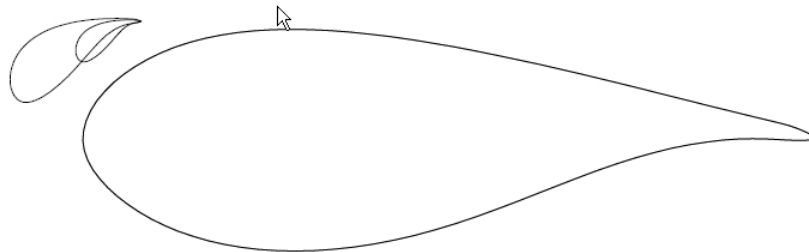
Big slats

0.3c and 0.5c



Small slats

0.1c and 0.2c



# Thick multielement airfoils

## Slat size investigation

Slat/main chord length ratio	$c_{slat}/c_{main}$	0.1	0.2	0.3	0.5
Relative angle of slat	$\beta$	$-30.0^\circ$	$-30.0^\circ$	$-27.5^\circ$	$-27.5^\circ$
Position of slat TE along main airfoil	$s_{TE,slat}$	0.15	0.15	0.15	0.15
Distance between slat TE and main airfoil	$n_{TE,slat}$	0.05	0.05	0.05	0.05
Slat additional parabolic camber	$k_{camber,slat}$	0.1	0.1	0.1	0.1
Lift ratio slat/main airfoil at max $l/d$	$L_{slat}/L_{tot}$	1%	33%	50%	64%
Max lift ratio multiple/isolated main airfoil	$L_{mult}/L_1$	$\sim 1$	$\sim 1.5$	$\sim 2.2$	$>\sim 2.5$

## Further work

- Airfoil designs
  - Thin low noise airfoil will be designed (in EUDP 2009 Low Noise Airfoil project)
  - Final multielement airfoil will be designed
  - Flat back airfoil will be designed
- Wind tunnel tests
  - Multielement airfoil and flat back airfoil will likely be tested in the LM LSWT around summer 2011





Risø DTU is the National Laboratory for Sustainable Energy. Our research focuses on development of energy technologies and systems with minimal effect on climate, and contributes to innovation, education and policy. Risø has large experimental facilities and interdisciplinary research environments, and includes the national centre for nuclear technologies.

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